Balls, Urns, and the Supreme Court

Supreme Court case: Berghuis v. Smith

If a group is underrepresented in a jury pool, how do you tell?

- Article by Erin Miller Friday, January 22, 2010
- Thanks to Josh Falk for pointing out this article

Justice Breyer [Stanford Alum] opened the questioning by invoking the binomial theorem. He hypothesized a scenario involving **"an urn with a thousand balls, and sixty are red, and nine hundred forty are black, and then you select them at random... twelve at a time."** According to Justice Breyer and the binomial theorem, if the red balls were black jurors then **"you would expect... something like <u>a third to a half of</u> juries would have at least one black person"** on them.

Justice Scalia's rejoinder: "We don't have any urns here."

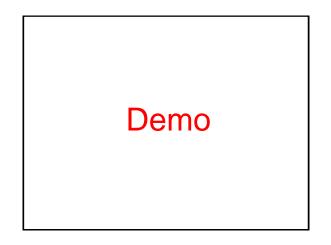
Justice Breyer Meets CS109

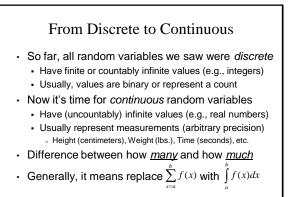
- Should model this combinatorially
 Ball draws not independent trials (balls not replaced)
- Exact solution: P(draw 12 black balls) = $\binom{940}{12} / \binom{1000}{12} \approx 0.4739$

 $P(draw \ge 1 \text{ red ball}) = 1 - P(draw 12 \text{ black balls}) \approx 0.5261$

- Approximation using Binomial distribution
 - Assume P(red ball) constant for every draw = 60/1000
 - X = # red balls drawn. X ~ Bin(12, 60/1000 = 0.06)
 - $P(X \ge 1) = 1 P(X = 0) \approx 1 0.4759 = 0.5240$

In Breyer's description, should actually expect just <u>over half</u> of juries to have at least one black person on them





Continuous Random Variables

• X is a <u>Continuous Random Variable</u> if there is function $f(x) \ge 0$ for $-\infty \le x \le \infty$, such that: $P(a \le X \le b) = \int_{-\infty}^{b} f(x) dx$

$$\mathbf{J}_{a}$$

f is a Probability Density Function (PDF) if:

$$P(-\infty < X < \infty) = \int_{-\infty}^{\infty} f(x) dx = 1$$

