
CSE 331

Software Design & Implementation

Topic: Rep. Exposure; Abstraction Functions

 **Discussion:** How was your long weekend?

Reminders

- Make sure to check Gitlab when submitting
 - must commit, tag, and pass the Gitlab pipeline
- Uploaded replacement recording for Specifications

Upcoming Deadlines

- HW3 due Thursday (7/7)

Last Time...

- Abstract Data Types
- ADTs in Java
 - overview
 - abstract state
 - creators
 - observers
 - producers
 - mutators
- Representation Invariants

Today's Agenda

- Representation Exposure
- Abstraction Functions
- Intro to Testing

Abstract Data Type (ADT)

ADT abstracts from the *organization* to *meaning* of data

- details of data structures are hidden from the client
- client see only the operations that provided

Choose a representation so that:

- it is possible to implement required operations
- the most frequently used operations are efficient / simple / ...
 - abstraction allows the rep to change later
 - almost always better to start simple

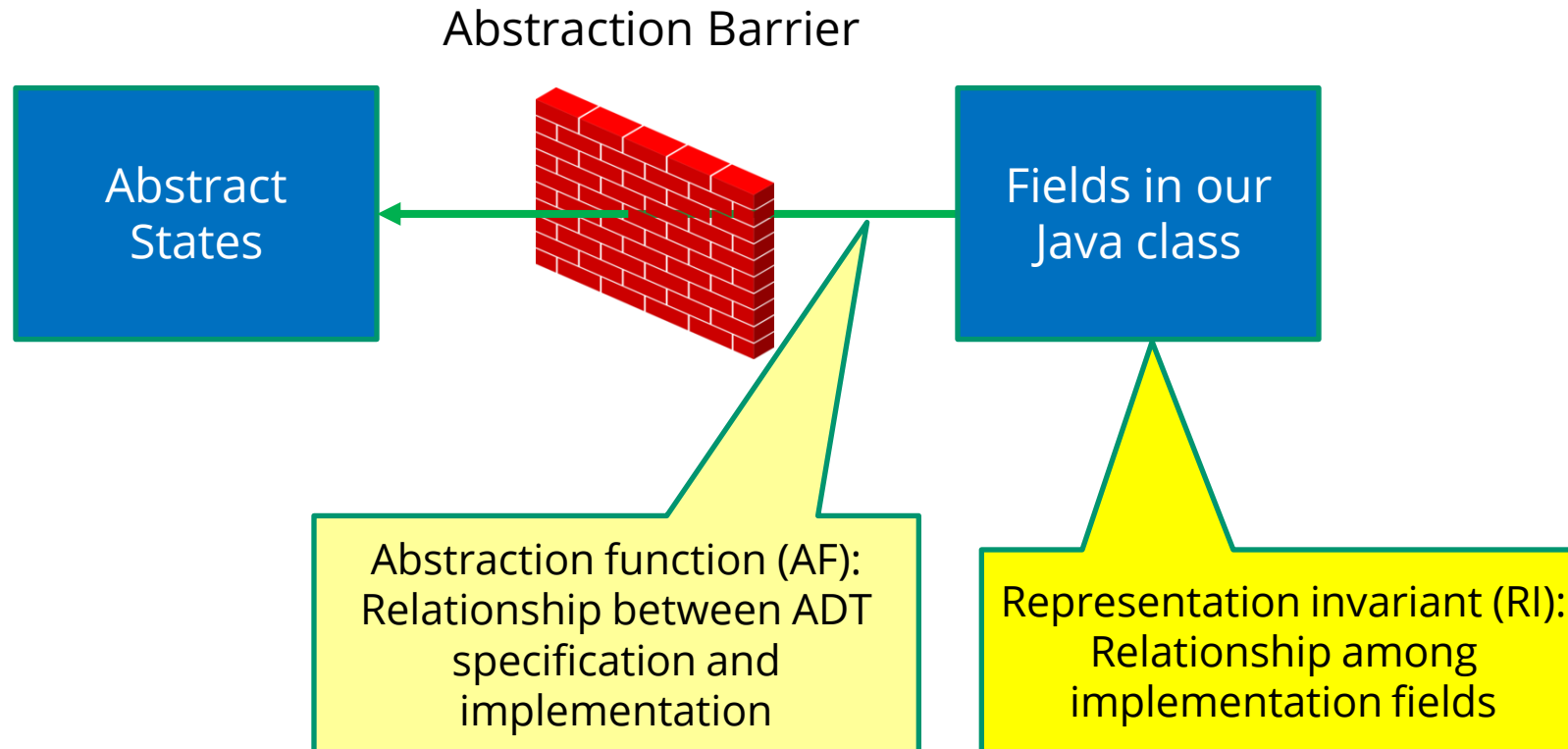
Then use **reasoning** to verify the operations are correct

- two intellectual tools are helpful for this...

Data abstraction outline

ADT specification

ADT implementation



Connecting implementations to specs

For implementers / debuggers / maintainers of the implementation:

Representation Invariant: maps Object \rightarrow boolean

- defines the set of valid concrete values
- must hold before and after any public method is called
- **no object should ever violate the rep invariant**
 - such an object has no useful meaning

Abstraction Function: maps Object \rightarrow abstract state

- we'll discuss this later!

Example: Circle 2

```
/** Represents a mutable circle in the plane. For example,  
 * it can be a circle with center (0,0) and radius 1. */  
public class Circle {  
  
    // Rep invariant: center != null and edge != null  
    //   and !center.equals(edge)  
    private Point center, edge;  
  
    // Abstraction function:  
    // AF(this) = a circle with center at this.center  
    //   and radius this.center.distanceTo(this.edge)  
  
    // ...  
}
```

Example: Polynomial 2

```
/** An immutable polynomial with integer coefficients.
 * Examples include 0, 2x, and x + 3x^2 + 5x. */
public class IntPoly {

    // Rep invariant: terms != null and
    //     no two terms have the same degree and
    //     terms is sorted in descending order by degree
    private final LinkedList<IntTerm> terms;

    // Abstraction function:
    // AF(this) = sum of monomials in this.terms

    // ... coeff, degree, etc.
```

Defensive Programming with ADTs

Checking rep invariants

Remember that representation invariants should hold before and after each method in the public specification.

Should you write code to check that the rep invariant holds?

- Yes, if it's inexpensive [depends on the invariant]
- Yes, for debugging [even when it's expensive]
- Often hard to justify turning the checking off
 - better argument is removing clutter (improve understandability)

A great debugging technique:

Catch bugs by implementing and using a function to check the rep-invariant

Example: CharSet ADT

```
// Overview: A CharSet is a finite mutable set of Characters
// @effects: creates a fresh, empty CharSet
public CharSet() {...}

// @modifies: this
// @effects: this changed to this + {c}
public void insert(Character c) {...}

// @modifies: this
// @effects: this changed to this - {c}
public void delete(Character c) {...}

// @return: true iff c is in this set
public boolean member(Character c) {...}

// @return: cardinality of this set
public int size() {...}
```

Example: CharSet ADT

```
// Rep invariant: elts != null and  
//           elts has no nulls and no dups  
// AF(this) = list of chars in elts  
private List<Character> elts;
```

Checking the rep invariant

How do we check whether this invariant holds?

```
public void delete(Character c) {  
  
    elts.remove(c); // removes 0 or 1 copies of c  
  
}
```

Checking the rep invariant

Rule of thumb: check on entry *and* on exit (why?)

```
public void delete(Character c) {
    checkRep();
    elts.remove(c); // removes 0 or 1 copies of c
    checkRep();
}

// Verify that elts contains no nulls or dups
private void checkRep() {
    assert elts != null;
    for (int i = 0; i < elts.size(); i++) {
        assert elts.get(i) != null;
        assert elts.indexOf(elts.get(i)) == i;
    }
}
```

Practice *defensive programming*

- Question is not: will you make mistakes? You will.
- Question is: will you **catch** those mistakes before users do?
- Write and incorporate code designed to catch the errors you make
 - check rep invariant on entry and exit (of mutators)
 - check preconditions (don't trust other programmers)
 - check postconditions (don't trust yourself either)
- Checking the rep invariant helps *discover* errors while testing
- Reasoning about the rep invariant helps *discover* errors while coding

Practice *defensive programming*

- Checking pre- and post-conditions and rep invariants is one tip
- More of these in Effective Java
 - first required reading (see calendar for items)
- Focus on defensive programming against **subtle bugs**
 - obvious bugs (e.g., crashing every time) will be caught in testing
 - subtle bugs that only occasionally cause problems can sneak out
 - be especially defensive against (and scared of) these

Listing the elements of a CharSet

Consider adding the following method to `CharSet`

```
// returns: a List containing the members of this  
public List<Character> getElts();
```

Consider this implementation:

```
public List<Character> getElts() { return elts; }
```

Does this implementation preserve the rep invariant?

Can't say!

Representation exposure

Consider this client code (outside the `CharSet` implementation):

```
CharSet s = new CharSet();  
Character a = new Character('a');  
s.insert(a);  
s.getElts().add(a);  
s.delete(a);  
if (s.member(a)) ...
```

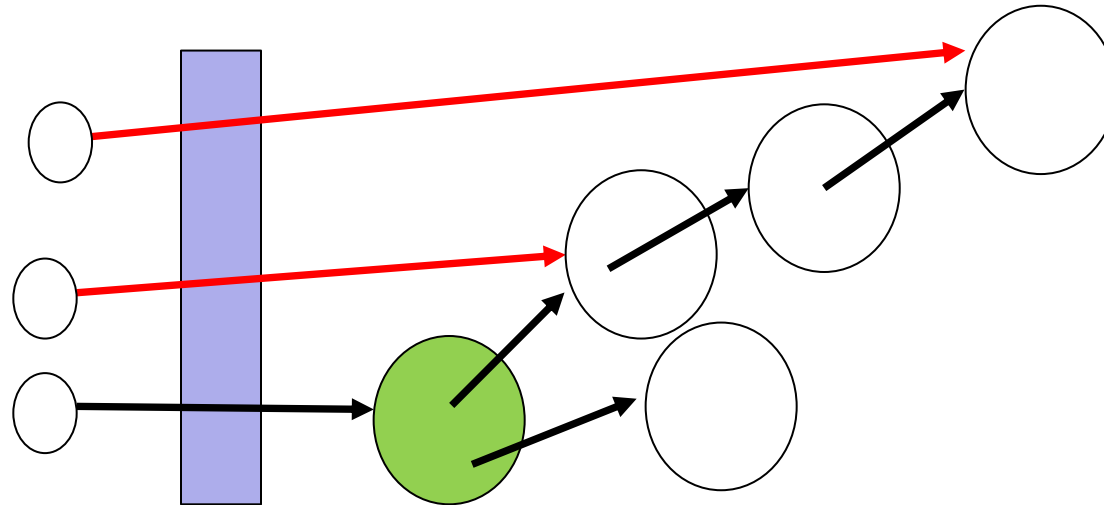
- [Representation exposure](#) is external access to the rep
- Representation exposure is almost always **bad**
 - can cause bugs that will be **very hard to detect**
- Rule #1: Don't do it!
- Rule #2: If you do it, document it clearly and then feel guilty about it!

Avoiding representation exposure

- *Understand* what representation exposure is
- *Design* ADT implementations to make sure it doesn't happen
- Treat rep exposure as a bug: *fix* your bugs
 - absolutely must avoid in libraries with many clients
 - can allow (but feel guilty) for code with few clients
- *Test* for it with *adversarial clients*:
 - pass values to methods and then mutate them
 - mutate values returned from methods

private is not enough

- Making fields **private** does *not* suffice to prevent rep exposure
 - see our example
 - issue is ***aliasing of mutable data outside the abstraction***



- So **private** is a hint to you: no aliases outside abstraction to references to mutable data reachable from **private** fields
- Three general ways to avoid representation exposure...

Avoiding rep exposure (way #1)

- One way to avoid rep exposure is to make **copies** of all data that cross the abstraction barrier
 - Copy in [parameters that become part of the implementation]
 - Copy out [results that are part of the implementation]
- Examples of copying (assume **Point** is a mutable ADT):

```
class Line {  
    private Point s, e;  
    public Line(Point s, Point e) {  
        this.s = new Point(s.x, s.y);  
        this.e = new Point(e.x, e.y);  
    }  
    public Point getStart() {  
        return new Point(this.s.x, this.s.y);  
    }  
}
```

...

Avoiding rep exposure (way #2)

- One way to avoid rep exposure is to exploit the **immutability** of (other) ADTs the implementation uses
 - aliasing is no problem if nobody can change data
 - have to mutate the rep to break the rep invariant
- Examples (assuming `Point` is an *immutable* ADT):

```
class Line {  
    private Point s, e;  
    public Line(Point s, Point e) {  
        this.s = s;  
        this.e = e;  
    }  
    public Point getStart() {  
        return this.s;  
    }  
    ...  
}
```

Alternative #3

```
// returns: elts currently in the set
public List<Character> getElts() { // version 1
    return new ArrayList<Character>(elts); //copy out!
}

public List<Character> getElts() { // version 2
    return Collections.unmodifiableList(elts);
}
```

From the JavaDoc for `Collections.unmodifiableList`:

*Returns an unmodifiable view of the specified list. This method allows modules to provide users with "read-only" access to internal lists. Query operations on the returned list "read through" to the specified list, and attempts to modify the returned list... result in an **UnsupportedOperationException**.*

The good news

```
public List<Character> getElts() { // version 2
    return Collections.unmodifiableList(elts);
}
```

- Clients cannot *modify (mutate)* the rep
 - cannot break the rep invariant
- (For long lists,) more efficient than copy out
- Uses standard libraries

The bad news

```
public List<Character> getElts() { // version 1
    return new ArrayList<Character>(elts); //copy out!
}
```

```
public List<Character> getElts() { // version 2
    return Collections.unmodifiableList(elts);
}
```

The two implementations do not do the same thing!

- both avoid allowing clients to break the rep invariant
- both return a list containing the elements

But consider:

```
xs = s.getElts();
s.insert('a');
xs.contains('a');
```

Version 2 is *observing* an exposed rep, leading to different behavior

Different specifications

Ambiguity of “returns a list containing the current set elements”

“returns a fresh mutable list containing the elements in the set *at the time of the call*”

vs.

“returns read-only access to a list that the ADT *continues to update to hold the current elements in the set*”

A third spec weaker than both [but less simple and useful!]

“returns a list containing the current set elements. *Behavior is unspecified (!) if client attempts to mutate the list or to access the list after the set’s elements are changed*”

Also note: Version 2’s spec also makes changing the rep later harder

- only “simple” to implement with rep as a **List**

Suggestions

Best options for implementing `getEltS()`

- if $O(n)$ time is acceptable for relevant use cases, copy the list
 - safest option
 - best option for changeability
- if $O(1)$ time is required, then return an unmodifiable list
 - prevents breaking rep invariant
 - clearly document that behavior is unspecified after mutation
 - ideally, write your own unmodifiable view of the list that throws an exception on all operations after mutation
- if $O(1)$ time is required and there is no unmodifiable version and you don't have time to write one, expose rep and feel guilty

Abstraction Functions

Specifying an ADT

Different types of operations:

1. **creators**
2. **observers**
3. **producers**
4. **mutators** (if mutable)

Described in terms of how they change the **abstract state**

- abstract description of what the object means
 - difficult (unless concept is already familiar) but vital
- specs have no information about concrete representation
 - leaves us free to change those in the future

Connecting implementations to specs

For implementers / debuggers / maintainers of the implementation:

Representation Invariant: maps Object \rightarrow boolean

- we saw this earlier!

Abstraction Function: maps Object \rightarrow abstract state

- says what the data structure *means* in vocabulary of the ADT
- maps the fields to the abstract state they represent
 - can check that the abstract value after each method meets the postcondition described in the specification

Example: Circle

```
/** Represents a mutable circle in the plane. For example,  
 * it can be a circle with center (0,0) and radius 1. */  
public class Circle {  
  
    // Rep invariant: center != null and rad > 0  
    private Point center;  
    private double rad;  
  
    // Abstraction function:  
    // AF(this) = a circle with center at this.center  
    //   and radius this.rad  
  
    // ...  
}
```

Example: Circle 2

```
/** Represents a mutable circle in the plane. For example,  
 * it can be a circle with center (0,0) and radius 1. */  
public class Circle {  
  
    // Rep invariant: center != null and edge != null  
    //   and !center.equals(edge)  
    private Point center, edge;  
  
    // Abstraction function:  
    // AF(this) = a circle with center at this.center  
    //   and radius this.center.distanceTo(this.edge)  
  
    // ...  
}
```


Example: Polynomial

```
/** An immutable polynomial with integer coefficients.
 * Examples include 0, 2x, and x + 3x^2 + 5x. */
public class IntPoly {

    // Rep invariant: coeffs != null
    private final int[] coeffs;

    // Abstraction function:
    // AF(this) = sum of this.coeffs[i] * x^i
    //   for i = 0 .. this.coeffs.length

    // ... coeff, degree, etc.
```

Example: Polynomial 2

```
/** An immutable polynomial with integer coefficients.
 * Examples include 0, 2x, and x + 3x^2 + 5x. */
public class IntPoly {

    // Rep invariant: terms != null and
    //     no two terms have the same degree and
    //     terms is sorted in descending order by degree
    private final LinkedList<IntTerm> terms;

    // Abstraction function:
    // AF(this) = sum of monomials in this.terms

    // ... coeff, degree, etc.
```

The abstraction function

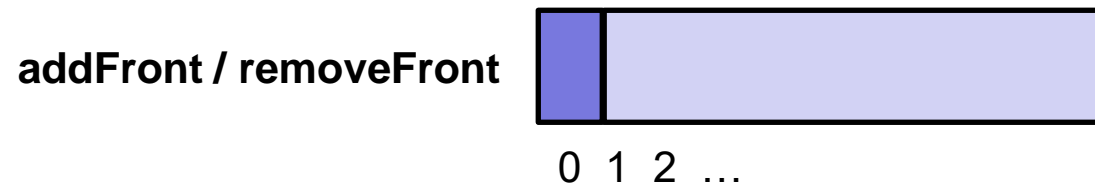
- Purely conceptual (not a Java function)
- Allows us to check correctness
 - use reasoning to show that the method leaves the abstract state such that it satisfies the postcondition

Example: IntDeque

// List that only allows insert/remove at ends.



addLast / removeLast



addFront / removeFront

Example: IntDeque

// List that only allows insert/remove at ends.

addLast



removeFront



Example: IntDeque

// List that only allows insert/remove at ends.



addLast + removeFront



addLast + removeFront

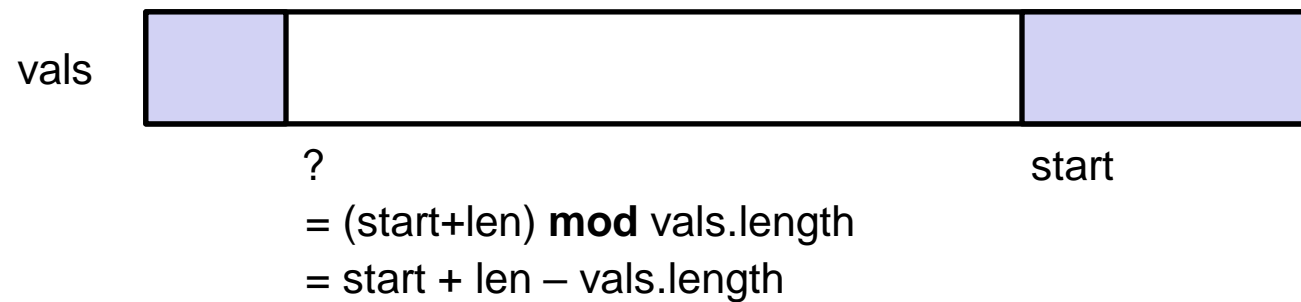


addLast + removeFront



Example: IntDeque

```
// List that only allows insert/remove at ends.
```



Example: IntDeque

```
/** List that only allows insert/remove at ends. */
public class IntDeque {

    // AF(this) =
    //   vals[start..start+len-1]   if start+len <= vals.length
    //   vals[start..] + vals[0..?] otherwise
    private int[] vals;
    private int start, len;

    // Creates an empty list.
    public IntDeque() {
        vals = new int[3];
        start = len = 0;
    }
}
```

← AF(this) = vals[0..-1] = []

Example: IntDeque

```
/** List that only allows insert/remove at ends. */
public class IntDeque {

    // AF(this) =
    //   vals[start..start+len-1]    if start+len <= vals.length
    //   vals[start..] + vals[0..?]  otherwise
    private int[] vals;
    private int start, len;

    // ...

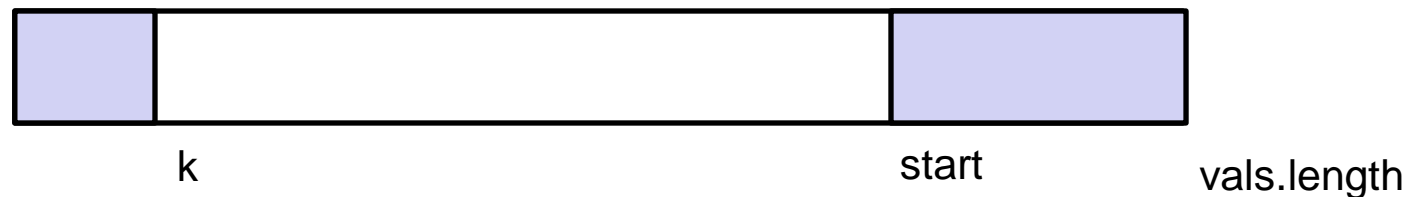
    // @returns length of the list
    public int getLength() {
        return len;
    }
}
```

Example: IntDeque

```
// List that only allows insert/remove at ends.
```



#items = len



#items = vals.length - (start - k) (= len?)

holds iff $k = \text{start} + \text{len} - \text{vals.length}$

Example: IntDeque

```
/** List that only allows insert/remove at ends. */
```

```
public class IntDeque {
```

```
    // AF(this) =
```

```
    //    vals[start..start+len-1]    if start+len <= vals.length
```

```
    //    vals[start..] + vals[0..k]  otherwise
```

```
private int[] vals;
```

```
private int start, len;
```

```
    // ...
```

```
    // @returns length of the list
```

```
public int getLength() {
```

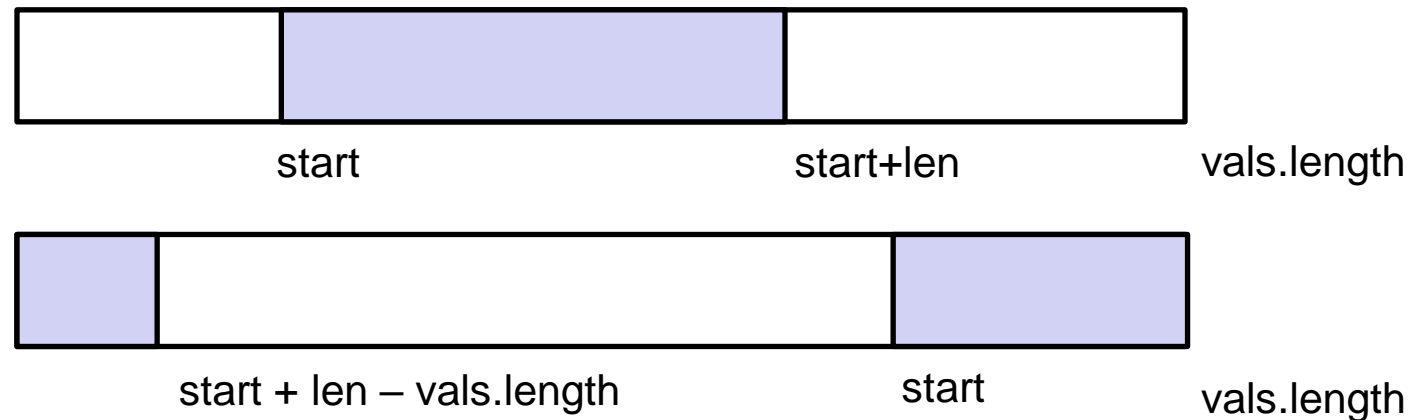
```
    return len;
```

```
}
```

**1 line of code
but 2 cases for reasoning**

Example: IntDeque

```
/** List that only allows insert/remove at ends. */  
public class IntDeque {  
  
    // @requires 0 <= i < length  
    // @returns this[i]  
    public int get(int i) { ... }  
}
```



Example: IntDeque

```
/** List that only allows insert/remove at ends. */
public class IntDeque {

    // @requires 0 <= i < length
    // @returns this[i]
    public int get(int i) {
        if (start + len <= vals.length) {
            return vals[start + i];
        } else {
            return vals[(start + i) % vals.length];
        }
    }
}
```

Example: IntDeque

```
/** List that only allows insert/remove at ends. */  
public class IntDeque {  
  
    // @requires 0 <= i < length  
    // @returns this[i]  
    public int get(int i) {  
        return vals[(start + i) % vals.length];  
    }  
}
```

Example: IntDeque

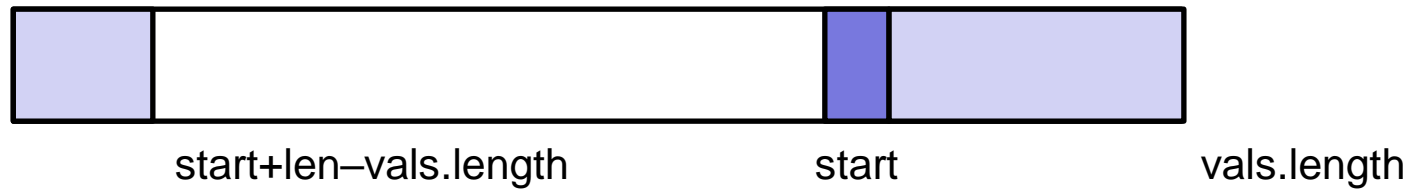
```
/** List that only allows insert/remove at ends. */  
public class IntDeque {  
  
    // @requires list length > 0  
    // @modifies this  
    // @effects first element of list is removed  
    // @returns value at the front of the list  
    public int removeFront() { ... }  
}
```

Example: IntDeque

```
// List that only allows insert/remove at ends.
```



removeFront



Example: IntDeque

```
// AF(this) =  
//   vals[start..start+len-1]   if start+len <= vals.length  
//   vals[start..] + vals[0..k] otherwise  
  
// @requires list length > 0  
// @modifies this  
// @effects first element of list is removed  
public void removeFront() {  
    if (start + 1 < vals.length) {  
        start += 1;  
    } else {  
        start = 0;  
    }  
    len -= 1;  
}
```

Example: IntDeque

```
// AF(this) =
//   vals[start..start+len-1]   if start+len <= vals.length
//   vals[start..] + vals[0..k] otherwise

// @requires list length > 0
// @modifies this
// @effects first element of list is removed
public void removeFront() {
    start = (start + 1) % vals.length;
    len -= 1;
}
```

Example: IntDeque

```
// AF(this) =  
//   vals[start..start+len-1]    if start+len <= vals.length  
//   vals[start..] + vals[0..k]  otherwise  
  
// @requires list length > 0  
// @modifies this  
// @effects first element of list is removed  
// @returns value at the front of the list  
public int removeFront() {  
    int val = get(0);  
    start = (start + 1) % vals.length;  
    len -= 1;  
    return val;  
}
```

Before next class...

1. Start on [Prep. Quiz: HW4](#) as early as possible!
 - Reminds you about common set operations
 - E.g. union, intersection, complement
 - Think about some non-trivial cases needed for the homework
2. Section tomorrow will focus on [HW4](#) preparation.

Extra: Abstract Interpretation

- Abstraction functions are good for much more (e.g. program analysis)

Extra: Testing

- What is testing? What makes something a good test case?