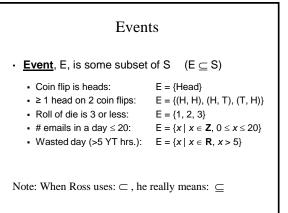
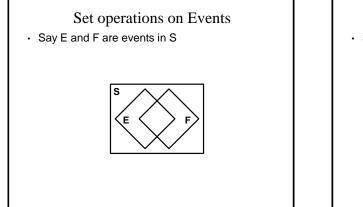
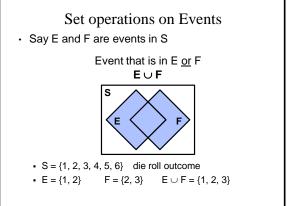
## Sample Spaces

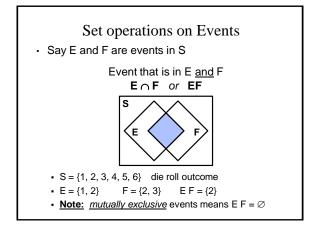
· Sample space, S, is set of all possible outcomes of an experiment

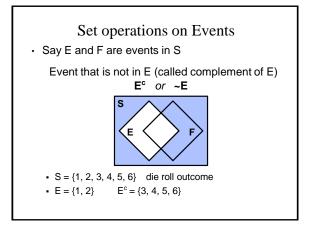
- · Coin flip:
- S = {Head, Tails} • Flipping two coins: S = {(H, H), (H, T), (T, H), (T, T)}
- Roll of 6-sided die: S = {1, 2, 3, 4, 5, 6}
- # emails in a day:  $S = \{x \mid x \in \mathbb{Z}, x \ge 0\}$  (non-neg. ints)
- YouTube hrs. in day:  $S = \{x \mid x \in \mathbb{R}, 0 \le x \le 24\}$

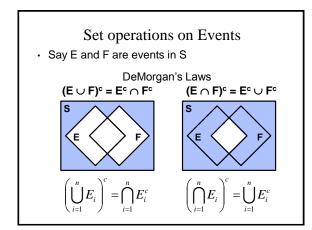


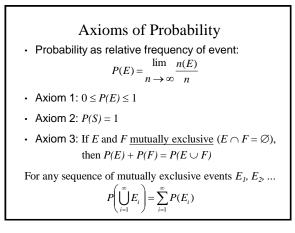


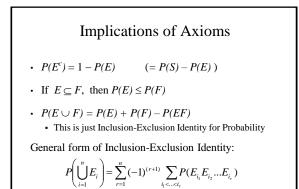


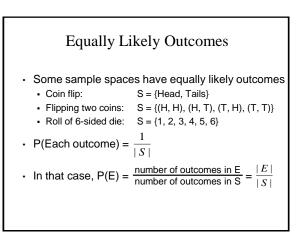


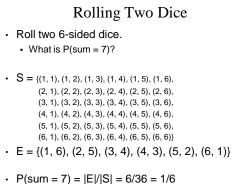


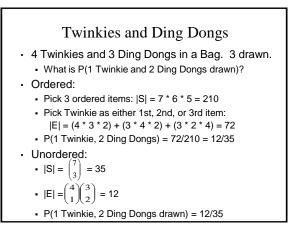


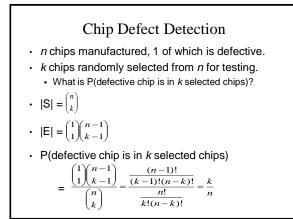


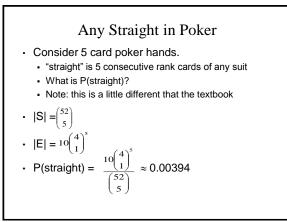


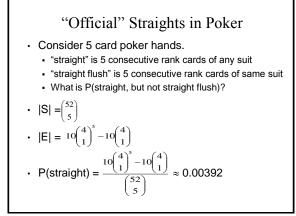


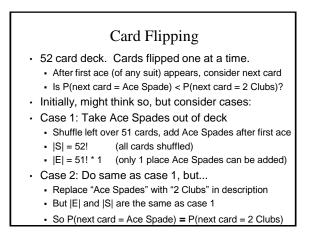


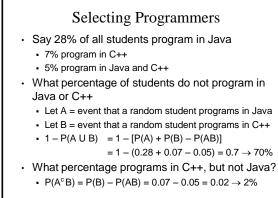












Birthdays • What is the probability that of *n* people, none share the same birthday (regardless of year)? •  $|S| = (365)^n$ • |E| = (365)(364)...(365 - n + 1)• P(no matching birthdays) =  $(365)(364)...(365 - n + 1)/(365)^n$ • Interesting values of *n* • *n* = 23: P(no matching birthdays) < ½ (least such *n*) • *n* = 77: P(no matching birthdays) < 1/5,000 • *n* = 100: P(no matching birthdays) < 1/3,000,000 • *n* = 150: P(no matching birthdays) < 1/3,000,000,000,000

## Birthdays

- What is the probability that of *n* other people, none of them share the same birthday as **vou**?
  - |S| = (365)<sup>n</sup>
  - |E| = (364)<sup>n</sup>
  - P(no birthdays matching yours) = (364)<sup>n</sup>/(365)<sup>n</sup>
- Interesting values of n
  - n = 23: P(no matching birthdays)  $\approx 0.9388$
  - n = 77: P(no matching birthdays)  $\approx 0.8096$ 
    - Anyone born on May 10th?
      Is today anyone's birthday?
  - n = 253: P(no matching birthdays)  $\approx 0.4995$
  - Least such *n* for which P(no matching birthdays) <  $\frac{1}{2}$
  - Why are these probabilities much higher then before?