## Deterministic Finite Automaton

Our machine is going to get a string as input. It will read one character at a time and update "its state." At every step, the machine thinks of itself as in one of the (finite number) vertices.
When it reads the character it follows the arrow labeled with that character to its next state.

Start at the "start state" (unlabeled, incoming arrow). After you've read the last character, accept the string if and only if you're in a "final state" (double circle).


## Deterministic Finite Automata

What is the language of this DFA?
I.e. the set of all strings it accepts?

| Old State | 0 | 1 |
| :---: | :---: | :---: |
| $s_{0}$ | $s_{0}$ | $s_{1}$ |
| $s_{1}$ | $s_{0}$ | $s_{2}$ |
| $s_{2}$ | $s_{0}$ | $s_{3}$ |
| $s_{3}$ | $s_{3}$ | $s_{3}$ |



## Design some DFAs

Let $\Sigma=\{0,1,2\}$
$M_{1}$ should recognize "strings with an even number of 2's.
What do you need to remember?
$M_{2}$ should recognize "strings where the sum of the digits is congruent to $0(\bmod 3) "$

The set of binary strings with a 1 in the $3^{\text {rd }}$ position from the start

