

| DS.A. 2 |  |  |
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| 1. Why do we analyze algorithms? |  |  |
| 2. How do we measure the efficiency of an algorithm? |  |  |
| A. Time it on my computer. |  |  |
| B. Compare its time to that of another algorithm that has already been analyzed. |  |  |
| C. Count how many instructions it will execute for an arbitrary input data set. |  |  |
| Suppose there are $\mathbf{n}$ inputs. |  |  |
| We'd like to find a time function $\mathbf{T}(\mathbf{n})$ that shows how the execution time depends on $\mathbf{n}$. |  |  |
| $\mathrm{T}(\mathrm{n})=3 \mathrm{n}+4$ | $\mathrm{T}(\mathrm{n})=\mathrm{e}^{\mathrm{n}}$ | $\mathrm{T}(\mathrm{n})=2$ |


| "Big-Oh" |
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| $\mathrm{T}(\mathrm{N})=\mathrm{O}(\mathrm{f}(\mathrm{N}))$ if there are positive constants <br> c and n 0 such that $\mathrm{T}(\mathrm{N}) \leq \mathrm{cf}(\mathrm{N})$ when $\mathrm{N} \geq \mathrm{n} 0$. |
|  |
| We say " $\mathrm{T}(\mathrm{N})$ has order $\mathrm{f}(\mathrm{N})$." |
| We try to simplify $\mathrm{T}(\mathrm{N})$ into one or more |
| common functions. |
| Ex. $1 \mathrm{~T}(\mathrm{~N})=3 \mathrm{~N}+4$ <br> $\mathrm{~T}(\mathrm{~N})$ is linear. Intuitively, $\mathrm{f}(\mathrm{N})$ should be N. <br> More formally, <br> $\mathrm{T}(\mathrm{N})=3 \mathrm{~N}+4 \leq 3 \mathrm{~N}+4 \mathrm{~N}, \mathrm{~N} \geq 1$ <br> $\mathrm{~T}(\mathrm{~N}) \leq 7 \mathrm{~N}, \mathrm{~N} \geq 1$ <br> So $\mathrm{T}(\mathrm{N})$ is of order N. |




