CSE 321: Discrete Structures Assignment #3 October 15, 2004 Due: Friday, October 22

Reading Assignment: Read Sections 1.6 - 1.8, 2.4, and 2.5.

Problems:

- 1. Section 1.5, exercise 20.
- 2. Section 1.5, exercise 26.
- 3. Section 1.5, exercise 28.
- 4. Prove that for all integers n, n^2 always leaves a remainder of 0 or 1 when divided by 4.
- 5. Section 1.5, exercise 74.
- 6. Prove or disprove that $n^2 + 3n + 1$ is always prime for integer n > 0.
- 7. Prove the following statements using the definitions of set operations and properties:
 - $(A \cap B = A) \to (A \subseteq B)$
 - $(A \subseteq B) \leftrightarrow (\bar{B} \subseteq \bar{A})$
- 8. Extra Credit: Prove that any prime number larger than 3 leaves a remainder of 1 or 5 when divided by 6.