# CSE 331: Software Design & Engineering Midterm: Section A

Spring 2023 5/19/2023 10:30am

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This exam contains 9 pages (including this cover page) and 4 problems. Check to see if any pages are missing. Enter all requested information on the top of this page.

### Instructions:

- Closed book, closed notes, no cell phones, no calculators.
- You have **50 minutes** to complete the exam.
- Answer all problems on the exam paper.
- If you need extra space use the back of a page.
- Problems are not of equal difficulty; if you get stuck on a problem, move on.
- It may be to your advantage to read all the problems before beginning the exam.

Problem	Points	Score
1	18	
2	18	
3	28	
4	16	
Total:	80	

The following function findIndex searches for a string in an array of strings that is promised to be sorted in **decreasing** order. In other words, we are promised that  $A[0] \ge A[1] \ge \cdots \ge A[n-1]$ , where the ordering of strings is according to >= in TypeScript, (reverse) alphabetical ordering.

```
/**
 * Finds the index where x appears in the given sorted array or where, if
 * it is not in the array, it could be inserted to maintain sorted order.
 * @param A Array of strings in *decreasing* order
 * @param x String to look for in a.
 * @returns an integer k such that A[j] > x for any 0 <= j < k and
 * x >= A[j] for any k <= j < A.length
 */
function findIndex(A: string[], x: string): number</pre>
```

Suppose that the function returns k. If x is in the array, then we must have A[k] = x. If x is not in the array, then we must have  $(k = n \text{ or } k \ge 0)$  and  $A[k] \ne x$ .

For example, suppose that A is the array ["mouse", "dog", "dog", "cat"]. Then, the specification above tells us that

- A call to findIndex(A, "zebra") would return 0.
- A call to findIndex(A, "dog") would return 1 (not 2).
- A call to findIndex(A, "cat") would return 3.
- A call to findIndex(A, "bat") would return 4.
- A call to findIndex(A, "kangaroo") would return 1.

#### 1. (18 points) Loop, There It Is

Consider the following code, which claims to implement findIndex from the prior page.

The precondition is that  $A[j] \ge A[j+1]$  for any  $0 \le j < n-1$ , where n is A.length.

let k: number = A.length; {{  $P_1$ : \_\_\_\_\_}}} {{ **Inv:**  $x \ge A[j]$  for any  $k \le j < n$  and  $k \ge 0$  }} while (k !== 0 && x >= A[k - 1]) { {{  $P_2$ : \_\_\_\_\_}}} {{  $Q_2$ : \_\_\_\_\_}}} k = k - 1; {{ \_\_\_\_\_}} {{ \_\_\_\_\_}}} {{  $Q_2$ : \_\_\_\_\_}}} k = k - 1; {{ \_\_\_\_\_}} {{ \_\_\_\_\_}}} {{  $Q_3$ : A[j] > x for any  $0 \le j < k$  and  $x \ge A[j]$  for any  $k \le j < n$  }} return k;

- (a) Use reasoning to fill in all blank assertions above. The ' $P_i$ 's should be filled in with forward reasoning and the ' $Q_i$ 's should be filled in with backward reasoning.
- (b) Prove that  $P_1$  implies Inv.

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(c) Prove that  $P_2$  implies  $Q_2$ .

(d) Prove that  $P_3$  implies  $Q_3$ .

## 2. (18 points) Give It Your Test Shot

Fill in the body of the following unit test for findIndex. Include comments explaining the test cases, as we did in the coding homework problems.

<pre>it('findIndex', function() {     //</pre>	
assert.deepStrictEqual(	
findIndex(	_,),
);	
//	
assert.deepStrictEqual(	
findIndex(	_,),
);	
//	
assert.deepStrictEqual(	
findIndex(	_,),
);	
//	
assert.deepStrictEqual(	
findIndex(	_,),
);	
//	
assert.deepStrictEqual(	
findIndex(	_,),
);	
//	
assert.deepStrictEqual(	
findIndex(	_,),
);	
}	

The remaining problems involve the implementation of the following ADT:

```
/** An array of strings with no duplicates. */
interface StringSet {
  /**
   * Returns a set that includes all the current elements and x also
   * Oparam x a string to insert into the set (if not already present)
   * @returns obj if contains(obj, x) = T
                  if contains(obj, x) = F
              L
   *
   *
         where L = A ++ [x] ++ B with obj = A ++ B (i.e., L is an array
         containing the strings from obj with x inserted somewhere)
   *
   */
   insert(x: string): StringSet;
  /**
   * Returns the largest string in the set
   * @requires obj.length > 0
   * @returns max(obj), where max is defined on non-empty lists by
                 max([y]) := y
   *
           \max(A ++ [y]) := \max(A)
                                      if y < max(A)
   *
   *
           max(A ++ [y]) := y
                                      if y \ge max(A)
   */
 max(): string;
}
```

We will implement it with the following class, whose concrete representation is an array sorted in decreasing order.

```
class ArrayStringSet implements StringSet {
    // RI: elems[j] > elems[j+1] for any 0 <= j < elems.length - 1
    // AF: obj = this.elems
    readonly elems: readonly string[];
    // @requires elems is sorted in decreasing order, with no duplicates
    constructor(elems: readonly string[]) {
      this.elems = elems;
    }
    ...
}</pre>
```

#### 3. (28 points) Run Array! Run Array!

Fill in the missing parts of the implementation of insert. Your code must be correct with the **provided invariants**. (You do not need to turn in a proof, but it must be correct.)

```
insert = (x: string): StringSet => {
   const k = findIndex(this.elems, x);
   if (_____) {
     return this;
   }
   // Create an array one longer than this.elems.
   const E: string[] = new Array(this.elems.length + 1);
   // Define A := this.elems[0 .. k-1] as shorthand.
   let i: number =
   // Inv: E[0 .. i - 1] = A[0 .. i - 1]
   // (so E[0 .. i - 1] stores the first i elements from A)
   while (_____) {
   }
   // Now have E[0 \dots i - 1] = A and i = k
   // (so E[0 .. i - 1] now stores all of A)
   // Now have E[0 ... i - 1] = A ++ [x] and i = k + 1
   // (so E[0 .. i - 1] now stores all of A followed by x)
(Continued on next page...)
```

// Now have E[0 .. i - 1] = A ++ [x] and i = k + 1 (from previous page)
// Define B := this.elems[k .. this.elems.length-1] as shorthand.
// With these definitions, we have this.elems = A ++ B.
let j: number =
// Inv: E[0 .. i - 1] = A ++ [x] ++ B[0 .. j - 1] and i = k + 1 + j
// (so E[0 .. i - 1] now stores all of A, followed by x, followed by
// the first j elements of B)
while (\_\_\_\_\_\_\_) {

}

```
// Now have E[0 .. i - 1] = A ++ [x] ++ B and i = A.length + 1 + B.length,
// which means that E = A ++ [x] ++ B as promised.
return new ArrayStringSet(E);
};
```

### 4. (16 points) Here Array, Gone Tomorrow

(a) Fill in the implementation of max in ArrayStringSet.

max = (): string => {

};

(b) Explain in clear English (or prove formally, if you prefer) why your code above is correct.