

What are particle systems?

A **particle system** is a collection of point masses that obeys some physical laws (e.g, gravity or spring behaviors).

Particle systems can be used to simulate all sorts of physical phenomena:

Reading

Required:

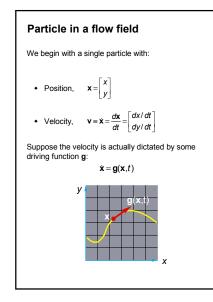
- Witkin, Particle System Dynamics, SIGGRAPH '97 course notes on Physically Based Modeling.
- Witkin and Baraff, Differential Equation Basics, SIGGRAPH '97 course notes on Physically Based Modeling.

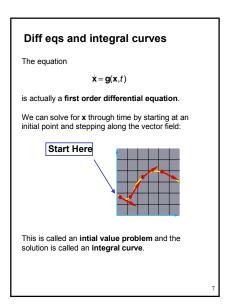
Optional

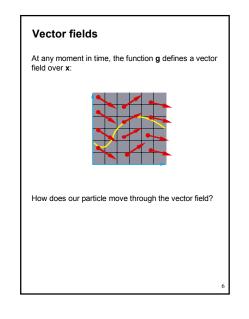
- Hocknew and Eastwood. Computer simulation using particles. Adam Hilger, New York, 1988.
 Gavin Miller. "The motion dynamics of snakes
- and worms." *Computer Graphics* 22:169-178, 1988.

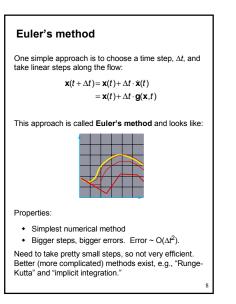
Overview

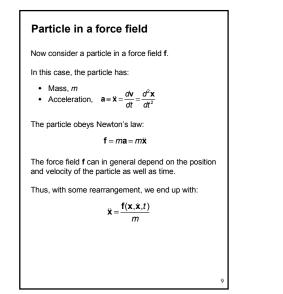
- A single particle
- Particle systems
- Forces: gravity, springs
- Collision detection

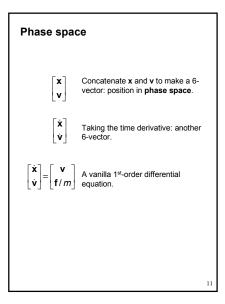


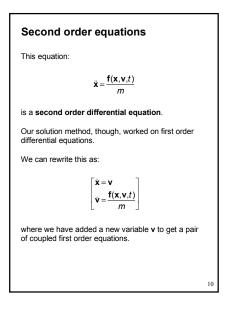




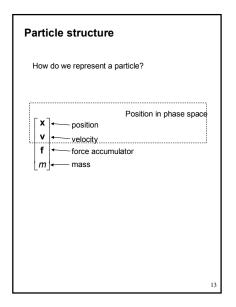


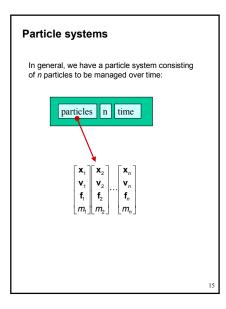


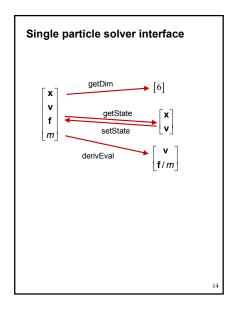


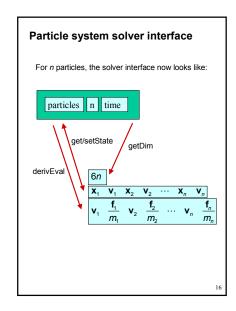


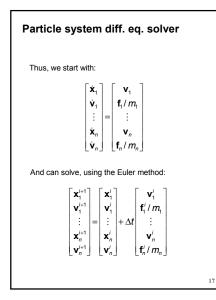
Differential equation solver	
Starting with:	
$\begin{bmatrix} \dot{\mathbf{x}} \\ \dot{\mathbf{v}} \end{bmatrix} = \begin{bmatrix} \mathbf{v} \\ \mathbf{f}/m \end{bmatrix}$	
Applying Euler's method:	
$\mathbf{x}(t + \Delta t) = \mathbf{x}(t) + \Delta t \cdot \dot{\mathbf{x}}(t)$ $\dot{\mathbf{x}}(t + \Delta t) = \dot{\mathbf{x}}(t) + \Delta t \cdot \ddot{\mathbf{x}}(t)$	
And making substitutions:	
$\mathbf{x}(t + \Delta t) = \mathbf{x}(t) + \Delta t \cdot \mathbf{v}(t)$ $\dot{\mathbf{x}}(t + \Delta t) = \dot{\mathbf{x}}(t) + \Delta t \cdot \frac{\mathbf{f}(\mathbf{x}, \dot{\mathbf{x}}, t)}{m}$	
Writing this as an iteration, we have:	
$\mathbf{x}^{i+1} = \mathbf{x}^i + \Delta t \cdot \mathbf{v}^i$	
$\mathbf{v}^{i+1} = \mathbf{v}^i + \Delta t \cdot \frac{\mathbf{f}^i}{m}$	
Again, performs poorly for large Δt .	
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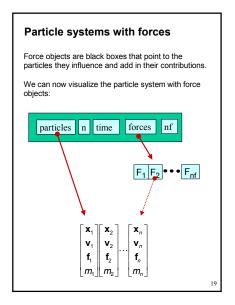


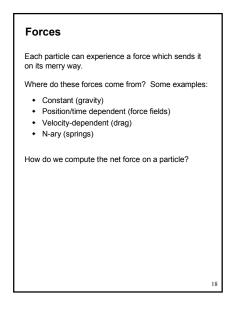


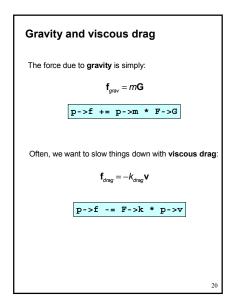


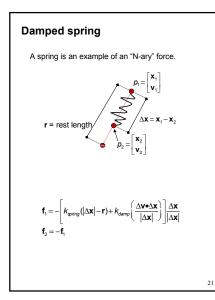


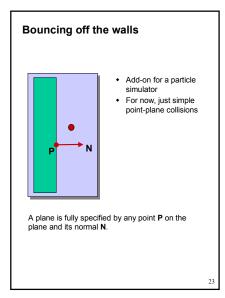


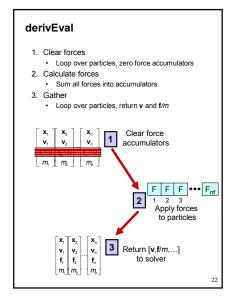


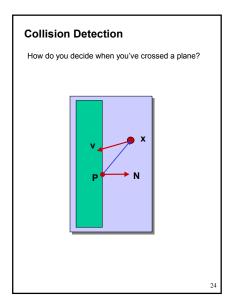


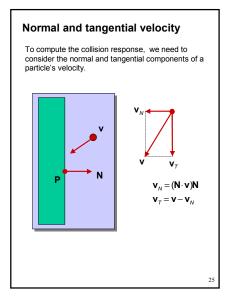


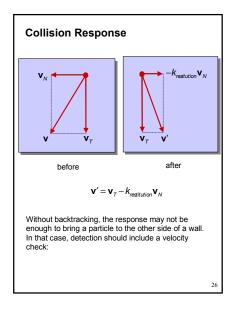












Summary

What you should take away from this lecture:

- The meanings of all the **boldfaced** terms
- Euler method for solving differential equations

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- Combining particles into a particle system
- Physics of a particle system
- Various forces acting on a particle
- Simple collision detection