CSE 326: Data Structures Splay Trees

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AVL Trees Revisited

- Balance condition: For every node x, -1 ≤ balance(x) ≤ 1
 Strong enough : Worst case depth is O(log n)
 Easy to maintain : *one* single or double rotation
 Guaranteed O(log n) running time for
 Find ?
 Insert ?
 - Delete ?
 - buildTree ?

AVL Trees Revisited

- What extra info did we maintain in each node?
- Where were rotations performed?
- How did we locate this node?

Other Possibilities?

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- Could use different balance conditions, different ways to maintain balance, different guarantees on running time, ...
- Why aren't AVL trees perfect?
- Many other balanced BST data structures
 - Red-Black trees
 - AA trees
 - Splay Trees
 - 2-3 Trees
 - **B-Trees**



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Recall: Amortized Complexity

- Is amortized guarantee any weaker than worstcase?
- Is amortized guarantee any stronger than averagecase?
- Is average case guarantee good enough in practice?
- Is amortized guarantee good enough in practice?



Find/Insert in Splay Trees

- 1. <u>Find</u> or <u>insert</u> a node k
- 2. Splay *k* to the root using: zig-zag, zig-zig, or plain old zig rotation

Why could this be good??

- 1. Helps the new root, *k* o *Great if k is accessed again*
- 2. And helps many others!o Great if many others on the path are accessed

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Splaying node *k* to the root: Need to be careful!

One option (that we won't use) is to repeatedly use AVL single rotation until k becomes the root: (see Section 4.5.1 for details)





















But Wait...

What happened here?

Didn't *two* find operations take linear time instead of logarithmic?

What about the amortized O(log *n*) guarantee?

Why Splaying Helps

- If a node *n* on the access path is at depth *d* before the splay, it's at about depth *d*/2 after the splay
- Overall, nodes which are low on the access path tend to move closer to the root
- Splaying gets amortized O(log n) performance. (Maybe not now, but soon, and for the rest of the operations.)

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Practical Benefit of Splaying

- No heights to maintain, no imbalance to check for - Less storage per node, easier to code
- Often data that is accessed once, is soon accessed again!
 - Splaying does implicit caching by bringing it to the root

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Splay Operations: Find

- Find the node in normal BST manner
- Splay the node to the root
 - if node not found, splay what would have been its parent

What if we didn't splay?

Splay Operations: Insert

- Insert the node in normal BST manner
- Splay the node to the root

What if we didn't splay?







