CSE 413
Programming Languages & Implementation

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Context-Free Grammars and Parsing

The Plan

- Parsing overview
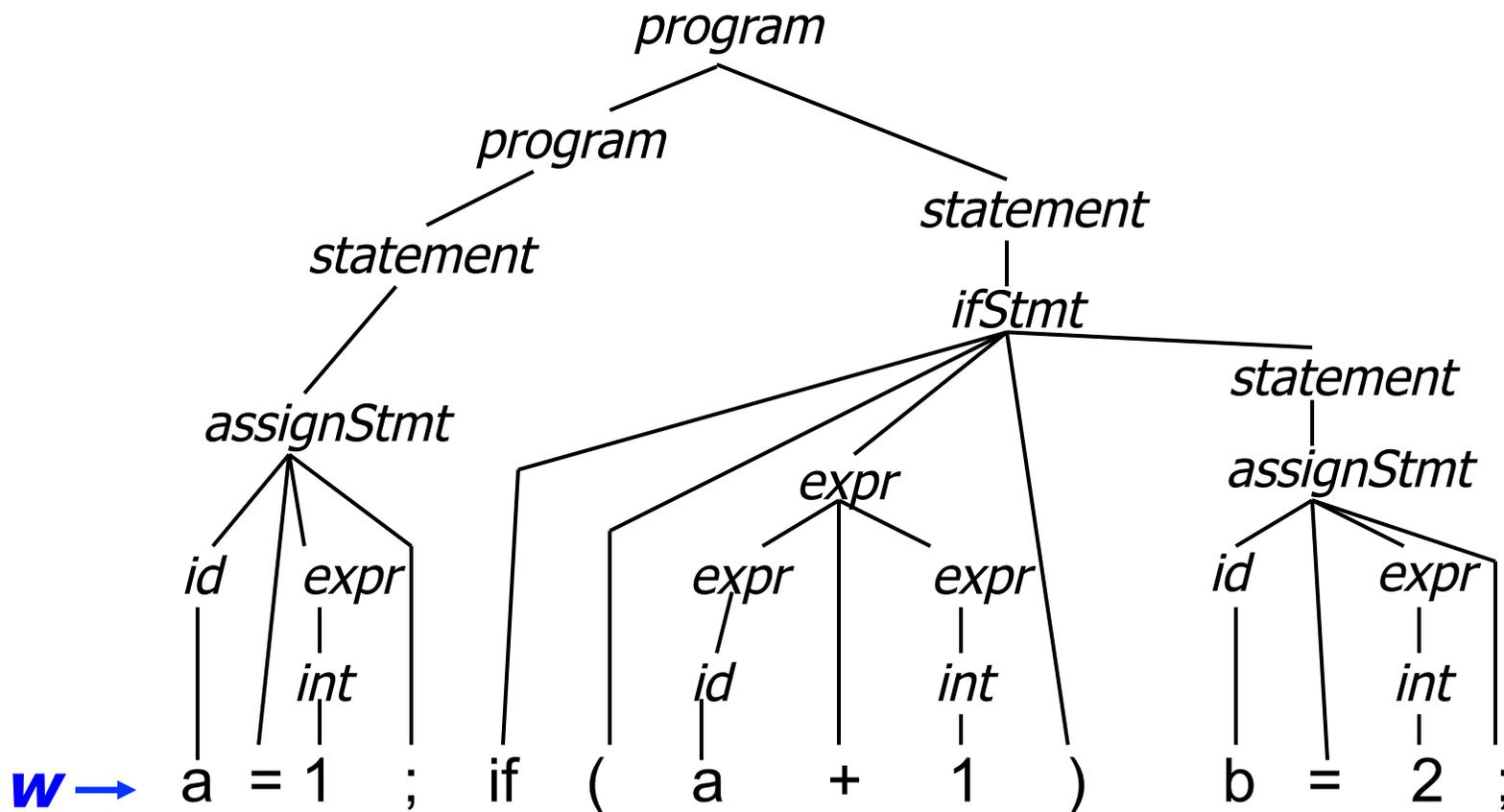- Context free grammars
- Grammar problems - ambiguity

Parsing

- The syntax of most programming languages can be specified by a *context-free grammar* (CGF)

- **Parsing**: Given a grammar *G* and a sentence *w* in *L(G)*, traverse the derivation (parse tree) for *w* in some *standard order* and do *something useful* at each node

  – The tree might not be produced explicitly, but the control flow of a parser corresponds to a traversal

Old Example

G

program ::= *statement* | *program statement*
statement ::= *assignStmt* | *ifStmt*
assignStmt ::= *id* = *expr* ;
ifStmt ::= if (*expr*) *statement*
expr ::= *id* | *int* | *expr* + *expr*
id ::= a | b | c | i | j | k | n | x | y | z
int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

program
program   *statement*
statement   *ifStmt*
assignStmt   *statement*
assignStmt
id *expr*   *expr* *expr*   *id* *expr*
int   *id* *int*   *int*
w → a = 1 ; if (a + 1) b = 2 ;

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"Standard Order"

- For practical reasons we want the parser to be *deterministic* (no backtracking), and we want to examine the source program from *left to right*.

  - (i.e., parse the program in linear time in the order it appears in the source file)

Common Orderings

- Top-down
  - Start with the root
  - Traverse the parse tree depth-first, left-to-right (leftmost derivation)
  - LL(k)
- Bottom-up
  - Start at leaves and build up to the root
    - Effectively a rightmost derivation in reverse(!)
  - LR(k) and subsets (LALR(k), SLR(k), etc.)

"Something Useful"

- At each point (node) in the traversal, perform some *semantic action*

    – Construct nodes of full parse tree (rare)

    – Construct abstract syntax tree (common)

    – Construct linear, lower-level representation (more common in later parts of a modern compiler)

    – Generate target code or interpret on the fly (1-pass compilers & interpreters; not common in production compilers – but what we will do for our project)

Context-Free Grammars (review)

- Formally, a grammar G is a tuple $<N,\Sigma,P,S>$ where:
  - N a finite set of non-terminal symbols
  - Σ a finite set of terminal symbols
  - P a finite set of productions
    - A subset of $N \times (N \cup \Sigma)^*$
  - S the *start symbol,* a distinguished element of N
    - If not specified otherwise, this is usually assumed to be the non-terminal on the left of the first production

Standard Notations

- a, b, c   elements of Σ
- w, x, y, z   elements of Σ^*
- A, B, C   elements of N
- X, Y, Z   elements of $N \cup \Sigma$
- α, β, γ elements of $(N \cup \Sigma)^*$
- A$\rightarrow\alpha$ or A ::= α if <A, α> in P

Derivation Relations (1)

- α A γ => α β γ iff A ::= β in *P*
  - derives

- A =>* w if there is a *chain* of productions starting with A that generates w
  - transitive closure

Derivation Relations (2)

- w A γ =>$_{lm}$ w β γ iff A ::= β in *P*
  - derives leftmost
- α A w =>$_{rm}$ α β w   iff A ::= β in *P*
  - derives rightmost
- Parsers normally work with only leftmost or rightmost derivations – not random orderings

Languages

- For A in *N*, *L*(A) = { w | A =>* w }
  - i.e., set of strings (words, terminal symbols) generated by nonterminal A
- If *S* is the start symbol of grammar *G*, we define *L*(*G*) = *L*(*S*)

Reduced Grammars

- Grammar G is *reduced* iff for every production
  A ::= α in G there is some derivation

    S =>* x A z => x α z =>* xyz

  – i.e., no production is useless
- Convention: we will use only reduced grammars

Example

program ::= statement | program statement
statement ::= assignStmt | ifStmt
assignStmt ::= id = expr ;
ifStmt ::= if (expr) stmt
expr ::= id | int | expr + expr
id ::= a | b | c | i | j | k | n | x | y | z
int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

- Top down, Leftmost derivation for: a = 1 + b ;

Example

- Grammar

  $S ::= aABe$

  $A ::= Abc \mid b$

  $B ::= d$

- Top down, leftmost derivation of: **abbcde**

Ambiguity

- Grammar G is *unambiguous* iff every w in L(G) has a unique leftmost (or rightmost) derivation
  - Fact: either unique leftmost or unique rightmost implies the other
- A grammar without this property is *ambiguous*
  - Other grammars that generate the same language may be unambiguous
- We need unambiguous grammars for parsing

Example: Ambiguous Grammar for Arithmetic Expressions

expr ::= *expr* + *expr* | *expr* - *expr*
       | *expr* * *expr* | *expr* / *expr* | *int*

int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

- Exercise: show that this is ambiguous
  - How? Show two different leftmost or rightmost derivations for the same string
  - Equivalently: show two different parse trees for the same string

Example (cont)

- Give a leftmost derivation of 2+3*4 and show the parse tree

Example (cont)

- Give a different leftmost derivation of 2+3*4 and show the parse tree

Another example

- Give two different derivations of 5+6+7

What's going on here?

- This grammar has no notion of precedence or associatively

- Standard solution
  - Create a non-terminal for each level of precedence
  - Isolate the corresponding part of the grammar
  - Force the parser to recognize higher precedence subexpressions first

Classic Expression Grammar

expr ::= *expr* + *term* | *expr* – *term* | *term*

term ::= *term* * *factor* | *term* / *factor* | *factor*

factor ::= *int* | (*expr*)

int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

Check: Derive 2 + 3 * 4

Check: Derive 5 + 6 + 7

- Note interaction between left- vs right-recursive rules and resulting associativity

Check: Derive 5 + (6 + 7)

Another Classic Example

- Grammar for conditional statements

    stmt ::= if (*cond*) *stmt*
              | if (*cond*) *stmt* else *stmt*
              | *assign*

- Exercise: show that this is ambiguous
    - How?

One Derivation

stmt ::= if (*cond*) *stmt*
| if (*cond*) *stmt* else *stmt*
| *assign*

if (*cond*) if (*cond*) *stmt*   else   *stmt*

Another Derivation

$stmt$ ::= if ($cond$) $stmt$
| if ($cond$) $stmt$ else $stmt$
| $assign$

if ($cond$) if ($cond$) $stmt$ else $stmt$

Solving if Ambiguity

- Fix the grammar to separate if statements with else from if statements with no else

    – Done in original Java reference grammar

    – Adds lots of non-terminals

        • Need productions for things like "while statement that contains an unmatched if" and "while statement with only matched ifs", etc. etc. etc.

- Use some ad-hoc rule in parser

    – "else matches closest unpaired if"

Parser Tools and Operators

- Most parser tools can cope with ambiguous grammars
  - Makes life simpler if used with discipline
- Typically one can specify operator precedence & associativity
  - Allows simpler, ambiguous grammar with fewer nonterminals as basis for generated parser, without creating problems

Parser Tools and Ambiguous Grammars

- Possible rules for resolving other problems
  - Earlier productions in the grammar preferred to later ones
  - Longest match used if there is a choice
- Parser tools normally allow for this
  - But be sure that what the tool does is really what you want

Or…

- If the parser is hand-written, either fudge the grammar or the parser, or cheat where it helps.

to be continued…