

Terminology

- **Terminals** – alphabet of language defined by CFG
- **Nonterminals** – symbols defined in terms of terminals and nonterminals
- **Productions** – rules for how a nonterminal (lefthand side, lhs) is defined in terms of a (possibly empty) sequence of terminals and nonterminals
 - Multiple alternative productions allowed for a nonterminal
- **Start symbol** – root of the defining language

```
Program ::= Stmt
Stmt ::= if ( Expr ) then Stmt else Stmt
       while ( Expr ) do Stmt
```

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Derivations and Parse Trees

- **Derivation**: a sequence of expansion steps, beginning with a start symbol and leading to a sequence of terminals
- **Parsing**: inverse of derivation
 - Given a sequence of terminals (i.e., tokens) recover the nonterminals representing structure
- Can represent a derivation as a parse tree, that is, the concrete syntax tree

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Example Grammar

```
E ::= E op E | - E | ( E ) | id
op ::= + | - | * | /
```

a * (b + - c)

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Ambiguity

- Some grammars are ambiguous: multiple distinct parse trees for the same terminal string
 - The “hi2bob” lexing example was essentially the same problem
- Since the structure of the parse tree captures much of the meaning of the program, ambiguity implies multiple possible meanings for the same program
- This isn’t good for programming languages: if the programmer wrote an ambiguous program, the decision of the compiler writer would define the semantics of the program
- “The good news about computers is that they do what you tell them to do. The bad news is that they do what you tell them to do.” [Ted Nelson]

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Famous Ambiguity: “Dangling Else”

```

Stmt ::= ... |
      if ( Expr ) Stmt |
      if ( Expr ) Stmt else Stmt

```

if (e_1) if (e_2) s_1 else s_2 : if (e_1) if (e_2) s_1 else s_2

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Resolving Ambiguity: first two options

- Option 1: a meta-rule such as “else associates with closest previous if”
 - works, keeps original grammar intact
 - ad hoc and informal
- Option 2: rewrite the grammar to avoid ambiguity
 - formal, no additional rules beyond syntax
 - sometimes obscures original grammar

```

Stmt      ::= MatchedStmt | UnmatchedStmt
MatchedStmt ::= ... |
            if ( Expr ) MatchedStmt else MatchedStmt
UnmatchedStmt ::= if ( Expr ) Stmt |
                 if ( Expr ) MatchedStmt else UnmatchedStmt

```

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Resolving Ambiguity Example

```

Stmt      ::= MatchedStmt | UnmatchedStmt
MatchedStmt ::= ... |
            if ( Expr ) MatchedStmt else MatchedStmt
UnmatchedStmt ::= if ( Expr ) Stmt |
                 if ( Expr ) MatchedStmt else UnmatchedStmt

```

if (e_1) if (e_2) s_1 else s_2

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Resolving Ambiguity: third option

- Redesign the language to remove the ambiguity
 - formal, clear, elegant
 - allows sequence of **Stmts** in **then** and **else** branches, no braces are needed
 - extra **end** required for every **if**

```

Stmt ::= ... |
      if Expr then Stmt end |
      if Expr then Stmt else Stmt end

```

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Expression example: reprise

```
E ::= E Op E | - E | ( E ) | id
Op ::= + | - | * | /
```

```
a + b * c : a + b * c
```

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Resolving Ambiguity (Option 1)

- Add some meta-rules, e.g. precedence and associativity rules

Example:

```
E ::= E Op E | - E | E ++
      | ( E ) | id
Op ::= + | - | * | / | %
      | ** | == | < | &&
      | |
```

Operator	Preced	Assoc
++ [postfix]	Highest	Left
- [prefix]		Right
**		Right
*, /, %		Left
+, -		Left
==, <		None
&&		Left
	Lowest	Left

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Removing Ambiguity (Option 2)

- Modify the grammar to explicitly resolve the ambiguity
 - create a nonterminal for each precedence level
 - expr is lowest precedence nonterminal
 - each nonterminal can be rewritten with higher precedence operator, highest precedence operator includes atomic expressions
 - at each precedence level, use
 - left recursion for left-associative operators
 - right recursion for right-associative operators
 - no recursion for non-associative operators

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Redone Example

```
E ::= E0
E0 ::= E0 || E1 | E1                left associative
E1 ::= E1 && E2 | E2                left associative
E2 ::= E3 (== | <) E3 | E3          non associative
E3 ::= E3 (+ | -) E4 | E4          left associative
E4 ::= E4 (* | / | %) E5 | E5       left associative
E5 ::= E6 ** E5 | E6               right associative
E6 ::= - E6 | E7                   right associative
E7 ::= E7 ++ | E8                  left associative
E8 ::= id | ( E )
```

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Designing A Grammar

- Accurate
- Unambiguous
- Formal
- Readable, Clear
- Parsable by a particular algorithm
 - Top down parser \implies LL(k) Grammar
 - Bottom up Parser \implies LR(k) Grammar
- Design to implementation relatively straightforward
 - By hand
 - By automatic tools

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Brainstorm: how to parse?

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