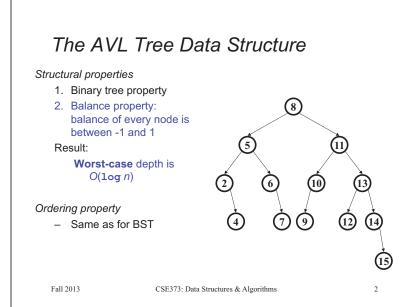




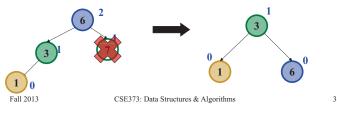
CSE373: Data Structures & Algorithms Optional Slides: AVL Delete

Dan Grossman Fall 2013

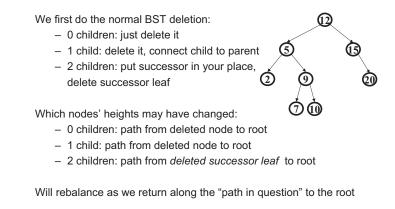


AVL Tree Deletion

- Similar to insertion: do the delete and then rebalance
 - Rotations and double rotations
 - Imbalance may propagate upward so rotations at multiple nodes along path to root may be needed (unlike with insert)
- Simple example: a deletion on the right causes the left-left grandchild to be too tall
 - Call this the left-left case, despite deletion on the right
 - insert(6) insert(3) insert(7) insert(1) delete(7)



Properties of BST delete



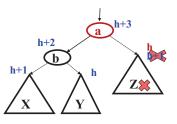
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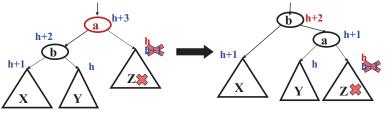
Case #1 Left-left due to right deletion

Start with some subtree where if right child becomes shorter we are unbalanced due to height of left-left grandchild



A delete in the right child could cause this right-side shortening

Case #1: Left-left due to right deletion

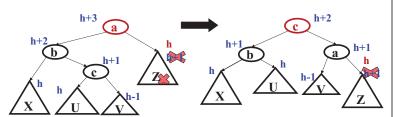


- Same single rotation as when an insert in the left-left grandchild caused imbalance due to X becoming taller
- But here the "height" at the top decreases, so more rebalancing farther up the tree might still be necessary

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Case #2: Left-right due to right deletion



• Same double rotation when an insert in the left-right grandchild caused imbalance due to c becoming taller

• But here the "height" at the top decreases, so more rebalancing farther up the tree might still be necessary

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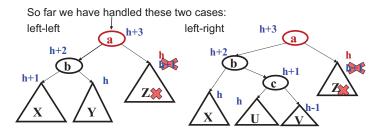
And the other half

- Naturally two more mirror-image cases (not shown here)
 - Deletion in left causes right-right grandchild to be too tall
 - Deletion in left causes right-left grandchild to be too tall
 - (Deletion in left causes both right grandchildren to be too tall, in which case the right-right solution still works)
- And, remember, "lazy deletion" is a lot simpler and might suffice for your needs

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No third right-deletion case needed



But what if the two left grandchildren are now both too tall (h+1)?

- Then it turns out left-left solution still works
- The children of the "new top node" will have heights differing by 1 instead of 0, but that's fine

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