



# Announcements

Project 1B due Today at 11:00 PM  
Midterm Friday, in class



# More Digital Representation



*Discrete information is represented in binary (PandA), and "continuous" information is made discrete*



## Return To RGB

Images are constructed from picture elements (pixels); color uses RGB light

The RGB color intensities are specified by 3 numbers in the range [0, 255], ie 1 byte each

	Black = [ 0, 0, 0]	0000 0000 0000 0000 0000 0000
	Gray = [128,128,128]	1000 0000 1000 0000 1000 0000
	White = [255,255,255]	1111 1111 1111 1111 1111 1111

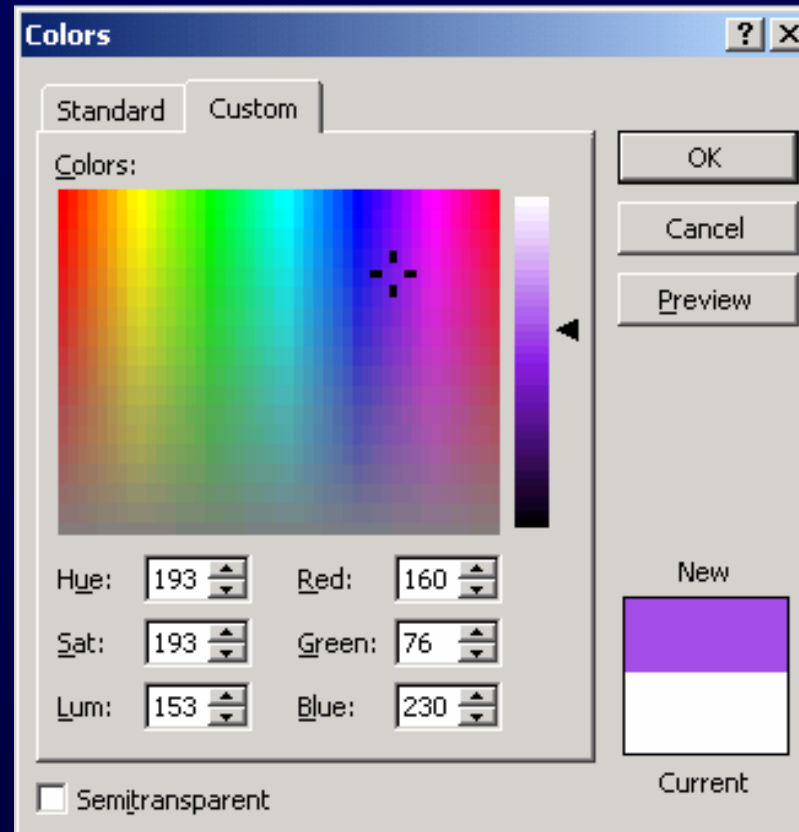
White-gray-black all have same values for RGB



# Colors

Colors use different combinations of RGB

- Husky Purple  
Red=160  
Green=76  
Blue=230





# Positional Notation

The RGB intensities are binary numbers  
Binary numbers, like decimal numbers,  
use *place notation*

$$\begin{aligned} 1101 &= 1 \times 1000 + 1 \times 100 + 0 \times 10 + 1 \times 1 \\ &= 1 \times 10^3 + 1 \times 10^2 + 0 \times 10^1 + 1 \times 10^0 \end{aligned}$$

except that the base is 2 not 10

$$\begin{aligned} 1101 &= 1 \times 8 + 1 \times 4 + 0 \times 2 + 1 \times 1 \\ &= 1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 \end{aligned}$$

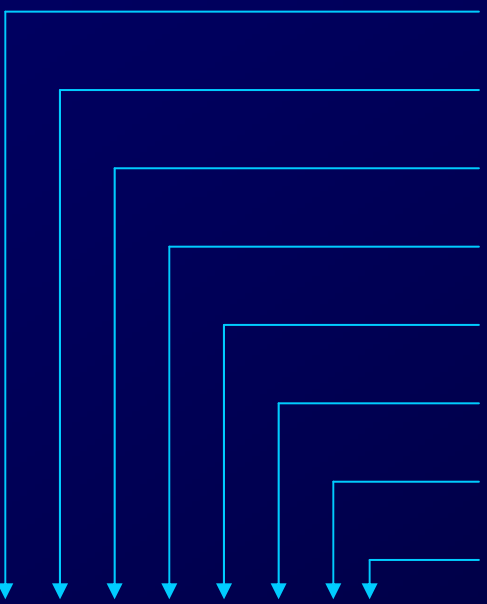
Base or  
radix

1101 in binary is 13 in decimal



# Binary Numbers

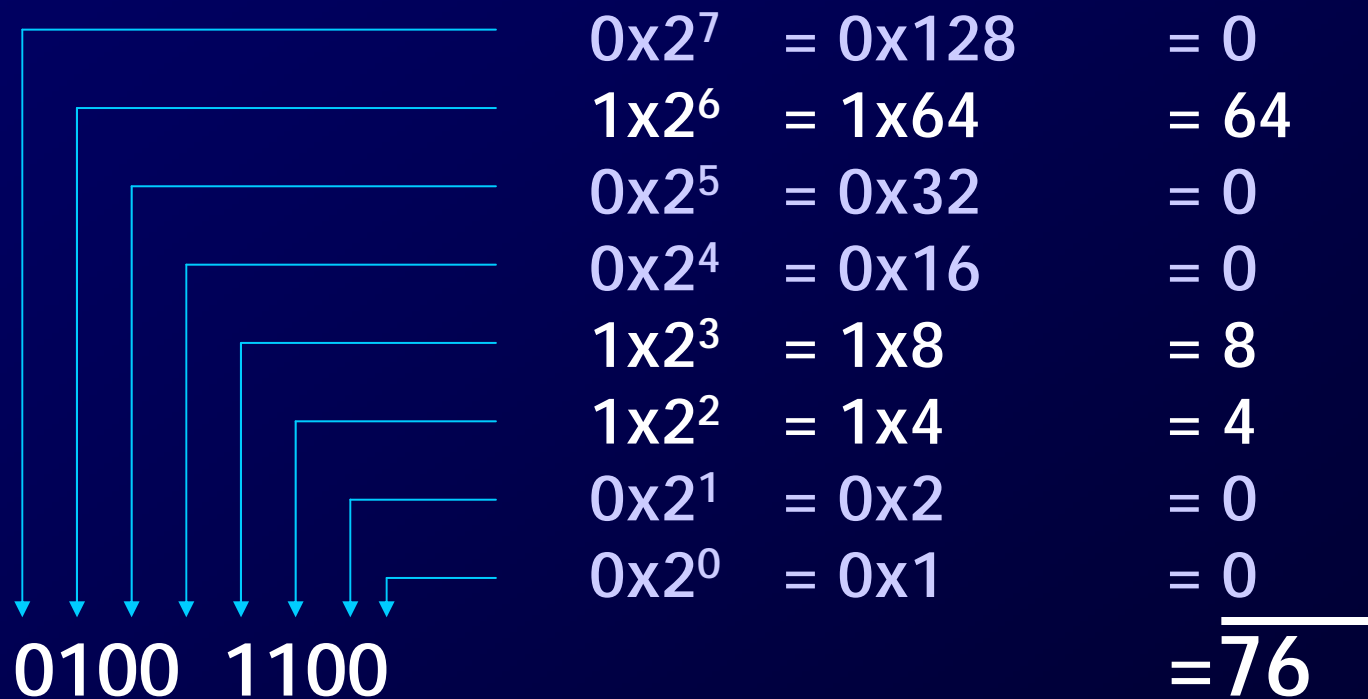
Given a binary number, add up the powers of 2 corresponding to 1s

	$1 \times 2^7 = 1 \times 128$	$= 128$
	$0 \times 2^6 = 0 \times 64$	$= 0$
	$1 \times 2^5 = 1 \times 32$	$= 32$
	$0 \times 2^4 = 0 \times 16$	$= 0$
	$0 \times 2^3 = 0 \times 8$	$= 0$
	$0 \times 2^2 = 0 \times 4$	$= 0$
	$0 \times 2^1 = 0 \times 2$	$= 0$
	$0 \times 2^0 = 0 \times 1$	$= 0$
<b>1010 0000</b>		<b><u>160</u></b>



# Binary Numbers

Given a binary number, add up the powers of 2 corresponding to 1s





# Binary Numbers

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	$1 \times 2^5 = 1 \times 32$	$= 32$
	$0 \times 2^4 = 0 \times 16$	$= 0$
	$0 \times 2^3 = 0 \times 8$	$= 0$
	$1 \times 2^2 = 1 \times 4$	$= 4$
	$1 \times 2^1 = 1 \times 2$	$= 2$
	$0 \times 2^0 = 0 \times 1$	$= 0$
<b>1110 0110</b>		<b><u>230</u></b>





## Husky Purple

Recall that Husky purple is (160,76,230)  
which in binary is

1010 0000 0100 1100 1110 0110  
160 76 230

Suppose you decide it's not "red" enough

- Increase the red by 16 = 1 0000

$$\begin{array}{r} 1010\ 0000 \\ + \quad 1\ 0000 \\ \hline 1011\ 0000 \end{array}$$

Adding in binary is  
pretty much like  
adding in decimal



# A Redder Purple

Increase by 16 more

$$\begin{array}{r} 00110\ 000 \leftarrow \text{Carries} \\ 1011\ 0000 \\ \underline{\quad} + \underline{\quad} 1\ 0000 \\ 1100\ 0000 \\ \quad \uparrow \uparrow \end{array}$$



The rule: When the "place sum" equals the radix or more, subtract radix & carry



# Find Binary From Decimal

Fill in the Table:

Num Being Converted	230	230	102	38	6	6	6	2	0
Place Value	256	128	64	32	16	8	4	2	1
Subtract		102	38	6			2	0	
Binary Num	0	1	1	1	0	0	1	1	0



# Find Binary From Decimal

Place number to be converted into the table; fill place value row with decimal powers of 2

Num Being Converted	230								
Place Value	256	128	64	32	16	8	4	2	1
<i>Subtract</i>									
Binary Num									



# Find Binary From Decimal

Rule: Subtract PV from the number; a positive result gives new number and "1"; otherwise, "0"

Num Being Converted	230 → 230								
Place Value	256	128	64	32	16	8	4	2	1
<i>Subtract</i>									
Binary Num	0								



# Find Binary From Decimal

Rule: Subtract PV from the number; a positive result gives new number and "1"; otherwise, "0"

Num Being Converted	230	→ 230	102						
Place Value	256	128	64	32	16	8	4	2	1
Subtract		102							
Binary Num	0	1							



# Find Binary From Decimal

Rule: Subtract PV from the number; a positive result gives new number and "1"; otherwise, "0"

Num Being Converted	230 → 230	102	38						
Place Value	256	128	64	32	16	8	4	2	1
Subtract		102	38						
Binary Num	0	1	1						



# Find Binary From Decimal

Rule: Subtract PV from the number; a positive result gives new number and "1"; otherwise, "0"

Num Being Converted	230 → 230	102	38	6					
Place Value	256	128	64	32	16	8	4	2	1
Subtract		102	38	6					
Binary Num	0	1	1	1					





# Find Binary From Decimal

Rule: Subtract PV from the number; a positive result gives new number and "1"; otherwise, "0"

Num Being Converted	230 → 230	102	38	6 → 6					
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Rule: Subtract PV from the number; a positive result gives new number and "1"; otherwise, "0"

Num Being Converted	230 → 230	102	38	6 → 6 → 6					
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Rule: Subtract PV from the number; a positive result gives new number and "1"; otherwise, "0"

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Place Value	256	128	64	32	16	8	4	2	1
Subtract		102	38	6			2		
Binary Num	0	1	1	1	0	0	1		



# Find Binary From Decimal

Rule: Subtract PV from the number; a positive result gives new number and "1"; otherwise, "0"

Num Being Converted	230	→ 230	102	38	6	→ 6	→ 6	2	0
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Binary Num	0	1	1	1	0	0	1	1	



# Find Binary From Decimal

Rule: Subtract PV from the number; a positive result gives new number and "1"; otherwise, "0"

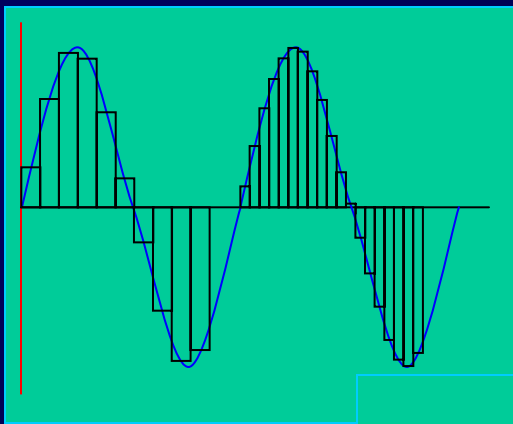
Num Being Converted	230	→ 230	102	38	6	→ 6	→ 6	2	0
Place Value	256	128	64	32	16	8	4	2	1
Subtract		102	38	6			2	0	
Binary Num	0	1	1	1	0	0	1	1	0

Read off the result: 0 1110 0110

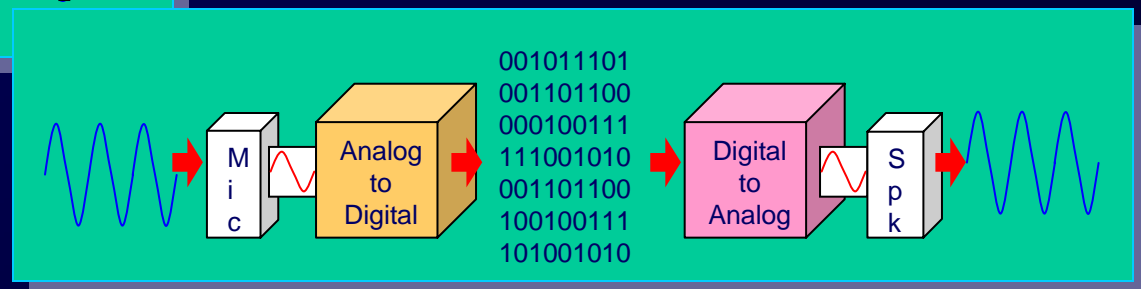


# Digitizing

“Continuous” information like light and sound must be made “discrete”



Digital audio uses 44,100 samples per second of 16 bits on two channels, or 10,584,000 B/min





# Compression

Compression: use fewer bits

JPEG

- \* Lossless – Recover the data
- \* Lossy– Lose the original data



Original

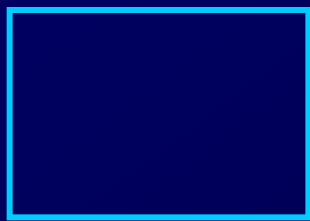


Over compressed



# Run-Length Compression

Give number of 1s, number of 0s, etc.



Forget row encoding ... alternate

[Size: 270x200](542)(266)(4)(266)(4)(266)(4)(266) ...





## Bits Are It

Bits represent information, but their interpretation gives bits meaning

0000 0000 1111 0001 0000 1000 0010 0000

- Could be a number, color, instruction, ASCII, sound samples, IP address, ...

*Bias-free Universal Medium Principle:* Bits can represent all discrete information; bits have no inherent meaning



## Summary

### Bits can represent any information

- \* Discrete information is directly encoded using binary
- \* Continuous information is made discrete
- \* Bias-free Universal Medium Principle