Announcements

- Midterm due now
- Project 3 due next Wednesday

Multiview stereo

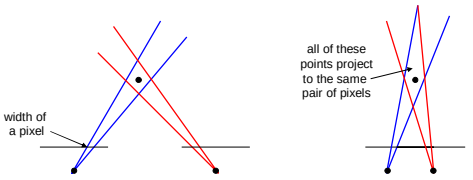
CMU's 3D Room

Stereo with mirrors video

Readings **(Optional)**

- S. M. Seitz and C. R. Dyer, Photorealistic Scene Reconstruction by Voxel Coloring, *International Journal of Computer Vision*, 35(2), 1999, pp. 151-173.

Choosing the Baseline



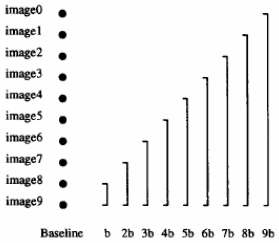
Large Baseline **Small Baseline**

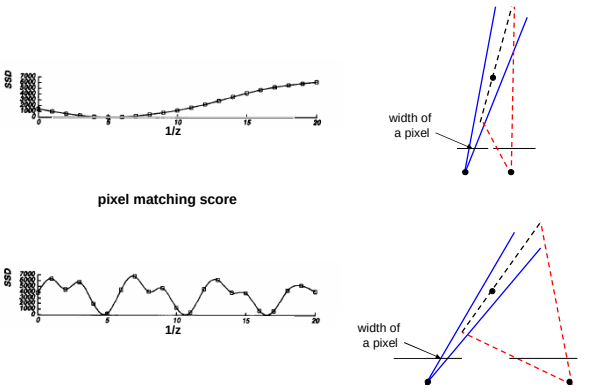
What's the optimal baseline?

- Too small: large depth error
- Too large: difficult search problem

The Effect of Baseline on Depth Estimation

Figure 2: An example scene. The grid pattern in the background has ambiguity of matching.





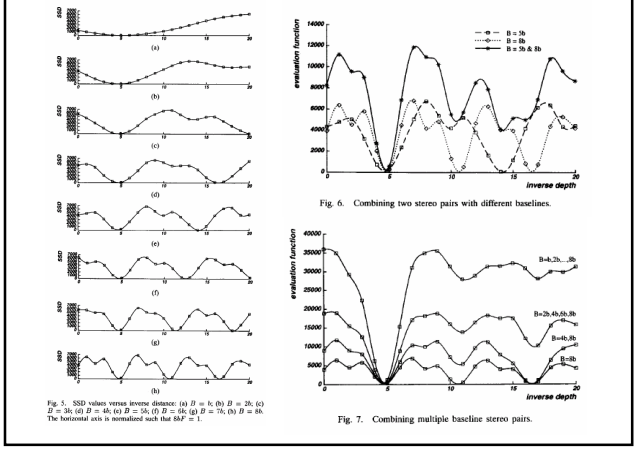


Fig. 6. Combining two stereo pairs with different baselines.

Fig. 5. SSD values versus inverse distance: (a) $B = b$; (b) $B = 2b$; (c) $B = 3b$; (d) $B = 4b$; (e) $B = 5b$; (f) $B = 6b$; (g) $B = 7b$; (h) $B = 8b$. The horizontal axis is normalized such that $bbF = 1$.

Fig. 7. Combining multiple baseline stereo pairs.

Multibaseline Stereo

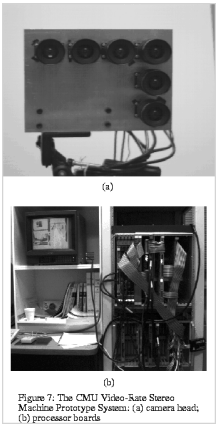
Basic Approach

- Choose a reference view
- Use your favorite stereo algorithm BUT
  - > replace two-view SSD with SSD over all baselines

Limitations

- Must choose a reference view (bad)
- Visibility!

CMU's 3D Room Video



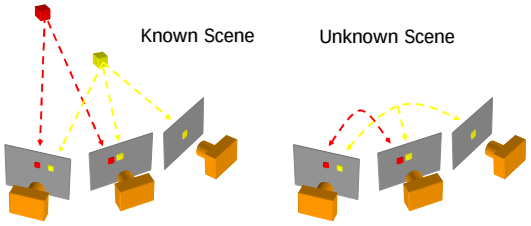
(a)

(b)

Figure 7: The CMU Video-Rate Stereo Machine Prototype System: (a) camera head; (b) processor boards

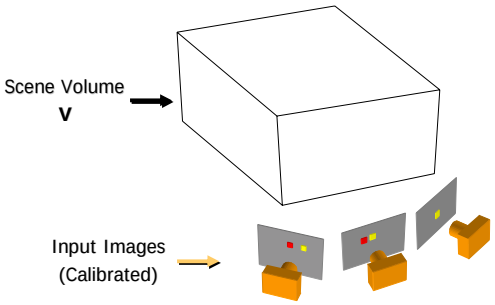
The visibility problem

Which points are visible in which images?



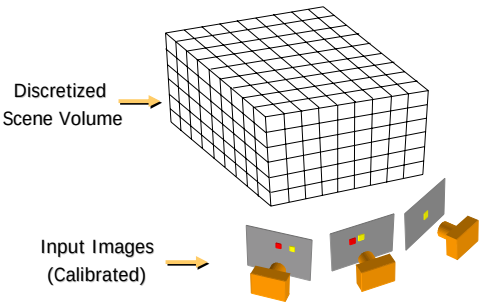
Forward Visibility *Inverse Visibility*

Volumetric stereo



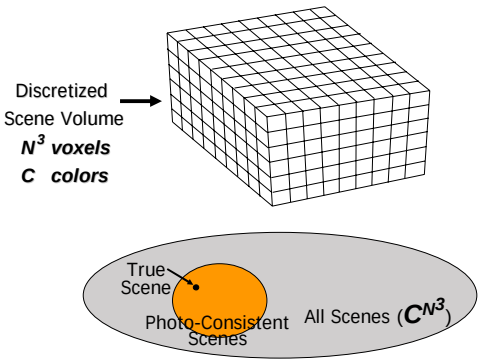
Goal: **Determine occupancy, "color" of points in V**

Discrete formulation: Voxel Coloring



Goal: **Assign RGBA values to voxels in V**
photo-consistent **with images**

Complexity and computability



Issues

Theoretical Questions

- Identify class of *all* photo-consistent scenes

Practical Questions

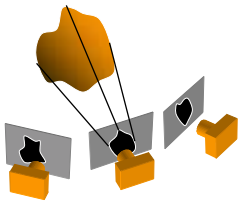
- How do we compute photo-consistent models?

Voxel coloring solutions

1. C=2 (shape from silhouettes)
   - Volume intersection [Baumgart 1974]
     > For more info: *Rapid octree construction from image sequences.* R. Szeliski, CVGIP: Image Understanding, 58(1):23-32, July 1993. (this paper is apparently not available online)
2. C unconstrained, viewpoint constraints
   - Voxel coloring algorithm [Seitz & Dyer 97]
3. General Case
   - Space carving [Kutulakos & Seitz 98]

Reconstruction from Silhouettes (C = 2)

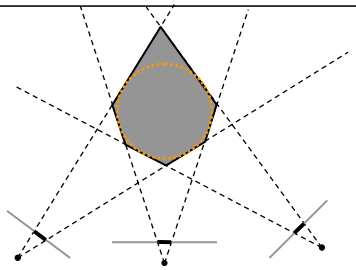
Binary Images →



Approach:

- *Backproject* each silhouette
- Intersect backprojected volumes

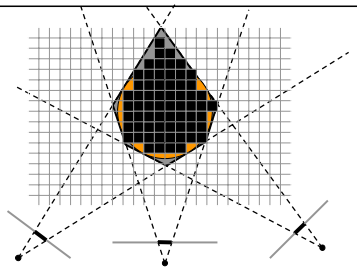
Volume intersection



Reconstruction Contains the True Scene

- But is generally not the same
- In the limit (all views) get *visual hull*
  > Complement of all lines that don't intersect S

Voxel algorithm for volume intersection



Color voxel black if on silhouette in every image

- O(?), for M images, N^3 voxels
- Don't have to search 2^{N^3} possible scenes!

Properties of Volume Intersection

Pros

- Easy to implement, fast
- Accelerated via octrees [Szeliski 1993]

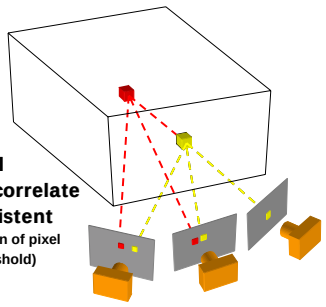
Cons

- No concavities
- Reconstruction is not photo-consistent
- Requires identification of silhouettes

Voxel Coloring Solutions

1. C=2 (silhouettes)
   - Volume intersection [Baumgart 1974]
2. C unconstrained, viewpoint constraints
   - Voxel coloring algorithm [Seitz & Dyer 97]
     > For more info: http://www.cs.washington.edu/homes/seitz/papers/ijcv99.pdf
3. General Case
   - Space carving [Kutulakos & Seitz 98]

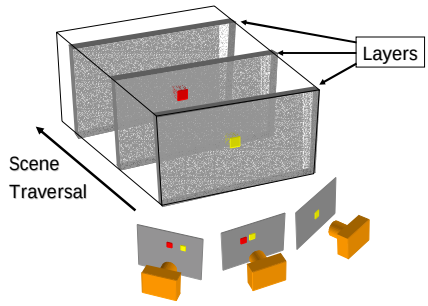
Voxel Coloring Approach



1. **Choose voxel**
2. **Project and correlate**
3. **Color if consistent**
   (standard deviation of pixel colors below threshold)

Visibility Problem: **in which images is each voxel visible?**

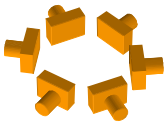
Depth Ordering: visit occluders first!



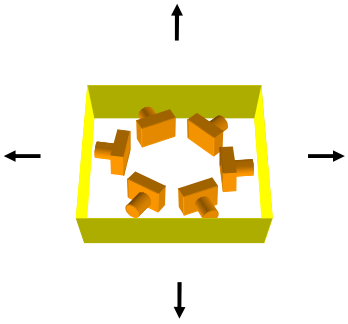
Condition: depth order is the *same for all input views*

Panoramic Depth Ordering

- Cameras oriented in many different directions
- Planar depth ordering does not apply

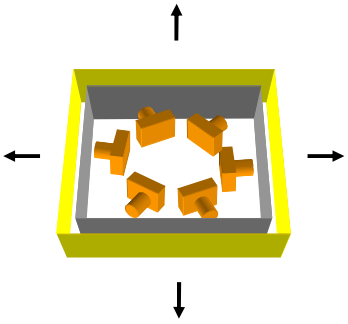


Panoramic Depth Ordering



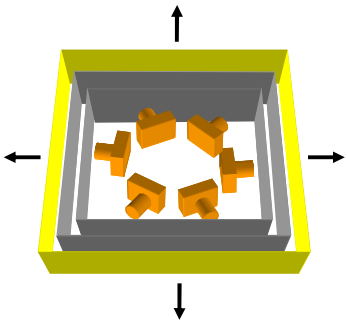
Layers radiate outwards from cameras

Panoramic Layering



Layers radiate outwards from cameras

Panoramic Layering

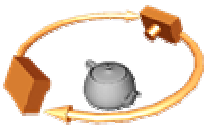


Layers radiate outwards from cameras

Compatible Camera Configurations

Depth-Order Constraint

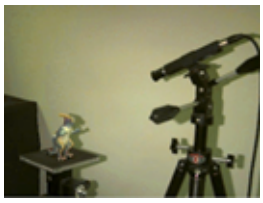
- Scene outside convex hull of camera centers



Inward-Looking

Outward-Looking

Calibrated Image Acquisition



Calibrated Turntable

Selected Dinosaur Images

Selected Flower Images

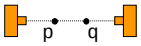
Voxel Coloring Results (Video)

Dinosaur Reconstruction
72 K voxels colored
7.6 M voxels tested
7 min. to compute
on a 250MHz SGI

Flower Reconstruction
70 K voxels colored
7.6 M voxels tested
7 min. to compute
on a 250MHz SGI

Limitations of Depth Ordering

A view-independent depth order may not exist



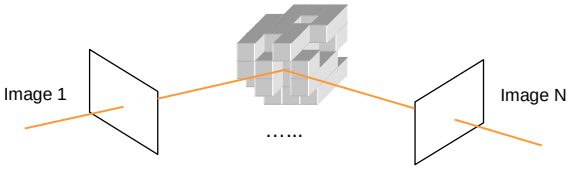
Need more powerful general-case algorithms

- Unconstrained camera positions
- Unconstrained scene geometry/topology

Voxel Coloring Solutions

1. C=2 (silhouettes)
   - Volume intersection [Baumgart 1974]
2. C unconstrained, viewpoint constraints
   - Voxel coloring algorithm [Seitz & Dyer 97]
3. General Case
   - Space carving [Kutulakos & Seitz 98]
     > For more info: http://www.cs.washington.edu/homes/seitz/papers/kutu-ijcv00.pdf

Space Carving Algorithm



Space Carving Algorithm

- Initialize to a volume V containing the true scene
- Choose a voxel on the current surface
- Project to visible input images
- Carve if not photo-consistent
- Repeat until convergence

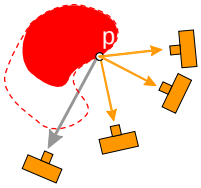
Convergence

Consistency Property

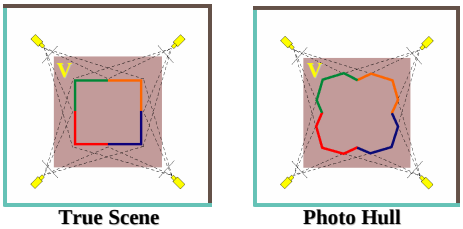
- The resulting shape is photo-consistent
  > all inconsistent points are removed

Convergence Property

- Carving converges to a non-empty shape
  > a point on the true scene is *never* removed



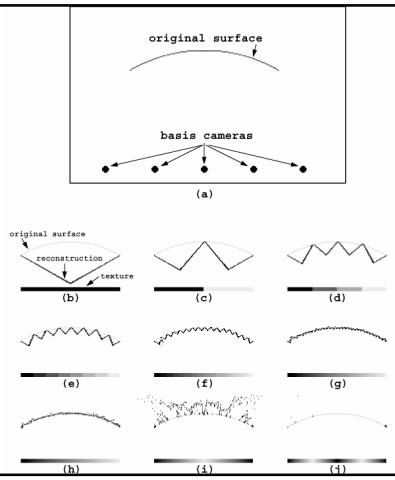
Which shape do you get?



True Scene **Photo Hull**

The Photo Hull *is the UNION of all photo-consistent scenes in V*

- It is a photo-consistent scene reconstruction
- Tightest possible bound on the true scene



Space Carving Algorithm

The Basic Algorithm is Unwieldy

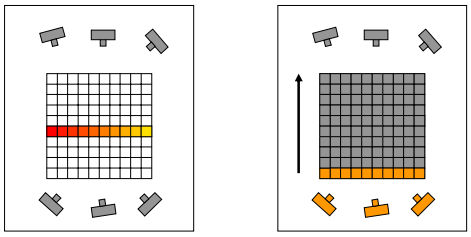
- Complex update procedure

Alternative: Multi-Pass Plane Sweep

- Efficient, can use texture-mapping hardware
- Converges quickly in practice
- Easy to implement

Multi-Pass Plane Sweep

- Sweep plane in each of 6 principle directions
- Consider cameras on only one side of plane
- Repeat until convergence



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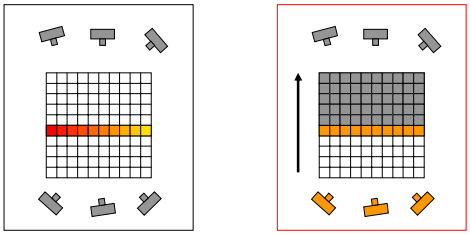

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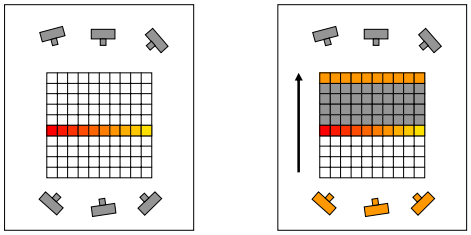

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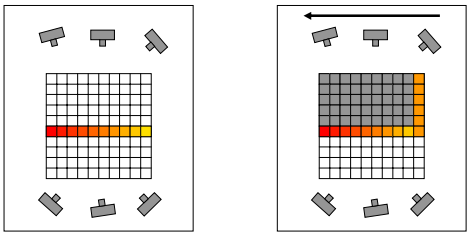

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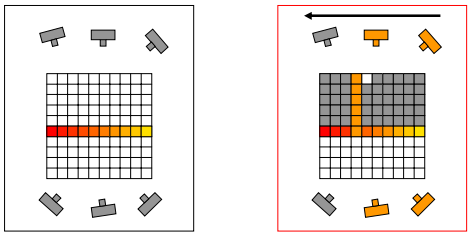

Multi-Pass Plane Sweep

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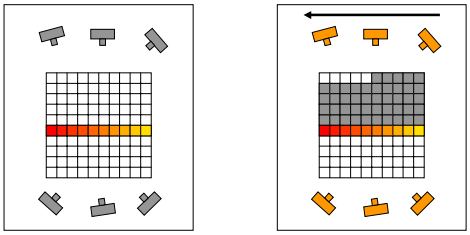
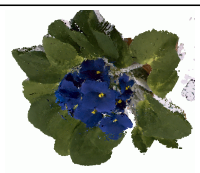


Space Carving Results: African Violet

Input Image (1 of 45)

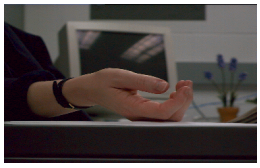


Reconstruction

Reconstruction

Reconstruction

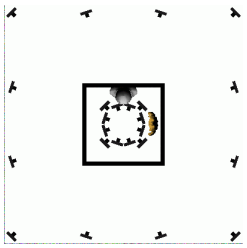
Space Carving Results: Hand



Input Image
(1 of 100)

Views of Reconstruction

House Walkthrough



24 rendered input views from inside *and* outside

Space Carving Results: House

Input Image
(true scene)

Reconstruction
370,000 voxels

Space Carving Results: House

Input Image
(true scene)

Reconstruction
370,000 voxels

Space Carving Results: House

New View (true scene)

Reconstruction

New View
(true scene)

Reconstruction

Reconstruction
(with new input view)

Other Features

Coarse-to-fine Reconstruction

- Represent scene as octree
- Reconstruct low-res model first, then refine

Hardware-Acceleration

- Use texture-mapping to compute voxel projections
- Process voxels an entire plane at a time

Limitations

- Need to acquire calibrated images
- Restriction to simple radiance models
- Bias toward maximal (fat) reconstructions
- Transparency not supported

Other Approaches

Level-Set Methods ***[Faugeras & Keriven 1998]***

- Evolve implicit function by solving PDE's

Probabilistic Voxel Reconstruction ***[DeBonet & Viola 1999], [Broadhurst et al. 2001]***

- Solve for voxel uncertainty (also transparency)

Transparency and Matting ***[Szeliski & Golland 1998]***

- Compute voxels with alpha-channel

Max Flow/Min Cut ***[Roy & Cox 1998]***

- Graph theoretic formulation

Mesh-Based Stereo ***[Fua & Leclerc 1995], [Zhang & Seitz 2001]***

- Mesh-based but similar consistency formulation

Virtualized Reality ***[Narayan, Rander, Kanade 1998]***

- Perform stereo 3 images at a time, merge results

Bibliography

Volume Intersection

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- Szeliski, "Rapid Octree Construction from Image Sequences", Computer Vision, Graphics, and Image Processing: Image Understanding, 58(1), 1993, pp. 23-32.

Voxel Coloring and Space Carving

- Seitz & Dyer, "Photorealistic Scene Reconstruction by Voxel Coloring", Proc. Computer Vision and Pattern Recognition (CVPR), 1997, pp. 1067-1073.
- Seitz & Kutulakos, "Plenoptic Image Editing", Proc. Int. Conf. on Computer Vision (ICCV), 1998, pp. 17-24.
- Kutulakos & Seitz, "A Theory of Shape by Space Carving", Proc. ICCV, 1998, pp. 307-314.

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Related References

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- DeBonet & Viola, "Poxels: Probabilistic Voxelized Volume Reconstruction", Proc. Int. Conf. on Computer Vision (ICCV) 1999.
- Broadhurst, Drummond, and Cipolla, "A Probabilistic Framework for Space Carving", International Conference of Computer Vision (ICCV), 2001, pp. 388-393.
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- Szeliski & Golland, "Stereo Matching with Transparency and Matting", Proc. Int. Conf. on Computer Vision (ICCV), 1998, 517-524.
- Roy & Cox, "A Maximum-Flow Formulation of the N-camera Stereo Correspondence Problem", Proc. ICCV, 1998, pp. 492-499.
- Fua & Leclerc, "Object-centered surface reconstruction: Combining multi-image stereo and shading", International Journal of Computer Vision, 16, 1995, pp. 35-56.
- Narayanan, Rander, & Kanade, "Constructing Virtual Worlds Using Dense Stereo", Proc. ICCV, 1998, pp. 3-10.

Summary

Things to take away from this lecture

- Baseline tradeoff
- Multibaseline stereo approach
- Voxel coloring problem
- Volume intersection algorithm
- Voxel coloring algorithm
- Space carving algorithm