## Computer Vision

$$
\begin{aligned}
& \text { CSE } 455 \\
& \text { Learning I }
\end{aligned}
$$

## Linda Shapiro

Professor of Computer Science \& Engineering Professor of Electrical Engineering

## Learning

- AI/Vision systems are complex and may have many parameters.
- It is impractical and often impossible to encode all the knowledge a system needs.
- Different types of data may require very different parameters.
- Instead of trying to hard code all the knowledge, it makes sense to learn it.


## Learning from Observations

- Supervised Learning - learn a function from a set of training examples which are preclassified feature vectors.

| feature vector | class |
| :--- | :---: |
| (shape, color) |  |
| (square, red) | I |
| (square, blue) | I |
| (circle, red) | II |
| (circle blue) | II |
| (triangle, red) | I |
| (triangle, green) | I |
| (ellipse, blue) | II |
| (ellipse, red) | II |

Given a previously unseen feature vector, what is the rule that tells us if it is in class I or class II?
(circle, green)
(triangle, blue)

## Real Observations

\%Training set of Calenouria and Dorenouria @DATA
0,1,1,0,0,0,0,0,0,1,1,2,3,0,1,2,0,0,0,0,0,0,0,0,1,0,0,1,
$0,2,0,0,0,0,1,1,1,0,1,8,0,7,0,0,0,1,0,0,0,0,0,0,0,0,0,0,0,0,1,0,0$, $3,3,4,0,2,1,0,1,1,1,0,0,0,0,1,0,0,1,1$, cal $0,1,0,0,0,1,0,0,0,4,1,2$ ,2,0,1,0,0,0,0,0,1,0,0,3,0,2,0,0,1,1,0,0,1,0,0,0,1,0,1,6,1,8,2,0,0, $0,0,1,0,0,0,0,0,0,0,0,0,0,1,1,0,0,1,2,0,5,0,0,0,0,0,0,0,1,3,0,0,0,0$, $0, \mathrm{cal}$
0,0,1,0,1,0,0,1,0,1,0,0,1,0,3,0,1,0,0,2,0,0,0,0,1,3,0,0,0,0,0,0,1,0, $2,0,2,0,1,8,0,5,0,1,0,1,0,1,1,0,0,0,0,0,0,0,0,0,2,2,0,0,3,0,0,2,1,1$, 5,0,0,0,2,1,3,2,0,1,0,0,cal 0,0,0,0,0,0,0,0,2,0,0,1,2,0,1,1,0,0,0,1 , $0,0,0,0,0,0,0,0,0,1,0,0,0,1,0,0,3,0,0,4,1,8,0,0,0,1,0,0,0,0,0,1,0,1$ , $0,1,0,0,0,0,0,0,4,2,0,2,1,1,2,1,1,0,0,0,0,2,0,0,2,2, \mathrm{cal}$

## Learning from Observations

- Unsupervised Learning - No classes are given. The idea is to find patterns in the data. This generally involves clustering.

- Reinforcement Learning - learn from feedback after a decision is made.


## Topics to Cover

- Inductive Learning
- decision trees
- ensembles
- neural nets
- kernel machines
- Unsupervised Learning
- K-Means Clustering
- Expectation Maximization (EM) algorithm


## Decision Trees

- Theory is well-understood.
- Often used in pattern recognition problems.
- Has the nice property that you can easily understand the decision rule it has learned.


## Decision Tree Hypothesis Space

If the features are continuous, internal nodes may test the value of a feature against a threshold.


## Classic ML example: decision tree for "Shall I play tennis today?"

## The Stonefly Problem



## Imaging Setup at OSU



Transportation Apparatus
Imaging Setup

## Original Image Analysis



Fig. 1 Regions defined by principal curvature. (a) The original, (b) principal curvature, and (c) cleaned binary images. The resulting (d) boundaries and (e) regions that result by applying the watershed transform to (c). (f) The final detected regions created by fitting an ellipse to each region.

## Feature vector: histogram of SIFT descriptors in a bag of words type of approach.

## A Real Decision Tree (WEKA)

part23 < 0.5
part29 < 3.5
part34<0.5
part8 < 2.5
part2 < 0.5
part63 < 3.5
part20 < 1.5 : dor (53/12) [25/8]
part20 >= 1.5
part37 < 2.5 : cal (6/0) [5/2]
part37>= 2.5 : dor (3/1) [2/0]
Calenouria

```
    part63 >= 3.5 : dor (14/0) [3/0]
```

    | part2 >= 0.5 : cal (21/8) [10/4]
    part8 >= \(2.5:\) dor (14/0) [14/0]
    part34 >= 0.5 : cal (38/12) [18/4]
    part29 >= 3.5 : dor (32/0) [10/2]
part23 $>=0.5$
part29 < 7.5 : cal (66/8) [35/12]
part29 >= 7.5
part24 < 5.5 : dor (9/0) [4/0]
part24 >= 5.5 : cal (4/0) [4/0]

## Evaluation

| Correctly Classified Instances | 281 | $73.5602 \%$ |
| :--- | :---: | :--- |
| Incorrectly Classified Instances | 101 | $26.4398 \%$ |
| Kappa statistic | 0.4718 |  |
| Mean absolute error | 0.3493 |  |
| Root mean squared error | 0.4545 |  |
| Relative absolute error | $69.973 \%$ |  |
| Root relative squared error | $90.7886 \%$ |  |
| Total Number of Instances | 382 |  |

=== Detailed Accuracy By Class ===

|  | TP Rate | FP Rate | Precision | Recall | F-Measure | ROC Area Class |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.77 | 0.297 | 0.713 | 0.77 | 0.74 | 0.747 | cal |  |
| 0.703 | 0.23 | 0.761 | 0.703 | 0.731 | 0.747 | dor |  |
| Wg Avg. | 0.736 | 0.263 | 0.737 | 0.736 | 0.735 | 0.747 |  |

=== Confusion Matrix ===

> a b <-- classified as

144 43 | a = cal
58137 | b=dor

$$
\begin{aligned}
& \text { Precision }=T P /(T P+F P) \\
& \text { Recall }=T P /(T P+F N) \\
& F-\text { Measure }=2 \times \text { Precision } \times \text { Recall } \\
& \quad \text { Precision }+ \text { Recall }
\end{aligned}
$$

## Properties of Decision Trees

- They divide the decision space into axis parallel rectangles and label each rectangle as one of the k classes.
- They can represent Boolean functions.
- They are variable size and deterministic.
- They can represent discrete or continuous parameters.
- They can be learned from training data.


## Learning Algorithm for Decision Trees

Growtree(S) /* Binary version */ if ( $\mathrm{y}==0$ for all ( $\mathbf{x}, \mathrm{y}$ ) in S) return newleaf(0) else if ( $y==1$ for all ( $\mathbf{x}, \mathrm{y}$ ) in S) return newleaf(1) else
choose best attribute $\mathrm{x}_{\mathrm{j}}$
$S_{0}=(x, y)$ with $x_{j}=0$
$S_{1}=(x, y)$ with $x_{j}=1$
return new node $\left(\mathrm{x}_{\mathrm{j}}\right.$, Growtree $\left(\mathrm{S}_{0}\right)$, Growtree $\left(\mathrm{S}_{1}\right)$ ) end

How do we choose the best attribute?
What should that attribute do for us?

## Shall I play tennis today? Which attribute should be selected?



## Criterion for attribute selection

- Which is the best attribute?
- The one that will result in the smallest tree
- Heuristic: choose the attribute that produces the "purest" nodes
- Need a good measure of purity!
- Maximal when?
- Minimal when?


## Information Gain

Which test is more informative?

Split over whether Balance exceeds 50K

Split over whether
applicant is employed


Unemployed Employed

## Information Gain

## Impurity/Entropy (informal)

- Measures the level of impurity in a group of examples



## Impurity

## Very impure group



Less impure


Minimum impurity


## Entropy: a common way to measure impurity

- Entropy $=\sum_{i}-p_{i} \log _{2} p_{i}$
$p_{i}$ is the probability of class $i$


Compute it as the proportion of class $i$ in the set.
16/30 are green circles; 14/30 are pink crosses
$\log _{2}(16 / 30)=-.9 ; \quad \log _{2}(14 / 30)=-1.1$
Entropy $=-(16 / 30)(-.9)-(14 / 30)(-1.1)=.99$

- Entropy comes from information theory. The higher the entropy the more the information content.
What does that mean for learning from examples?


## 2-Class Cases:

- What is the entropy of a group in which all examples belong to the same class?
- entropy $=-1 \log _{2} 1=0$
not a good training set for learning

Minimum impurity


Maximum impurity


## Information Gain

- We want to determine which attribute in a given set of training feature vectors is most useful for discriminating between the classes to be learned.
- Information gain tells us how important a given attribute of the feature vectors is.
- We will use it to decide the ordering of attributes in the nodes of a decision tree.


## Calculating Information Gain

Information Gain = entropy(parent) - [average entropy(children)]
parent $-\left(\frac{14}{30} \cdot \log _{2} \frac{14}{30}\right)-\left(\frac{16}{30} \cdot \log _{2} \frac{16}{30}\right)=0.996 \quad \begin{aligned} & \text { child } \\ & \text { entropy }\end{aligned}-\left(\frac{13}{17} \cdot \log _{2} \frac{13}{17}\right)-\left(\frac{4}{17} \cdot \log _{2} \frac{4}{17}\right)=0.787$
Entire population (30 instances)

(Weighted) Average Entropy of Children = $\left(\frac{17}{30} \cdot 0.787\right)+\left(\frac{13}{30} \cdot 0.391\right)=0.615$
Information Gain $=0.996-0.615=0.38$ for this split

## Entropy-Based Automatic Decision Tree Construction

$$
\left.\begin{array}{l}
\text { Training Set } S \\
x_{1}=\left(f_{11}, f_{12}, \ldots f_{1 m}\right) \\
x_{2}=\left(f_{21}, f_{22},\right. \\
f_{2 m}
\end{array}\right)
$$

Node 1
What feature
should be used?


What values?

Quinlan suggested information gain in his ID3 system and later the gain ratio, both based on entropy.

## Using Information Gain to Construct a Decision Tree <br> (1)

Construct child nodes for each value of A. Set S ,

$$
S^{\prime}=\{\mathrm{s} \in \mathrm{~S} \mid \text { value }(\mathrm{A})=\mathrm{v} 1\}
$$

Each has an associated subset of vectors in which A has a particular value.

## (3)

repeat
recursively
till when?

## Simple Example

Training Set: 3 features and 2 classes

| X | Y | Z | C |
| :---: | ---: | ---: | ---: |
| 1 | 1 | 1 | I |
| 1 | 1 | 0 | I |
| 0 | 0 | 1 | II |
| 1 | 0 | 0 | II |

How would you distinguish class I from class II?

| X | Y | Z | C |
| :--- | :--- | :--- | :--- |
| 1 | 1 | 1 | I |
| 1 | 1 | 0 | I |
| 0 | 0 | 1 | II |
| 1 | 0 | 0 | II |

Eparent= 1
Split on attribute X
If $X$ is the best attribute,


GAIN $=1-(3 / 4)(.9184)-(1 / 4)(0)=.3112$

| X | Y | Z | C |
| :--- | ---: | ---: | ---: |
| 1 | 1 | 1 | I |
| 1 | 1 | 0 | I |
| 0 | 0 | 1 | II |
| 1 | 0 | 0 | II |

## Eparent= 1 Split on attribute $Y$



GAIN $=1-(1 / 2) 0-(1 / 2) 0=1$; BEST ONE

| X | Y | Z | C |
| :--- | ---: | ---: | ---: |
| 1 | 1 | 1 | I |
| 1 | 1 | 0 | I |
| 0 | 0 | 1 | II |
| 1 | 0 | 0 | II |

Eparent= 1
Split on attribute Z


GAIN $=1-(1 / 2)(1)-(1 / 2)(1)=0 \quad$ ie. NO GAIN; WORST
feature vector
(square, red) (square, blue) (circle, red) (circle blue)
(triangle, red)
(triangle, green) (ellipse, blue) (ellipse, red)
class
II
I
I
II
II

Try the shape feature

Entropy?

## Entropy? Entropy? Entropy? Entropy? GAIN?



## Many-Valued Features

- Your features might have a large number of discrete values.
Example: pixels in an image have ( $\mathrm{R}, \mathrm{G}, \mathrm{B}$ ) which are each integers between 0 and 255.
- Your features might have continuous values.
Example: from pixel values, we compute gradient magnitude, a continuous feature


## One Solution to Both

- We often group the values into bins

What if we want


## Training and Testing

- Divide data into a training set and a separate testing set.
- Construct the decision tree using the training set only.
- Test the decision tree on the training set to see how it's doing.
- Test the decision tree on the testing set to report its real performance.


## Measuring Performance

- Given a test set of labeled feature vectors
e.g. (square,red) I
- Run each feature vector through the decision tree
- Suppose the decision tree says it belongs to class $X$ and the real label is $Y$
- If $(X=Y)$ that's a correct classification
- If $(X<>Y)$ that's an error


## Measuring Performance

- In a 2-class problem, where the classes are positive or negative (ie. for cancer)
- \# true positives
- \# true negatives
- \# false positives
- \# false negatives
- Accuracy = \#correct / \#total $=(\mathrm{TP}+\mathrm{TN}) /(\mathrm{TP}+\mathrm{TN}+\mathrm{FP}+\mathrm{FN})$
- Precision = TP / (TP + FP)

How many of the ones you said were cancer really were cancer?

- Recall = TP / (TP + FN) How many of the ones who had cancer did you call cancer?


## More Measures

- F-Measure $=2^{*}$ (Precision * Recall) / (Precision + Recall)

Gives us a single number to represent both precision and recall.

In medicine:

- Sensitivity = TP / (TP + FN) = Recall

The sensitivity of a test is the proportion of people who have a disease who test positive for it.

- Specificity = TN / (TN + FP)

The specificity of a test is the number of people who DON'T have a disease who test negative for it.

## Measuring Performance

- For multi-class problems, we often look at the confusion matrix.
true
class
assigned class

|  | $A$ | $B$ | $C$ | $D$ | $E$ | $F$ | $G$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $A$ |  |  |  |  |  |  |  |
| $B$ |  |  |  |  |  |  |  |
| C |  |  |  |  |  |  |  |
| $D$ |  |  |  |  |  |  |  |
| E |  |  |  |  |  |  |  |
| F |  |  |  |  |  |  |  |
| G |  |  |  |  |  |  |  |

$C(i, j)=$ number of times (or percentage) class $i$ is given label $j$.

## Overfitting

- Suppose the classifier $h$ has error (1accuracy) of error ${ }_{\text {train }}(\mathrm{h})$
- And there is an alternate classifier (hypothesis) h' that has error ${ }_{\text {train }}$ (h')
- What if error ${ }_{\text {train }}(\mathrm{h})<$ error $_{\text {train }}\left(\mathrm{h}^{\prime}\right)$
- But error ${ }_{D}(h)>\operatorname{error}_{D}\left(h^{\prime}\right)$ for full test set D
- Then we say h overfits the training data


## What happens as the decision tree gets bigger and bigger?

## Overfitting in Decision Tree Learning



Error on training data goes down, on testing data goes up

## Reduced Error Pruning

- Split data into training and validation sets
- Do until further pruning is harmful

1. Evaluate impact on validation set of pruning each possible node (and its subtree)
2. Greedily remove the one that most improves validation set accuracy

- Then you need an additional independent testing set.


## Effect of Reduced-Error Pruning



The tree is pruned back to the red line where it gives more accurate results on the test data.

- The WEKA example with Calenouria and Dorenouria showed you used the REPTree classifier with 21 nodes.
- The classic decision tree for the same data had 65 nodes.
- Performance was similar for our test set.
- Performance increased using a random forest of 10 trees, each constructed with 7 random features.


## Decision Trees: Summary

- Representation=decision trees
- Bias=preference for small decision trees
- Search algorithm=none
- Heuristic function=information gain or information content or others
- Overfitting and pruning
- Advantage is simplicity and easy conversion to rules.


## Ensembles

- An ensemble is a set of classifiers whose combined results give the final decision.



## MODEL* ENSEMBLES

- Basic Idea
- Instead of learning one model
- Learn several and combine them
- Often this improves accuracy by a lot
- Many Methods
- Bagging
- Boosting
- Stacking

[^0]
## Bagging

- Generate bootstrap replicates of the training set by sampling with replacement
- Learn one model on each replicate
- Combine by uniform voting



## Boosting

- Maintain a vector of weights for samples
- Initialize with uniform weights
- Loop
- Apply learner to weighted samples
- Increase weights of misclassified ones
- Combine models by weighted voting


## Idea of Boosting



## Boosting In More Detail (Pedro Domingos' Algorithm)

1. Set all E weights to 1, and learn H1.
2. Repeat $m$ times: increase the weights of misclassified Es, and learn $\mathrm{H} 2, \ldots \mathrm{Hm}$.
3. H1..Hm have "weighted majority" vote when classifying each test Weight $(\mathrm{H})=$ accuracy of H on the training data

## ADABoost

- ADABoost boosts the accuracy of the original learning algorithm.
- If the original learning algorithm does slightly better than $50 \%$ accuracy, ADABoost with a large enough number of classifiers is guaranteed to classify the training data perfectly.


# ADABoost Weight Updating (from Fig 18.34 text) 

/* First find the sum of the weights of the misclassified samples */
for $\mathrm{j}=1$ to N do /* go through training samples */ if $\mathrm{h}[\mathrm{m}]\left(\mathrm{x}_{\mathrm{j}}\right)<>\mathrm{y}_{\mathrm{j}}$ then error <- error $+\mathrm{w}_{\mathrm{j}}$
/* Now use the ratio of error to 1 -error to change the weights of the correctly classified samples */ for $\mathrm{j}=1$ to N do if $h[m]\left(x_{j}\right)=y_{j}$ then $w[j]<-w[j]$ * error/(1-error)

## Example

- Start with 4 samples of equal weight . 25 .
- Suppose 1 is misclassified. So error = 25 .
- The ratio comes out $.25 / .75=.33$
- The correctly classified samples get weight of $.25^{*} .33=.0825$
. 2500
.0825
.0825
. 0825 We want them to add up to 1 , not .4975 .
What's wrong? What should we do?

Answer: To normalize, divide each one by their sum (. 4975 or .5).

## Sample Application: Insect Recognition



Using circular regions of interest selected by an interest operator, train a classifier to recognize the different classes of insects.

## Boosting Comparison

- ADTree classifier only (alternating decision tree)
- Correctly Classified Instances

| 268 | $70.1571 \%$ |
| :---: | :---: |
| 114 | $29.8429 \%$ |
| 0.3855 |  |
| $77.2229 \%$ |  |


| Classified as -> | Hesperperla | Doroneuria |
| :--- | :---: | :---: |
| Real <br> Hesperperlas | 167 | 28 |
| Real <br> Doroneuria | 51 | 136 |

## Boosting Comparison

## AdaboostM1 with ADTree classifier

- Correctly Classified Instances 303 79.3194 \%
- Incorrectly Classified Instances 79 20.6806 \%
- Mean absolute error
- Relative absolute error
0.2277
45.6144 \%

| Classified as -> | Hesperperla | Doroneuria |
| :--- | :---: | :---: |
| Real <br> Hesperperlas | 167 | 28 |
| Real <br> Doroneuria | 51 | 136 |

## Boosting Comparison

- RepTree classifier only (reduced error pruning)
- Correctly Classified Instances

| 294 | $75.3846 \%$ |
| :---: | ---: |
| 96 | $24.6154 \%$ |
| 0.3012 |  |
| $60.606 \%$ |  |


| Classified as $->$ | Hesperperla | Doroneuria |
| :--- | :---: | :---: |
| Real <br> Hesperperlas | 169 | 41 |
| Real <br> Doroneuria | 55 | 125 |

## Boosting Comparison

## AdaboostM1 with RepTree classifier

- Correctly Classified Instances
- Incorrectly Classified Instances
324
66
0.1978
$39.7848 \%$

| Classified as $->$ | Hesperperla | Doroneuria |
| :--- | :---: | :---: |
| Real <br> Hesperperlas | 180 | 30 |
| Real <br> Doroneuria | 36 | 144 |

## References

- AdaboostM1: Yoav Freund and Robert E. Schapire (1996). "Experiments with a new boosting algorithm". Proc International Conference on Machine Learning, pages 148156, Morgan Kaufmann, San Francisco.
- ADTree: Freund, Y., Mason, L.: "The alternating decision tree learning algorithm". Proceeding of the Sixteenth International Conference on Machine Learning, Bled, Slovenia, (1999) 124133.


## Stacking

- Apply multiple base learners (e.g.: decision trees, naive Bayes, neural nets)
- Meta-learner: Inputs $=$ Base learner predictions
- Training by leave-one-out cross-validation: Meta-L. inputs $=$ Predictions on left-out examples



## Random Forests

- Tree bagging creates decision trees using the bagging technique. The whole set of such trees (each trained on a random sample) is called a decision forest. The final prediction takes the average (or majority vote).
- Random forests differ in that they use a modified tree learning algorithm that selects, at each candidate split, a random subset of the features.


## Back to Stone Flies

Random forest of 10 trees, each constructed while considering 7 random features. Out of bag error: 0.2487 . Time taken to build model: 0.14 seconds

| Correctly Classified Instances | 292 |
| :--- | :---: |
| Incorrectly Classified Instances | 90 |
| Kappa statistic | 0.5272 |
| Mean absolute error | 0.344 |
| Root mean squared error | 0.4069 |
| Relative absolute error | $68.9062 \%$ |
| Root relative squared error | $81.2679 \%$ |
| Total Number of Instances | 382 |

76.4398 \% (81.4 with AdaBoost) 23.5602 \%

Kappa statistic
Mean absolute error
0.344
0.4069
68.9062 \%
81.2679 \%

382

|  | TP Rate 0.69 | FP Rate | Precision R |  | Recall F-Measure |  | ROC Area Class |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0.164 | 0.801 | 0.69 | 0.741 | 0.848 | cal |
|  | 0.836 | 0.31 | 0.738 | 0.836 | 0.784 | 0.848 | dor |
| WAvg. | 0.764 | 0.239 | 0.769 | 0.764 | 0.763 | 0.848 |  |

> a b <-- classified as
$12958 \mid a=c a l$
32163 | b = dor



[^0]:    *A model is the learned decision rule. It can be as simple as a hyperplane in n-space (ie. a line in 2D or plane in 3D) or in the form of a decision tree or other modern classifier.

