

CSE341: Programming Languages

Lecture 12 Equivalence

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# Last Topic of Unit

More careful look at what "two pieces of code are equivalent" means

- Fundamental software-engineering idea
- Made easier with
  - Abstraction (hiding things)
  - Fewer side effects

Not about any "new ways to code something up"

# Equivalence

Must reason about "are these equivalent" all the time

- The more precisely you think about it the better
- Code maintenance: Can I simplify this code?
- Backward compatibility: Can I add new features without changing how any old features work?
- Optimization: Can I make this code faster?
- Abstraction: Can an external client tell I made this change?

To focus discussion: When can we say two functions are equivalent, even without looking at all calls to them?

May not know all the calls (e.g., we are editing a library)

### A definition

Two functions are equivalent if they have the same "observable behavior" no matter how they are used anywhere in any program

### Given equivalent arguments, they:

- Produce equivalent results
- Have the same (non-)termination behavior
- Mutate (non-local) memory in the same way
- Do the same input/output
- Raise the same exceptions

#### Notice it is much easier to be equivalent if:

- There are fewer possible arguments, e.g., with a type system and abstraction
- We avoid side-effects: mutation, input/output, and exceptions

# Example

Since looking up variables in ML has no side effects, these two functions are equivalent:

fun f 
$$x = x + x$$
 =  $\frac{\text{val } y = 2}{\text{fun f } x = y * x}$ 

But these next two are not equivalent in general: it depends on what is passed for £

Are equivalent if argument for f has no side-effects

- Example: g((fn i => print "hi"; i), 7)
- Great reason for "pure" functional programming

# Another example

These are equivalent *only if* functions bound to g and h do not raise exceptions or have side effects (printing, updating state, etc.)

Again: pure functions make more things equivalent

```
fun f x =
  let
  val y = g x
  val z = h x
  in
  (y,z)
  end
fun f x =
  let
  val z = h x
  val z = h x
  in
  (y,z)
  end
```

- Example: g divides by 0 and h mutates a top-level reference
- Example: g writes to a reference that h reads from

# One that really matters

Once again, turning the left into the right is great but only if the functions are pure:

map f (map g xs)

map (f o g) xs

# Syntactic sugar

Using or not using syntactic sugar is always equivalent

By definition, else not syntactic sugar

#### Example:

```
fun f x =
     x andalso g x

fun f x =
     if x
     then g x
     else false
```

But be careful about evaluation order

# Standard equivalences

Three general equivalences that always work for functions

- In any (?) decent language
- 1. Consistently rename bound variables and uses

But notice you can't use a variable name already used in the function body to refer to something else

# Standard equivalences

Three general equivalences that always work for functions

- In (any?) decent language
- 2. Use a helper function or do not

But notice you need to be careful about environments

# Standard equivalences

Three general equivalences that always work for functions

- In (any?) decent language
- 3. Unnecessary function wrapping

But notice that if you compute the function to call and *that* computation has side-effects, you have to be careful

### One more

If we ignore types, then ML let-bindings can be syntactic sugar for calling an anonymous function:

```
let val x = e1
in e2 end
```

$$(fn x => e2) e1$$

- These both evaluate e1 to v1, then evaluate e2 in an environment extended to map x to v1
- So exactly the same evaluation of expressions and result

But in ML, there is a type-system difference:

- x on the left can have a polymorphic type, but not on the right
- Can always go from right to left
- If x need not be polymorphic, can go from left to right

## What about performance?

According to our definition of equivalence, these two functions are equivalent, but we learned one is awful

(Actually we studied this before pattern-matching)

```
fun max xs =
  case xs of
  [] => raise Empty
  | x::[] => x
  | x::xs' =>
    if x > max xs'
    then x
    else max xs'
```

```
fun max xs =
  case xs of
   [] => raise Empty
    x::[] \Rightarrow x
   x::xs' =>
     let
       val y = max xs'
     in
        if x > y
       then x
        else y
```

# Different definitions for different jobs

- PL Equivalence (341): given same inputs, same outputs and effects
  - Good: Lets us replace bad max with good max
  - Bad: Ignores performance in the extreme
- Asymptotic equivalence (332): Ignore constant factors
  - Good: Focus on the algorithm and efficiency for large inputs
  - Bad: Ignores "four times faster"
- Systems equivalence (333): Account for constant overheads, performance tune
  - Good: Faster means different and better
  - Bad: Beware overtuning on "wrong" (e.g., small) inputs; definition does not let you "swap in a different algorithm"

Claim: Computer scientists implicitly (?) use all three every (?) day