## CSE 321: Discrete Structures

## PROBLEM SET 2 Due Friday, April 16, 2004, in class

**Instructions:** Same as for Problem Set 1.

All exercise numbers refer to the number in Rosen's book, 5th Edition.

- 1. Section 1.3, Exercise 8
- 2. Section 1.3, Exercise 56
- 3. Section 1.4, Exercise 10, parts d,h,i,j.
- 4. Determine the truth value of  $\exists x \forall y (x \leq y^2)$  when the universe of discourse is
  - (a) Positive reals
  - (b) Nonnegative reals
  - (c) Positive integers
  - (d) Nonnegative integers
- 5. Give the negation of each of the following statements (your final answer must be in the form of English sentences):
  - (a) Every number is greater than some number.
  - (b) No students of mathematics are unable to use a computer.
  - (c) Everyone in the class with an Internet connection has emailed at least one other student in the class.
  - (d) All good students study hard.
- 6. Prove or disprove the claim that  $\forall x(P(x) \to Q(x))$  is logically equivalent to  $\forall P(x) \to \forall Q(x)$ .
- 7. Prove the resolution inference rule which states that  $q \lor r$  follows from  $p \lor q$  and  $\neg p \lor r$ , using only the equivalences and basic inference rules described in class and the logic handout.
- 8. Section 1.5, Exercise 12.
- 9. Section 1.5, Exercise 22.