# Introduction to Database Systems CSE 444 

Lecture 20: Overview of
Query Optimization

## Announcements

- Project 3 is due tonight
- How is it going?
- HW3 is out and is due on Friday
- Rather short assignment
- But start early in case you have questions
- Project 4 will be out by Friday (last assignment)
- Group assignment: 2 to 4 students (but 1 ok too)


## Where We Are

- We are learning how a DBMS executes a query
- What we learned so far
- How data is stored and indexed (lectures 15 and 16)
- Logical query plans: relational algebra (lecture 17)
- Steps involved in processing a query (lecture 18)
- Operator algorithms (lecture 19)
- Today
- How to select logical \& physical query plans
- Chapter 16 in the book (optional reading)


## Query Optimization Goal

- For a query
- There exists many logical and physical query plans
- Query optimizer needs to pick a good one


## Query Optimization Algorithm

- Enumerate alternative plans
- Compute estimated cost of each plan
- Compute number of I/Os
- Compute CPU cost
- Choose plan with lowest cost
- This is called cost-based optimization


## Outine

- Search space
- Algorithm for enumerating query plans
- Estimating the cost of a query plan


## Relational Algebra Equivalences

- Selections
- Commutative: $\sigma_{\mathrm{c} 1}\left(\sigma_{\mathrm{c} 2}(R)\right)$ same as $\sigma_{\mathrm{c} 2}\left(\sigma_{\mathrm{c} 1}(R)\right)$
- Cascading: $\sigma_{\mathrm{c} 1 \wedge \mathrm{c} 2}(R)$ same as $\sigma_{\mathrm{c} 2}\left(\sigma_{\mathrm{c} 1}(R)\right)$
- Projections
- Cascading
- Joins
- Commutative : $R \bowtie S$ same as $S \bowtie R$
- Associative: $R \bowtie(S \bowtie T)$ same as $(R \bowtie S) \bowtie T$


## Left-Deep Plans and Bushy Plans



## Relational Algebra Equivalences

- Selects, projects, and joins
- We can commute and combine all three types of operators
- We just have to be careful that the fields we need are available when we apply the operator
- Relatively straightforward. See book 16.2


## Search Space Challenges

- Search space is huge!
- Many possible equivalent trees
- Many implementations for each operator
- Many access paths for each relation
- File scan or index + matching selection condition
- Cannot consider ALL plans
- Want search space that includes low-cost plans


## Outine

- Search space
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## Key Decisions

- When selecting a plan, some of the most important decisions include:
- Logical plan
- Can we push selections down?
- Can we push projections or aggregations down?
- What order to use for joins?
- Physical plan
- What join algorithms to use?
- What access paths to use (file scan or index)?


## Plan Enumeration Algorithms

- Rule-based vs cost-based algorithms
- Logical plans
- Heuristic-based algorithms
- Use size of intermediate results as cost measure
- Physical plans
- Top-down algorithms or
- Bottom-up: dynamic programming approaches
- Also called "Selinger-style" optimizers
- Use heuristics to limit search space


## Outine

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## Computing the Cost of a Plan

- Collect statistical summaries of stored data
- Compute cost in a bottom-up fashion
- For each operator compute
- Estimate cost of executing the operation
- Estimate statistical summary of the output data


## Statistics on Base Data

- Collected information for each relation
- Number of tuples (cardinality)
- Indexes, number of keys in the index
- Number of physical pages, clustering info
- Statistical information on attributes
- Min value, max value, number distinct values
- Histograms
- Correlations between columns (hard)
- Collection approach: periodic, using sampling


## Retrieving data from Storage

- Access path: a way to retrieve tuples from a table
- A file scan
- An index plus a matching selection condition
- Index matches selection condition if it can be used to retrieve just tuples that satisfy the condition
- Example: Supplier(sid,sname,scity,sstate)
- B+-tree index on (scity,sstate)
- matches scity=‘Seattle’
- does not match sid=3, does not match sstate=‘WA'


## Access Path Selection

- Supplier(sid,sname,scity,sstate)
- Selection condition: sid > $300 \wedge$ scity=‘Seattle’
- Indexes: B+-tree on sid and B+-tree on scity
- Which access path should we use?
- We should pick the most selective access path


## Access Path Selectivity

- Access path selectivity is the number of pages retrieved if we use this access path
- Most selective retrieves fewest pages
- As we saw earlier, for equality predicates
- Selection on equality: $\sigma_{a=v}(R)$
- $V(R, a)=\#$ of distinct values of attribute a
- $1 / V(R, a)$ is thus the reduction factor
- Clustered index on a: cost $B(R) / V(R, a)$
- Unclustered index on a: cost $T(R) / V(R, a)$
- (we are ignoring I/O cost of index pages for simplicity)


## Selectivity for Range Predicates

- Selection on range: $\sigma_{a>v}(R)$
- How to compute the selectivity?
- Assume values are uniformly distributed
- Reduction factor $X$
- $X=(\operatorname{Max}(R, a)-v) /(\operatorname{Max}(R, a)-\operatorname{Min}(R, a))$
- Clustered index on a, cost is $B(R)^{*} X$
- Unclustered index on a, cost is $T(R)^{*} X$


## Back to Our Example

- Selection condition: sid > 300 ^ scity=‘Seattle’
- Index I1: B+-tree on sid clustered
- Index I2: B+-tree on scity unclustered
- Let's assume
- V(Supplier,scity) $=20$
- Max(Supplier, sid) $=1000$, Min(Supplier,sid) $=1$
- B(Supplier) $=100, \mathrm{~T}$ (Supplier) $=1000$
- Cost I1: $\mathrm{B}(\mathrm{R})$ * (Max-v)/(Max-Min) $=100 * 700 / 999 \approx 70$
- Cost I2: $\mathrm{T}(\mathrm{R}) * \mathbf{1 / V}$ (Supplier,scity) $=\mathbf{1 0 0 0} / \mathbf{2 0}=50$


## Selectivity with Multiple Conditions

What if we have an index on multiple attributes?

- Example selection $\sigma_{a=v 1 \wedge b=v 2}(R)$ and index on <a,b>

How to compute the selectivity?

- Assume attributes are independent
- $X=1$ / ( $\mathrm{V}(\mathrm{R}, \mathrm{a})^{*} \mathrm{~V}(\mathrm{R}, \mathrm{b})$ )
- Clustered index on <a,b>: cost $B(R)^{*} X$
- Unclustered index on <a,b>: cost $T(R)^{*} X$


## Computing Cost of an Operator

- The cost of executing an operator depends
- On the operator implementation
- On the input data
- We learned how to compute this in the previous lecture, so we do not repeat it here


## Statistics on the Output Data

- Most important piece of information
- Size of operator result
- I.e., the number of output tuples
- Projection: output size same as input size
- Selection: multiply input size by reduction factor
- Similar to what we did for estimating access path selectivity
- Assume independence between conditions in the predicate
- (use product of the reduction factors for the terms)


## Estimating Result Sizes

- For joins $R \bowtie S$
- Take product of cardinalities of relations $R$ and $S$
- Apply reduction factors for each term in join condition
- Terms are of the form: column1 = column2
- Reduction: 1/ ( MAX( V(R,column1), V(S,column2))
- Assumes each value in smaller set has a matching value in the larger set


## Our Example

- Suppliers(sid,sname,scity,sstate)
- Supplies(pno,sid,quantity)
- Some statistics
- T(Supplier) = 1000 records
- B(Supplier) $=100$ pages
- T(Supplies) = 10,000 records
- B(Supplies) $=100$ pages
- $\mathrm{V}($ Supplier,scity $)=20, \mathrm{~V}($ Supplier,state $)=10$
- V(Supplies,pno) $=3,000$
- Both relations are clustered


## Physical Query Plan 1

(On the fly)
(On the fly)

Selection and project on-the-fly -> No additional cost.

Total cost of plan is thus cost of join:
$=\mathrm{B}$ (Supplier)+B(Supplier)*B(Supplies)
= $100+100$ * 100
$=10,100 \mathrm{I} / \mathrm{Os}$

Supplies
(File scan)

## Physical Query Plan 2



## Physical Query Plan 3

(On the fly)
(4) $\pi_{\text {sname }}$
(On the fly)
(3) $\sigma_{\text {scity }}=‘$ Seattle' $\wedge$ sstate $=' W A '$

Total cost
$=1$ (1)
+4 (2)
+0 (3)
+0 (3)
Total cost $\approx 5 \mathrm{I} / \mathrm{Os}$
(2) $\underset{\text { sno }=\text { sno }}{\infty}$ (Index nested loop)
(Use hash index) 4 tuples
(1) $\sigma_{p n o=2}$

Supplies
(Hash index on pno )
Assume: clustered

Suppliers
(Hash index on sno)
Clustering does not matter

## Simplifications

- In the previous examples, we assumed that all index pages were in memory
- When this is not the case, we need to add the cost of fetching index pages from disk

