CSE 312, 2013 Autumn, W.L.Ruzzo

Midterm Review

coverage

everything in text chapters 1-2, slides & homework pre-exam (except "continuous random variables," possibly started today) is included, except as noted below.

mechanics

closed book; 1 page of notes (8.5 x 11, \leq 2 sides, handwritten)

I'm more interested in setup and method than in numerical answers, so concentrate on giving a clear approach, perhaps including a terse English outline of your reasoning.

Corollary: calculators are probably irrelevant, but bring one to the exam if you want, just in case.

counting principle (product rule) permutations combinations indistinguishable objects binomial coefficients binomial theorem partitions & multinomial coefficients inclusion/exclusion

pigeon hole principle

sample spaces & events

axioms

complements, Venn diagrams, deMorgan, mutually exclusive events, etc.

equally likely outcomes

chapter 1: conditional probability and independence

- conditional probability
- chain rule, aka multiplication rule
- total probability theorem
- Bayes rule yes, learn the formula
- odds (and prior/posterior odds form of Bayes rule)
- independence
- conditional independence
- gambler's ruin

- discrete random variables
- probability mass function (pmf)
- expectation of X
- expectation of g(X) (i.e., a function of an r.v.)
- linearity: expectation of X+Y and aX+b
- variance
- cumulative distribution function (cdf)
- cdf as sum of pmf from $-\infty$
- independence; joint and marginal distributions
- important examples: know pmf, mean, variance of these bernoulli, binomial, poisson, geometric, uniform

some important (discrete) distributions

Name	PMF	E[k]	$E[k^2]$	σ^2
Uniform (a, b)	$f(k) = \frac{1}{(b-a+1)}, k = a, a+1, \dots, b$	$\frac{a+b}{2}$		$\frac{\sigma^2}{\frac{(b-a+1)^2-1}{12}}$
Bernoulli(p)	$f(k) = \begin{cases} 1-p & \text{if } k = 0\\ p & \text{if } k = 1 \end{cases}$	p	p	p(1-p)
Binomial(p, n)	$f(k) = \binom{n}{k} p^k (1-p)^{n-k}, k = 0, 1, \dots, n$	np		np(1-p)
Poisson(λ)	$f(k) = e^{-\lambda} \frac{\lambda^k}{k!}, k = 0, 1, \dots$	λ	$\lambda(\lambda+1)$	λ
Geometric(<i>p</i>)	$f(k) = p(1-p)^{k-1}, k = 1, 2, \dots$	$\frac{1}{p}$	$\frac{2-p}{p^2}$	$\frac{1-p}{p^2}$
Hypergeometric (n, N, m)	$f(k) = \frac{\binom{m}{k}\binom{N-m}{n-k}}{\binom{N}{n}}, k = 0, 1, \dots, N$	$\frac{nm}{N}$		$\frac{nm}{N}\left(\frac{(n-1)(m-1)}{N-1} + 1 - \frac{nm}{N}\right)$

See also the summary in B&T following pg 528

Calculus is a prereq, but I'd suggest the most important parts to brush up on are:

taylor's series for e^x

sum of geometric series: $\sum_{i\geq 0} x^i = 1/(1-x)$ (0≤x<1)

Tip: multiply both sides by (1-x)

 $\Sigma_{i\geq 1} ix^{i-1} = 1/(1-x)^2$

Tip1: slide numbered 34 in "random variables" lecture notes, or text Tip2: if it were $\Sigma_{i\geq 1}$ ixⁱ⁺¹, say, you could convert to the above form by dividing by x² etc.; 1st few terms may be exceptions

integrals & derivatives of polynomials, e^x; chain rule for derivatives; integration by parts

Good Luck!