CSE 312: Foundations of Computing II Instructor: Alex Tsun Date: 1/19/22 Lecture Topics: 3.4 Zoo of Discrete RVs I

[Tags: PSet2 Q9, Binomial RV, Linearity of Expectation]

- 1. To determine whether they have llama flu, 1000 people have their blood tested. However, rather than testing each individual separately (1000 tests is quite costly), it is decided to use a group testing procedure:
 - **Phase 1**: First, place people into groups of 5. The blood samples of the 5 people in each group will be pooled and analyzed together. If the test is positive (at least one person in the pool has llama flu), continue to Phase 2. Otherwise send the group home. 200 of these pooled tests are performed.
 - **Phase 2**: Individually test each of the 5 people in the group. 5 of these individual tests are performed per group in Phase 2.

Suppose that the probability that a person has llama flu is 5% for all people, independently of others, and that the test has a 100% true positive rate and 0% false positive rate (note that this is unrealistic). Using this strategy, compute the expected total number of blood tests (individual and pooled) that we will have to do across Phases 1 and 2.

[Tags: Bernoulli RV, Linearity of Expectation]

2. Suppose there is a network of *n* prisoners, and each pair of prisoners are enemies with probability *p*, independently of other pairs. You know the saying "The enemy of my enemy is my friend" (two prisoners are friends if there exists at least one other prisoner who is an enemy to both and they can be friends even if they are enemies). What is the expected number of friendships between pairs of the *n* prisoners?