











Perspective projections pros and cons:

- + Size varies inversely with distance looks realistic
- Distance and angles are not (in general) preserved
- Parallel lines do not (in general) remain parallel

Parallel projection pros and cons:

- Less realistic looking
- + Good for exact measurements
- + Parallel lines remain parallel
- Angles not (in general) preserved



Parallel projections

For parallel projections, we specify a **direction of projection** (**DOP**) instead of a COP.

There are two types of parallel projections:

- Orthographic projection DOP perpendicular to PP
- Oblique projection DOP not perpendicular to PP





For parallel projections, we specify a **direction of projection** (DOP) instead of a COP.

We can write orthographic projection onto the z=0 plane with a simple matrix.

$$\begin{bmatrix} x'\\y'\\1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0\\0 & 1 & 0 & 0\\0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x\\y\\z\\1 \end{bmatrix}$$

Normally, we do not drop the z value right away. Why not?







Properties of projections

The perspective projection is an example of a **projective transformation**.

Here are some properties of projective transformations:

- Lines map to lines
- Parallel lines *don't* necessarily remain parallel
- Ratios are not preserved



Coordinate systems for CG

- **Model space** for describing the objections (aka "object space", "world space")
- World space for assembling collections of objects (aka "object space", "problem space", "application space")
- Eye space a canonical space for viewing (aka "camera space")
- Screen space the result of perspective transformation (aka "normalized device coordinate space", "normalized projection space")
- Image space a 2D space that uses device coordinates (aka "window space", "screen space", "normalized device coordinate space", "raster space")









Perspective depth

Q: What did our perspective projection do to z?

Often, it's useful to have a z around — e.g., for hidden surface calculations.





Perspective drawings are often classified by the number of principal vanishing points.

- One-point perspective simplest to draw
- Two-point perspective gives better impression of depth
- Three-point perspective most difficult to draw

All three types are equally simple with computer graphics.









Summary

Here's what you should take home from this lecture:

- The classification of different types of projections.
- The concepts of vanishing points and one-, two-, and three-point perspective.
- An appreciation for the various coordinate systems used in computer graphics.
- How the perspective transformation works.