CSE 312 Foundations of Computing II

Lecture 1: Introduction & Counting

https://cs.washington.edu/312

Instructors

Stefano Tessaro [he/him]

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A Team of fantastic TAs



Jan Buzek



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Tanmay Shah



Chloe Winston



Claris Winston



Ben Zhang

See <u>https://cs.washington.edu/312/staff.html</u> to learn more about their backgrounds and interests!

Masking / COVID-19 policy

We follow the UW's <u>Face Covering Policy</u>

- Masking is <u>not</u> required, it is your choice!
 - Exception: Masking is <u>required</u> for a period of at least 10 days for anyone with recent COVID-19 or recent COVID-19 exposure.
- Masking is still recommended, in particular in a crowded setting
- Masking is strongly recommended for the first two weeks of the quarter

Lectures and Sections

Lectures MWF

- 9:30-10:20am (Stefano) or 1:30-2:20pm (Paul)
- Classes will be in person
- Panopto recording and video released after class also, live streaming!
- Annotated slides also uploaded.

Poll Everywhere

- We will sometimes use Poll Everywhere during class
- As of this quarter it requires that you sign up directly
- Sections Thu (starts this week)
 - Not recorded
 - Will prepare you for problem sets!

Go to

- https://www.pollev
- erywhere.com/login and login using <u>YOURNETID@uw.e</u> du

Questions and Discussions

- Office hours throughout the week (starting this <u>Friday</u>)
 - See <u>https://cs.washington.edu/312/staff.html</u>
- Ed Discussion
 - You should have received an invitation (synchronized with the class roaster)
 - Material (resources tab)
 - Announcements (discussion tab)
 - Discussion (discussion tab)

Use Ed discussion forum as much as possible. You can make private posts that only the staff can view! Email instructors for personal issues.

Engagement

- "Concept checks" after each lecture 5-8 %
 - Must be done (on Gradescope) before the next lecture by 9:00am
 - <u>Simple</u> questions to reinforce concepts taught in each class
 - Keep you engaged throughout the week, so that homework becomes less of a hurdle
- 8 Problem Sets (Gradescope) 45-50 %
 - Solved individually. Discussion with others allowed but separate solutions
 - Generally due Wednesdays starting next week
 - First problem set posted this week before section
- Midterm 15-20 %
 - In class on Wednesday, May 4
- Final Exam 30-35 %
 - Monday, June 6 either 2:30-4:20 or 4:30-6:20 location TBA
 - For the A section this is a different time from the one on the UW final exam timetable

Check out the syllabus for policies on late submission for checkpoints and HW

More details see

Course Webpage <u>https://cs.washington.edu/312</u>

Foundations of Computing II

Introduction to Counting, Probability & Statistics

for <u>computer scientists</u>

<u>What</u> is probability?? <u>Why</u> probability?!

Probability is our tool for understanding random processes

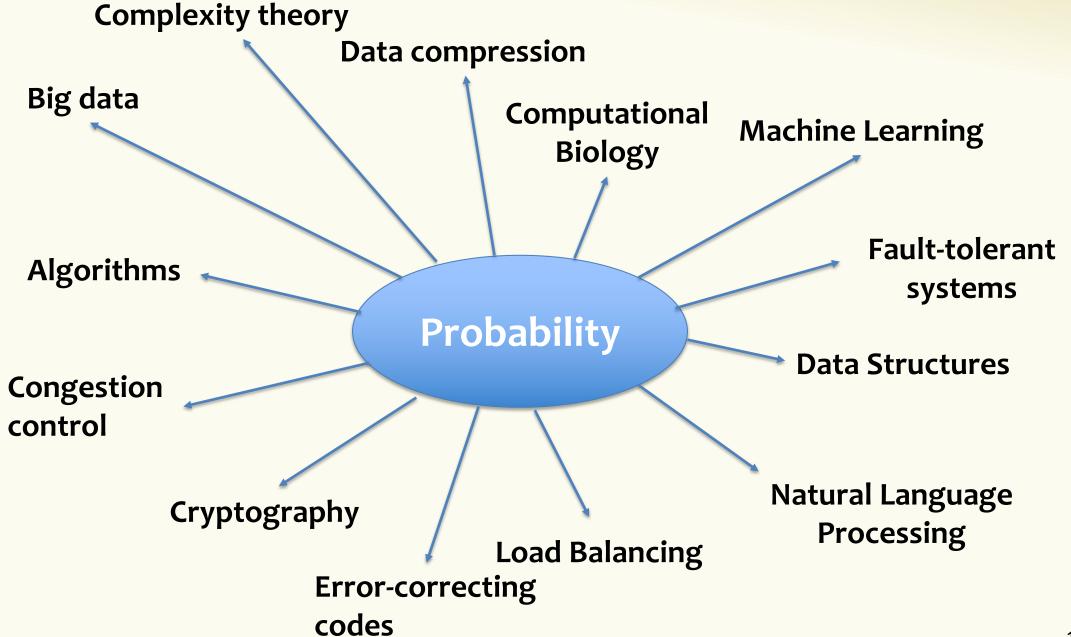
- Randomness in nature and the sciences/social sciences
 - At the quantum level, everything is random
 - Best way to understand and simulate behavior of complex systems
 - A way to design and understand experiments, observations
 - In the lab, the field, medical trials, surveys
- In Computer Science, randomness has these kinds of roles but also important new ones...

Probability and randomness in Computer Science

- Understanding/modelling the inputs to and behavior of our algorithms

 In ML, program testing/fuzzing, algorithm analysis, ...
- Experiments to validate our designs
 - In user studies, HCI, CS applications in other fields, ...
- A tool for hiding information, protecting against adversaries/failures
 - Cryptography, privacy, fault tolerance, computer security, ...
- A tool for simpler and more efficient design
 - Data structures, algorithms, ML, ...

+ much more!



Content

- Counting (basis of discrete probability)
 - Counting, Permutation, Combination, inclusion-exclusion, Pigeonhole Principle
- What is probability
 - Probability space, events, basic properties of probabilities, conditional probability, independence, expectation, variance
- Properties of probability
 - Various inequalities, Zoo of discrete random variables, Concentration, Tail bounds
- Continuous Probability
 - Probability Density Functions, Cumulative Density Functions, Uniform, Exponential, Normal distributions, Central Limit Theorem, Estimation
- Applications
 - A sample of randomized algorithms, differential privacy, learning ...

Today: Counting



We are interested in counting the number of objects with a certain given property.

"How many ways are there to assign 7 TAs to 5 sections, such that each section is assigned to two TAs, and no TA is assigned to more than two sections?"

> "How many positive integer solutions (x, y, z)does the equation $x^3 + y^3 = z^3$ have?"

Generally: Question boils down to computing <u>cardinality</u> |S| of some given set S.

(Discrete) Probability and Counting are Twin Brothers

"What is the probability that a random student from CSE312 has black hair?"

students with black hair

#students



Today – Two basic rules

- Sum rule
- Product rule

Sum Rule

If you can choose from

- EITHER one of *n* options,
- OR one of *m* options with NO overlap with the previous *n*

then the number of possible outcomes of the experiment is

n + m

Counting "lunches"

If a lunch order consists of **either** one of 6 soups **or** one of 9 salads, how many different lunch orders are possible?

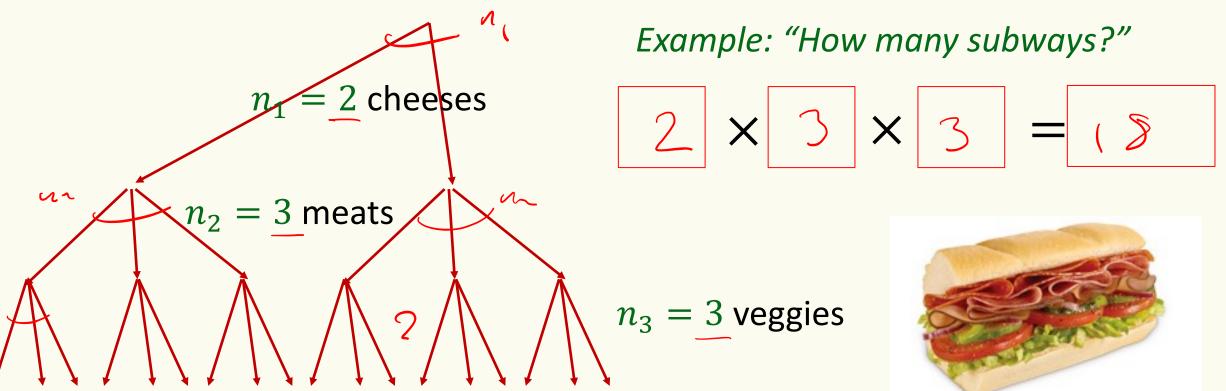




Product Rule: In a sequential process, there are

- n_1 choices for the first step,
- n_2 choices for the second step (given the first choice), ..., and
- n_m choices for the m^{th} step (given the previous choices),

then the total number of outcomes is $n_1 \times n_2 \times \cdots \times n_m$



Product rule example – Laptop customization

Alice wants to buy a new laptop.

- The laptop can be **blue**, **orange**, **purple**, or **silver**.
- The SSD storage can be 128GB, 256GB, and 512GB
- The available RAM can be **8GB** or **16GB**.
- The laptop comes with a 13" or with a 15" screen.

How many different laptop configurations are there?

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Product rule example – Strings

How many string of length 5 over the alphabet $\{A, B, C, ..., Z\}$ are there?

• E.g., AZURE, BINGO, TANGO, STEVE, SARAH, ...

$$26 \times 24 \times 26 \times 26 \times 26 = 26^{S}$$

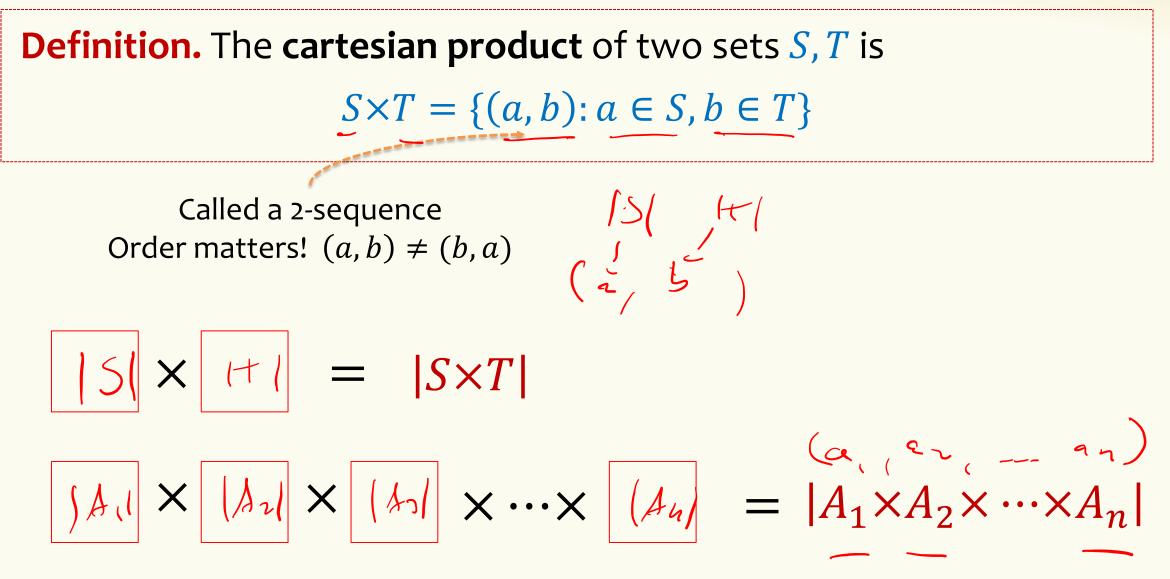
How many binary string of length mover the alphabet {0,1}?

• E.g.,
$$0 \cdots 0, 1 \cdots 1, 0 \cdots 01, \dots$$

2 X 2 X 2 X $\cdots X$ 2 = 2ⁿ

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Product rule example – Cartesian Product



Product rule example – Power set

Definition. The **power set** of S is the set of all subsets of S, $\{X: X \subseteq S\}$. Notations: $\mathcal{P}(S)$ or simply 2^{S} (which we will use).

Example.

$$2^{\{\bigstar,\bigstar\}} = \{\emptyset, \{\bigstar\}, \{\bigstar\}, \{\bigstar, \bigstar\}\}$$
$$2^{\emptyset} = \{\emptyset\}$$

How many different subsets of *S* are there if |S| = n?

Product rule example – Power set

set
$$S = \{e_1, e_2, e_3, \dots, e_n\}$$

subset $X = \{e_1, e_2, e_3, \dots, e_n\}$
 $2 \times 2 \times 2 \times \dots \times 2 = 2^n$
Proposition. $|2^{g}| = 2^{|S|}$

Product rule – One more example

5 books



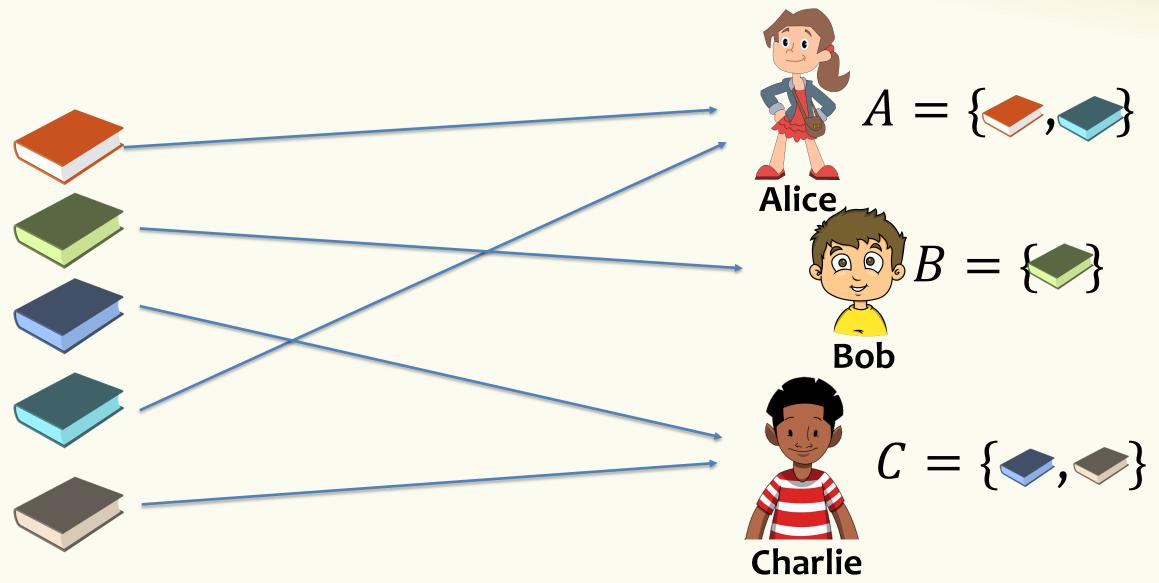


"How many ways are there to distribute 5 books among Alice, Bob, and Charlie?"

Every book to one person, everyone gets ≥ 0 books.



Example Book Assignment

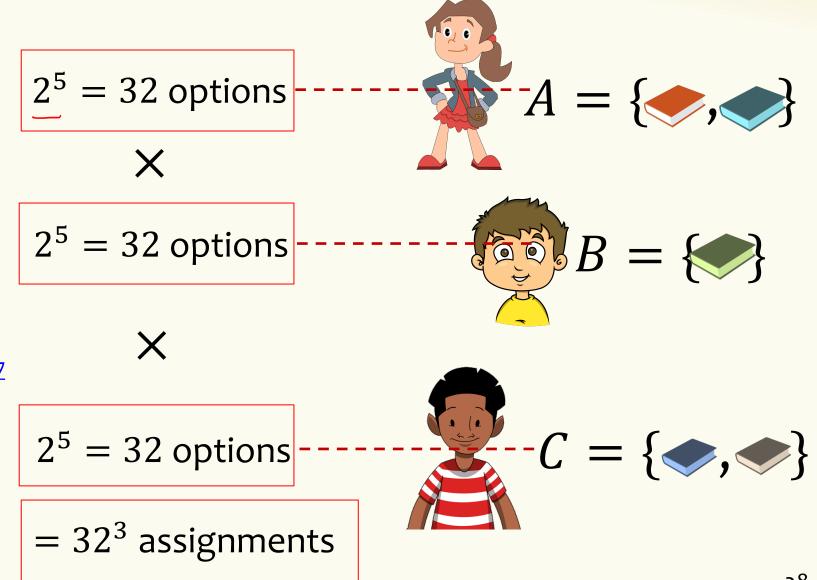


Book assignment – Modeling

Correct? <u>Poll:</u> A. Correct B. Overcount

- C. Undercount
- D. No idea

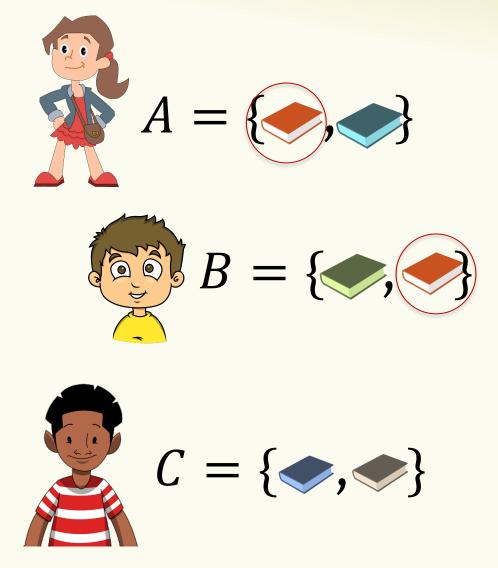
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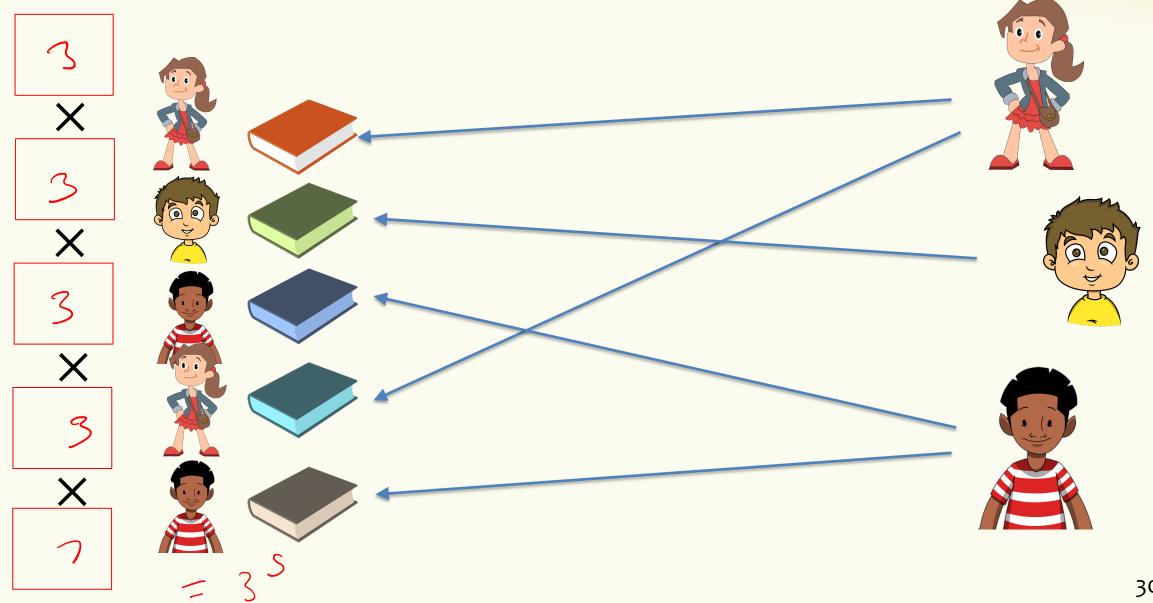
Problem – Overcounting

Problem: We are counting some invalid assignments!!! → overcounting!

What went wrong in the sequential process?After assigning *A* to Alice,*B* is no longer a valid option for Bob



Book assignments – A Clever Approach



Lesson: Representation of what we are counting is very important!

Tip: Use different methods to double check yourself Think about counter examples to your own solution.

The first concept check is out and due 9:00am before the next lecture

The concept checks are meant to help you immediately reinforce what is learned.

Students from previous quarters have found them really useful!