

## B-Trees

What makes them disk-friendly?

1. Many keys stored in a node

- All brought to memory/cache in one access!

2. Internal nodes contain only keys;

Only leaf nodes contain keys and actual data

- The tree structure can be loaded into memory irrespective of data object size
- Data actually resides in disk

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## B-trees vs. AVL trees

Suppose we have 100 million items ( $100,000,000$ ):

- Depth of AVL Tree
- Depth of B+ Tree with M $=128, \mathrm{~L}=64$


## $M=3 I=2 \quad$ Splitting the Root






## Does Adoption Always Work?

- What if the sibling doesn't have enough for you to borrow from?
e.g. you have $\lceil L / 2\rceil-1$ and sibling has $\lceil L / 2\rceil$ ?



## Deletion Algorithm

1. Remove the key from its leaf
2. If the leaf ends up with fewer than $\lceil\overline{L / 2}\rceil$ items, underflow!

- Adopt data from a sibling; update the parent
- If adopting won't work, delete node and merge with neighbor
- If the parent ends up with
fewer than 「м/2ךitems,
underflow!
$\qquad$


## Thinking about B-Trees

- B-Tree insertion can cause (expensive) splitting and propagation
- B-Tree deletion can cause (cheap) adoption or (expensive) deletion, merging and propagation
- Propagation is rare if $\boldsymbol{M}$ and $\boldsymbol{L}$ are large (Why?)
- If $\boldsymbol{M}=\boldsymbol{L}=128$, then a B-Tree of height 4 will store at least $30,000,000$ items

