

CSE 322 Autumn 2009

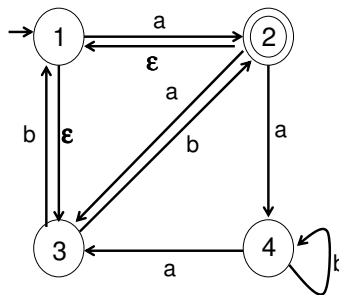
Assignment #2

Due: Friday, October 16, 2009 in class

Reading assignment: Read sections 1.2 and 1.3 of Sipser's book.

Problems:

- For languages A and B over alphabet Σ , let the *perfect shuffle* of A and B be the language $\{w \mid \text{there is some } k \geq 0 \text{ such that } w = a_1b_1 \dots a_kb_k \text{ where } a_1 \dots a_k \in A \text{ and } b_1 \dots b_k \in B, \text{ each } a_i, b_i \in \Sigma.\}$
(That is, it consists of all strings built by taking two strings of equal length from A and B and interleaving them as if they were cards in a perfect shuffle.) Given DFAs that recognize A and B give a brief intuitive description and then a formal description of how to build a DFA that recognizes the perfect shuffle of A and B .
- Sipser's book 2nd edition Problem 1.34 (1st edition Problem 1.27). Document the states of your DFA.
- Draw NFAs with at most 8 states that recognize each of the following languages. Explain why each of your NFAs is correct. (Full state-by-state documentation may be used as part of this explanation but is not required.)
 - The set of all binary strings containing 1001 or 010.
 - The set of all binary strings other than 010 or 101.
- Let $\Sigma = \{a, b\}$. For each $k \geq 1$, let C_k be the language consisting of all strings that contain an 'a' exactly k places from the right-hand end. Thus $C_k = \Sigma^*a\Sigma^{k-1}$. Describe an NFA with $k + 1$ states that recognizes C_k , both in terms of a state diagram and a formal description.
- Apply the subset construction to convert the following NFA to a DFA. Only the states reachable from the start state need to be shown.



6. **(Extra credit)** Sipser's book 2nd edition Problem 1.32 (1st edition Problem 1.25). Document the states of your DFA.
7. **(Extra credit due Oct 23)** Show that if A is recognized by a finite automaton there is a finite automaton that recognizes the set $A_{\frac{1}{2}-}$ of first halves of strings in A , i.e.

$$A_{\frac{1}{2}-} = \{x : xy \in A \text{ for some } y \text{ with } |x| = |y|\}.$$