

Sample Midterm 1 Solutions

Problem 1:

$$(a) F' = [(A'(B + C) + C')(A + B) + (ABC)']' \\ = [(A + B'C')C + A'B'](ABC)$$

$$F = (B + C)(A + B)(A + 1) + AC' \\ (b) = (AB + B + AC + BC)(A + 1) + AC' \\ = (AB + AB + AC + ABC + AB + B + AC + BC) + AC' \\ = (B + AC) + AC' = A + B$$

Problem 2:

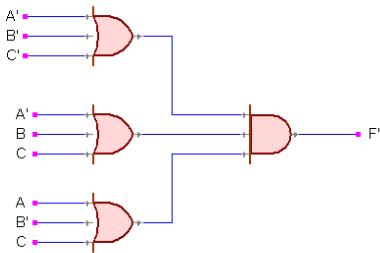
$$(a) F = (A + B + C + D')(A + B + C' + D)(A + B + C' + D')(A + B' + C + D)(A + B' + C + D')$$

(b) Five 4 input OR gates, one 5 input AND gate

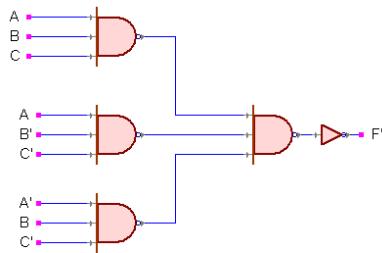
(c) Eleven 4 input AND gates, one 11 input OR gate

Problem 3: (Typo in sample midterm?)

$$(a) F' = [ABC + AB'C' + A'BC']' \\ = (A' + B' + C')(A' + B + C)(A + B' + C)$$



(b)



Problem 4:

(a)

| AB | | A | |
|----|---|---|---|
| CD | | | |
| | | D | |
| | 1 | 0 | 1 |
| | 1 | X | X |
| C | 1 | X | 0 |
| | 0 | X | 1 |
| | | B | |

(b)

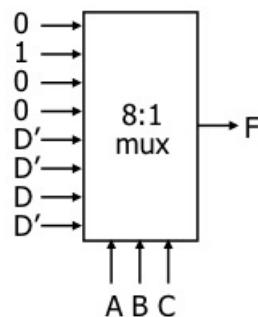
| AB | | A | |
|----|---|---|---|
| CD | | | |
| | | D | |
| | 1 | 0 | 1 |
| | 1 | X | X |
| C | 1 | X | 0 |
| | 0 | X | 1 |
| | | B | |

$$(c) F = B'C' + AD' + A'D$$

Problem 5:

(a)

| A | B | C | D | F | |
|---|---|---|---|---|----|
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 0 | |
| 0 | 0 | 1 | 0 | 1 | 1 |
| 0 | 0 | 1 | 1 | 1 | |
| 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 | |
| 0 | 1 | 1 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 | |
| 1 | 0 | 0 | 0 | 1 | D' |
| 1 | 0 | 0 | 1 | 0 | |
| 1 | 0 | 1 | 0 | 1 | D' |
| 1 | 0 | 1 | 1 | 0 | |
| 1 | 1 | 0 | 0 | 0 | D |
| 1 | 1 | 0 | 1 | 1 | |
| 1 | 1 | 1 | 0 | 1 | D' |
| 1 | 1 | 1 | 1 | 0 | |



(b)

| A | B | C | D | F | |
|---|---|---|---|---|-------------|
| 0 | 0 | 0 | 0 | 0 | C |
| 0 | 0 | 0 | 1 | 0 | |
| 0 | 0 | 1 | 0 | 1 | |
| 0 | 0 | 1 | 1 | 1 | |
| 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 | |
| 0 | 1 | 1 | 0 | 0 | |
| 0 | 1 | 1 | 1 | 0 | |
| 1 | 0 | 0 | 0 | 1 | D' |
| 1 | 0 | 0 | 1 | 0 | |
| 1 | 0 | 1 | 0 | 1 | |
| 1 | 0 | 1 | 1 | 0 | |
| 1 | 1 | 0 | 0 | 0 | C'D+ CD' |
| 1 | 1 | 0 | 1 | 1 | |
| 1 | 1 | 1 | 0 | 1 | |
| 1 | 1 | 1 | 1 | 0 | |

