CSE 401 – Compilers

LR Parser Construction
Hal Perkins
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Administrivia

- Scanners due tomorrow, 11 pm how's it going? Questions?
 - Be sure to implement both kinds of comments
- Project discussion board, email: Wrong: "I am confused/have a question"
 Right: "we are confused/have a question"
- Schedule:
 - Today and in sections tomorrow: LR parsing and LR parser construction
 - HW2 (LR parsers) out Friday, due Thursday next week
 - Next part of the project, Parser + AST visitors, out by Monday, due a week from Thursday
 - More details/examples in lecture and sections next week
 - Assignment/project/exam dates on schedule will stay as-is
- HW1 sample solutions: pick up a copy at end of class today
- HW1 grading: "regexp unrolling"? Where did that come from??
 - "Very clever, -1"
 - "Premature optimization is the root of all evil" Knuth

Agenda

- LR(0) state construction
- FIRST, FOLLOW, and nullable
- Variations: SLR, LR(1), LALR

LR State Machine

- Idea: Build a DFA that recognizes handles
 - Language generated by a CFG is generally not regular, but
 - Language of handles for a CFG is regular
 - So a DFA can be used to recognize handles
 - LR Parser reduces when DFA accepts a handle

Prefixes, Handles, &c (review)

- If S is the start symbol of a grammar G,
 - If $S = * \alpha$ then α is a sentential form of G
 - γ is a *viable prefix* of *G* if there is some derivation $S = *_{rm} \alpha A w = *_{rm} \alpha \beta w$ and γ is a prefix of $\alpha \beta$.
 - The occurrence of β in $\alpha\beta$ w is a *handle* of $\alpha\beta$ w
- An *item* is a marked production (a . at some position in the right hand side)
 - -[A ::= .XY] [A ::= X.Y] [A ::= XY.]

Building the LR(0) States

Example grammar

```
S'::= S $
S::= (L)
S::= x
L::= S
L::= L, S
```

- We add a production S' with the original start symbol followed by end of file (\$)
 - We accept if we reach the end of this production
- Question: What language does this grammar generate?

Start of LR Parse

```
    S'::= S$
    S::= (L)
    S::= x
    L::= S
    L::= L, S
```

- Initially
 - Stack is empty
 - Input is the right hand side of S', i.e., S\$
 - Initial configuration is [S'::= . S \$]
 - But, since position is just before S, we are also just before anything that can be derived from S

Initial state

$$S'::= . S$$
 start
$$S::= . (L)$$

$$S::= . X$$
 completion

- A state is just a set of items
 - Start: an initial set of items
 - Completion (or closure): additional productions whose left hand side appears to the right of the dot in some item already in the state

Shift Actions (1)

$$S'::= .S$$

$$S::= .(L)$$

$$S::= .x$$

- To shift past the x, add a new state with appropriate item(s), including their closure
 - In this case, a single item; the closure adds nothing
 - This state will lead to a reduction since no further shift is possible

Shift Actions (2)

$$S'::= ...S$$
 $C ::= ...L , S$ $C ::= ...L , S$

S'::= S\$
 S::= (L)
 S::= x
 L::= S
 L::= L, S

- If we shift past the (, we are at the beginning of L
- The closure adds all productions that start with L, which also requires adding all productions starting with S

Goto Actions

$$S'::= .S \$$$

$$S::= .(L)$$

$$S::= .X$$

 Once we reduce S, we'll pop the rhs from the stack exposing the first state. Add a goto transition on S for this.

Basic Operations

- Closure (S)
 - Adds all items implied by items already in S
- Goto (I, X)
 - I is a set of items
 - X is a grammar symbol (terminal or non-terminal)
 - Goto moves the dot past the symbol X in all appropriate items in set I

Closure Algorithm

```
• Closure (S) = repeat for any item [A ::= \alpha . B \beta] in S for all productions B ::= \gamma add [B ::= . \gamma] to S until S does not change return S
```

Classic example of a fixed-point algorithm

Goto Algorithm

```
• Goto (I, X) = set new to the empty set for each item [A := \alpha . X \ \beta] in I add [A := \alpha X . \ \beta] to new return Closure (new)
```

This may create a new state, or may return an existing one

LR(0) Construction

- First, augment the grammar with an extra start production S' ::= S\$
- Let T be the set of states
- Let E be the set of edges
- Initialize T to Closure ([S'::= . S \$])
- Initialize E to empty

LR(0) Construction Algorithm

```
repeat
for each state I in T
for each item [A ::= \alpha . X \beta] in I
Let new be Goto(I, X)
Add new to T if not present
Add I \xrightarrow{X} new to E if not present
until E and T do not change in this iteration
```

 Footnote: For symbol \$, we don't compute goto(I, \$); instead, we make this an accept action.

Example: States for

Building the Parse Tables (1)

- For each edge $I \xrightarrow{x} J$
 - if X is a terminal, put sj in column X, row I of the action table (shift to state j)
 - If X is a non-terminal, put gj in column X, row I of the goto table

Building the Parse Tables (2)

- For each state I containing an item
 [S' ::= S . \$], put accept in column \$ of row I
- Finally, for any state containing
 [A ::= γ .] put action rn (reduce) in every column of row I in the table, where n is the production number

Example: Tables for

Where Do We Stand?

- We have built the LR(0) state machine and parser tables
 - No lookahead yet
 - Different variations of LR parsers add lookahead information, but basic idea of states, closures, and edges remains the same

A Grammar that is not LR(0)

 Build the state machine and parse tables for a simple expression grammar

$$S ::= E \$$

$$E ::= T + E$$

$$E ::= T$$

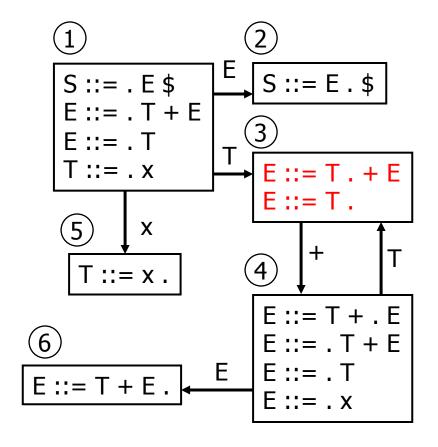
$$T := x$$

LR(0) Parser for

0.
$$S := E$$
\$
1. $E := T + E$

2.
$$E := T$$

3.
$$T := x$$



	X	+	\$	Е	Т
1	s5			g2	g3
2			acc		
3	r2	s4,r2	r2		
4	s5			g6	g3
5	r3	r3	r3		
6	r1	r1	r1		

- State 3 is has two possible actions on +
 - shift 4, or reduce 2
- ∴ Grammar is not LR(0)

How can we solve conflicts like this?

- Idea: look at the next symbol after the handle before deciding whether to reduce
- Easiest: SLR Simple LR. Reduce only if next input terminal symbol could follow resulting nonterminal
- More complex: LR and LALR. Store lookahead symbols in items to keep track of what can follow a particular instance of a reduction
 - LALR used by YACC/Bison/CUP; we won't examine in detail

SLR Parsers

- Idea: Use information about what can follow a nonterminal to decide if we should perform a reduction; don't reduce if the next input symbol can't follow the resulting non-terminal
- We need to be able to compute FOLLOW(A) the set of symbols that can follow A in any possible derivation
 - i.e., t is in FOLLOW(A) if any derivation contains At
 - To compute this, we need to compute FIRST(γ) for strings γ that can follow A

Calculating FIRST(γ)

- Sounds easy... If $\gamma = X Y Z$, then FIRST(γ) is FIRST(X), right?
 - But what if we have the rule $X := \varepsilon$?
 - In that case, FIRST(γ) includes anything that can follow X, i.e. FOLLOW(X), which includes FIRST(Y) and, if Y can derive ε , FIRST(Z), and if Z can derive ε , ...
 - So computing FIRST and FOLLOW involves knowing FIRST and FOLLOW for other symbols, as well as which ones can derive ε.

FIRST, FOLLOW, and nullable

- nullable(X) is true if X can derive the empty string
- Given a string γ of terminals and non-terminals, FIRST(γ) is the set of terminals that can begin strings derived from γ
 - For SLR we only need this for single terminal or non-terminal symbols, not arbitrary strings γ
- FOLLOW(X) is the set of terminals that can immediately follow X in some derivation
- All three of these are computed together

Computing FIRST, FOLLOW, and nullable (1)

- Initialization
 - set FIRST and FOLLOW to be empty sets set nullable to false for all non-terminals set FIRST[a] to a for all terminal symbols a
- Repeatedly apply four simple observations to update these sets
 - Stop when there are no further changes
 - Another fixed-point algorithm

Computing FIRST, FOLLOW, and nullable (2)

```
repeat
   for each production X := Y_1 Y_2 ... Y_k
    if Y_1 \dots Y_k are all nullable (or if k = 0)
      set nullable[X] = true
    for each i from 1 to k and each j from i +1 to k
      if Y_1 \dots Y_{i-1} are all nullable (or if i = 1)
        add FIRST[Y_i] to FIRST[X]
      if Y_{i+1} \dots Y_k are all nullable (or if i = k)
        add FOLLOW[X] to FOLLOW[Y_i]
      if Y_{i+1} ... Y_{i-1} are all nullable (or if i+1=j)
        add FIRST[Y_i] to FOLLOW[Y_i]
Until FIRST, FOLLOW, and nullable do not change
```

Example

• Grammar

Z ::= d

Z ::= X Y Z

 $Y ::= \varepsilon$

Y ::= c

X ::= Y

X ::= a

nullable FIRST FOLLOW

X

Υ

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LR(0) Reduce Actions (review)

- In a LR(0) parser, if a state contains a reduction, it is unconditional regardless of the next input symbol
- Algorithm:

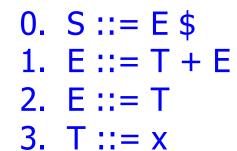
```
Initialize R to empty for each state I in T for each item [A ::= \alpha] in I add (I, A ::= \alpha) to R
```

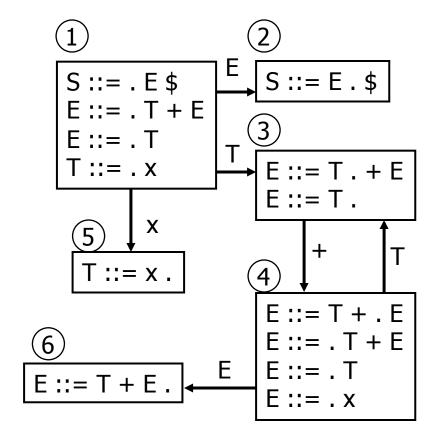
SLR Construction

- This is identical to LR(0) states, etc., except for the calculation of reduce actions
- Algorithm:

```
Initialize R to empty
for each state I in T
for each item [A ::= \alpha .] in I
for each terminal a in FOLLOW(A)
add (I, a, A ::= \alpha) to R
— i.e., reduce \alpha to A in state I only on lookahead a
```

SLR Parser for





	X	+	\$	E	Т
1	s5			g2	g3
2			acc		
3	r2	s4 ,r2	r2		
4	s5			g6	g3
5	r3	r3	r3		
6	r <u>l</u>	r <u>1</u>	r1		

On To LR(1)

- Many practical grammars are SLR
- LR(1) is more powerful yet
- Similar construction, but notion of an item is more complex, incorporating lookahead information

LR(1) Items

- An LR(1) item [$A := \alpha \cdot \beta$, a] is
 - A grammar production ($A := \alpha \beta$)
 - A right hand side position (the dot)
 - A lookahead symbol (a)
- Idea: This item indicates that α is the top of the stack and the next input is derivable from βa .
- Full construction: see the book

LR(1) Tradeoffs

- LR(1)
 - Pro: extremely precise; largest set of grammars
 - Con: potentially *very* large parse tables with many states

LALR(1)

- Variation of LR(1), but merge any two states that differ only in lookahead
 - Example: these two would be merged

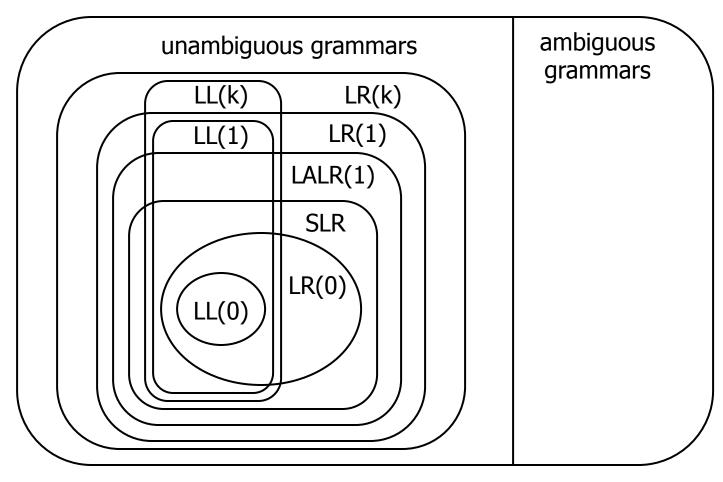
$$[A ::= x . , a]$$

$$[A ::= x . , b]$$

LALR(1) vs LR(1)

- LALR(1) tables can have many fewer states than LR(1)
 - Somewhat surprising result: will actually have same number of states as SLR parsers, even though LALR(1) is more powerful
 - After the merge step, acts like SLR parser with "smarter"
 FOLLOW sets (may be specific to particular handles)
- LALR(1) may have reduce conflicts where LR(1) would not (but in practice this doesn't happen often)
- Most practical bottom-up parser tools are LALR(1) (e.g., yacc, bison, CUP, ...)

Language Heirarchies



Coming Attractions

Lecture

- LL(k) Parsing Top-Down
- Recursive Descent Parsers
 - What you can do if you want a parser in a hurry

Sections

- AST construction what do do while you parse!
- Visitor Pattern how to traverse ASTs for further processing (type checking, code generation, ...)