How do we know recursion works?

```
//Assume i is a nonnegative integer
//returns 2^i.
public int CalculatesTwoToTheI(int i){
    if(i == 0)
        return 1;
    else
        return 2*CaclulatesTwoToTheI(i-1);
}
Why does CalculatesTwoToTheI(4) calculate 2^4?
Convince the people around you!
```



Making Induction Proofs Pretty

All of our induction proofs will come in 5 easy(?) steps!

- 1. Define P(n). State that your proof is by induction on n.
- 2. Show P(0) i.e. show the base case
- 3. Suppose P(k) for an arbitrary k.
- 4. Show P(k + 1) (i.e. get $P(k) \rightarrow P(k + 1)$)
- 5. Conclude by saying P(n) is true for all n by induction.

More Induction

Induction doesn't **only** work for code! Show that $\sum_{i=0}^{n} 2^{i} = 1 + 2 + 4 + \dots + 2^{n} = 2^{n+1} - 1$. Let $P(n) = \sum_{i=0}^{n} 2^{i} = 2^{n+1} - 1$. We show P(n) holds for all natural numbers n by induction on n. Base Case () Inductive Hypothesis: Inductive Step:

P(n) holds for all $n \ge 0$ by the principle of induction.