

**Problems:**

1. For the relation  $R = \{(b, c), (b, e), (c, e), (d, a), (e, b), (e, c)\}$  on  $\{a, b, c, d, e, f\}$ , compute the following.
  - (a) The reflexive closure of  $R$ .
  - (b) The symmetric closure of  $R$ .
  - (c) The transitive closure of  $R$ .
  - (d) The reflexive-transitive closure of  $R$ .
2. A relation  $R$  is called *circular* if  $aRb$  and  $bRc$  imply that  $cRa$  for every  $a, b$ , and  $c$ . Prove that  $R$  is reflexive and circular if and only if it is an equivalence relation.
3. Section 8.5, exercise 64 [5th edition: Section 7.5, exercise 50]