Nicholas Shahan Spring 2016

## Today's Agenda

- Standard Library Documentation (for HW3)
- Anonymous Functions
- "Unnecessary Function Wrapping"
- Returning Functions
- High-Order Functions
- Map
- Filter
- Fold
- More Practice
- Tree example
- Expression example


## What is in a Standard Library?

Standard Library Documentation

- Things that you simply can't implement on your own.
- Creating a timer, opening a file, etc.
- Things that are so common a "standardized" version will save you time and effort
- List.map, string concatenation, etc.
- A standard library makes writing and reading code easier.
- Common operations don't have to be implemented, and are immediately recognizable.

Online Documentation

- http://www.standardml.org/Basis/index.htm1
- http://www.sminj. org/doc/sminj-lib/Manual/toc. html

Helpful Subset

- Top-Level http://www.standardml.org/Basis/top-level-chapter.html
- List http://www.standardml.org/Basis/list.html
- ListPair http://www.standardml.org/Basis/list-pair.htm
- Real http://www.standardml.org/Basis/real.html
- String http://www.standardml. org/Basis/string.html


## Anonymous Functions

fn pattern => expression

- An expression that evaluates to a new function with no name
- Usually used as an argument or returned from a higher-order function
- Almost equivalent to the following:

```
let fun name pattern = expression in name end
```

- The difference is that anonymous functions cannot be recursive!
"Unnecessary Function Wrapping"

$$
\text { fn } \mathbf{x}=>\mathbf{f} \mathbf{x} \quad \text { vs. } \mathbf{f}
$$

- When called both functions will evaluate to the same result
- However, one creates an unnecessary function to wrap tl
- Compare to:
if el then true else false vs. el

| Bad Style: Lose Points | Good Style: Happy TA © |
| :--- | :--- |
| if $\mathrm{x}>0$ then true else false | $\mathrm{x}>0$ |
| n_times((fn ys $\mathrm{y}>\mathrm{tl} \mathrm{ys}), 3, \mathrm{xs})$ | n_times(tl, 3, xs) |

## Returning Functions

- Remember - Functions are first-class values - We can return them from functions
- Example:

$$
\begin{aligned}
& \text { fun double_or_triple } \mathbf{f}= \\
& \text { if } \mathbf{f} \\
& \text { then fn } \mathbf{x}=>2^{*} \mathbf{x} \\
& \text { else fn } \mathbf{x}=>3 * \mathbf{x}
\end{aligned}
$$

- Has type (int -> bool) -> (int -> int)
- The REPL will print (int $->$ bool) $->$ int $->$ int because it never prints an unnecessary parenthesis

High-order Hall of Fame

```
fun map (f, xs) =
    case xs of
        [] => []
    | x::xs' => (f x) ::(map(f, xs'))
```

```
fun filter (f, xs) =
    case xs of
        [] => []
    | x::xs' => if f x
                then x::(filter(f, xs'))
                else filter(f, xs')
```


## Fold

- Fold (synonyms/close relatives reduce, inject, etc.) is another very famous iterator over recursive structures
- Accumulates an answer by repeatedly applying a function $\mathbf{f}$ to the answer sofar
- fold(f, acc, $[\mathrm{x} 1, \mathrm{x} 2, \times 3, \times 4])$ computes $f(f(f(f(a c c, x 1), x 2), x 3), x 4)$
fun fold (f, acc, xs) =
case xs of
[] $\Rightarrow>$ acc
| x::xs' $=>$ fold(f, $\left.f(\mathbf{a c c}, \mathbf{x}), \mathbf{x s}^{\prime}\right)$
val fold = fn : ('a * 'b -> 'a) * 'a * 'b list -> 'a


## Practice - Tree Example

```
(* Generic Binary Tree Type *)
datatype 'a tree = Empty
        | Node of 'a * ' a tree * ' a tree
(* Apply a function to each element in a tree.*)
val tree_map = fn: (' a -> 'b) * 'a tree -> 'b tree
(* Returns true iff the given predicate returns true
when applied to each element in a tree. *)
val tree_all = fn: (' a -> bool) * 'a tree -> bool
```

Practice - Expression Example
(* Modified expression datatype from lecture 5. Now
there are variables. *)
datatype $\exp =$ Constant of int
Negate of exp
Negate of exp
Add of exp *
Add of exp * exp
Multiply of exp * exp
Multiply of exp
Var of string
(* Do a post order traversal of the given exp. At each
node, apply a function $f$ to it and replace the node with
the result. *)
val visit_post_order $=\mathrm{fn}:(\exp ->\exp )$ * exp $->$ exp
(* Simplify the root of the expression if possible. *)
val simplify_once $=$ fn : exp $->$ exp
(* Almost the same as evaluate but leaves variables
alone. *)
val simplify $=f n$ : exp -> exp

