

# Texture Mapping

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Adapted from Brian Curless  
CSE 457  
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## Reading

### Recommended

- ♦ Angel, 8.6, 8.7, 8.9, 8.10, 9.13-9.13.2
- ♦ Paul S. Heckbert. Survey of texture mapping. **IEEE Computer Graphics and Applications** 6(11): 56--67, November 1986.

### Optional

- ♦ Woo, Neider, & Davis, Chapter 9
- ♦ James F. Blinn and Martin E. Newell. Texture and reflection in computer generated images. **Communications of the ACM** 19(10): 542--547, October 1976.

## Texture mapping



Texture mapping (Woo et al., fig. 9-1)

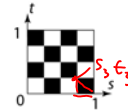
Texture mapping allows you to take a simple polygon and give it the appearance of something much more complex.

- ♦ Due to Ed Catmull, PhD thesis, 1974
- ♦ Refined by Blinn & Newell, 1976

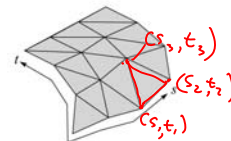
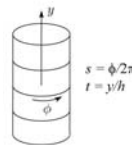
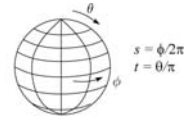
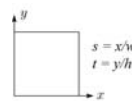
A texture can modulate just about any parameter – diffuse color, specular color, specular exponent, ...

## Implementing texture mapping

A texture lives in its own abstract image coordinates parameterized by  $(s,t)$  in the range  $([0..1], [0..1])$ :



It can be wrapped around many different surfaces:



With a ray caster, we can do the sphere and cylinder mappings directly (as we will see later). For z-buffers, everything gets converted to a triangle mesh with associated  $(s,t)$  coordinates.

Note: if the surface moves/deforms, the texture goes with it.

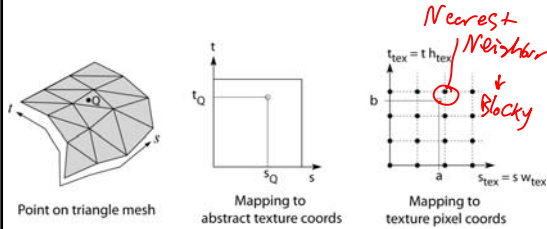
## Mapping to texture image coords

The texture is usually stored as an image. Thus, we need to convert from abstract texture coordinate:

$(s, t)$  in the range  $([0..1], [0..1])$

to texture image coordinates:

$(s_{tex}, t_{tex})$  in the range  $([0..w_{tex}], [0..h_{tex}])$



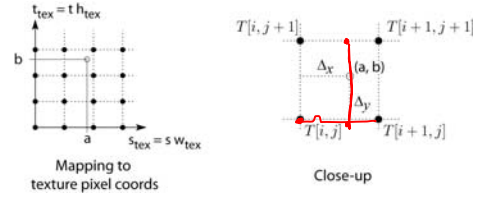
**Q:** What do you do when the texture sample you need lands between texture pixels?

5

## Texture resampling

$$0 \leq \Delta x, \Delta y \leq 1$$

We need to resample the texture:



Thus, we seek to solve for:  $T(a, b) = T(i + \Delta x, j + \Delta y)$

A common choice is **bilinear interpolation**:

$$T(i + \Delta x, j) = (1 - \Delta x) T[i, j] + \Delta x T[i + 1, j]$$

$$T(i + \Delta x, j + 1) = (1 - \Delta x) T[i, j + 1] + \Delta x T[i + 1, j + 1]$$

$$\begin{aligned} T(i + \Delta x, j + \Delta y) &= (1 - \Delta y) T(i + \Delta x, j) + \Delta y T(i + \Delta x, j + 1) \\ &= (1 - \Delta x)(1 - \Delta y) T[i, j] + \Delta x(1 - \Delta y) T[i + 1, j] + \\ &\quad (1 - \Delta x)\Delta y T[i, j + 1] + \Delta x \Delta y T[i + 1, j + 1] \end{aligned}$$

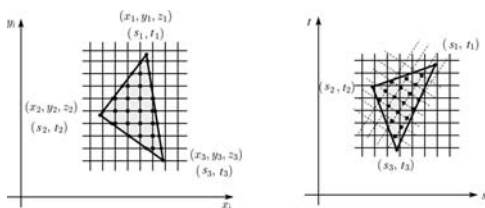
6

## Texture mapping and the z-buffer

Texture-mapping can also be handled in z-buffer algorithms.

Method:

- Scan conversion is done in screen space, as usual
- Each pixel is colored according to the texture
- Texture coordinates are found by Gouraud-style interpolation



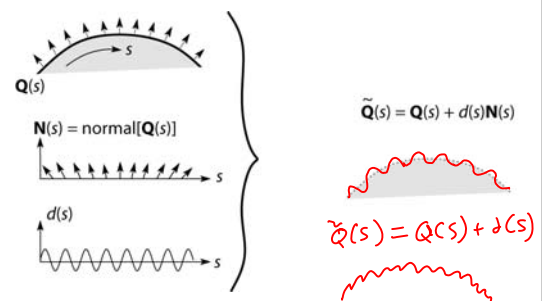
**Note:** Mapping is more complicated to handle perspective correctly!

7

## Displacement mapping

Textures can be used for more than just color.

In **displacement mapping**, a texture is used to perturb the surface geometry itself. Here's the idea in 2D:



- These displacements "animate" with the surface
- In 3D, you would of course have  $(s, t)$  parameters instead of just  $s$ .

Suppose  $Q$  is a simple surface, like a cube. Will it take more work to render the modified surface  $Q$ ? *Much more*

8

## Bump mapping

In **bump mapping**, a texture is used to perturb the normal:

- Use the original, simpler geometry,  $Q(s)$ , for hidden surfaces
- Use the normal from the displacement map for shading:

$$\tilde{N} = \text{normal}[\tilde{Q}(s)]$$



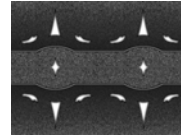
What artifacts in the images would reveal that bump mapping is a fake?

Shadows Silhouettes  
lighting perspective

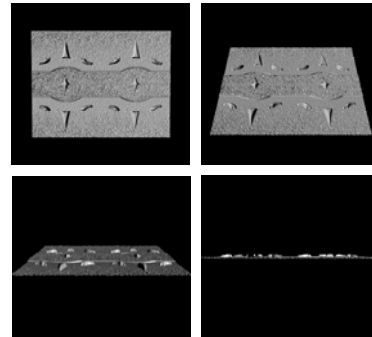
9

## Displacement vs. bump mapping

Input texture



Rendered as displacement map over a rectangular surface



10

## Displacement vs. bump mapping (cont'd)



Original rendering

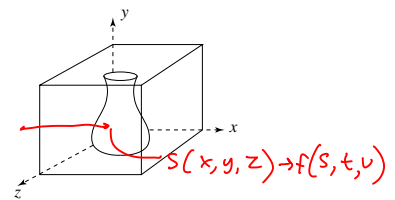
Rendering with bump map wrapped around a cylinder

Bump map and rendering by Wyvern Aldinger

11

## Solid textures

Q: What kinds of artifacts might you see from using a marble veneer instead of real marble?



One solution is to use **solid textures**:

- Use model-space coordinates to index into a 3D texture
- Like "carving" the object from the material

One difficulty of solid texturing is coming up with the textures.

12

## Solid textures (cont'd)

Here's an example for a vase cut from a solid marble texture:



*Solid marble texture by Ken Perlin, (Foley, IV-21)*

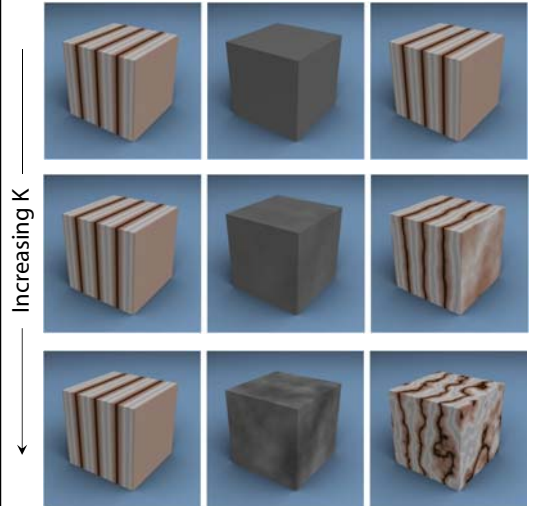
13

## Solid textures (cont'd)

$$\text{in}(x,y,z) = \text{stripes}(x)$$

$$\text{shift}(x,y,z) = K \cdot \text{noise}(x,y,z)$$

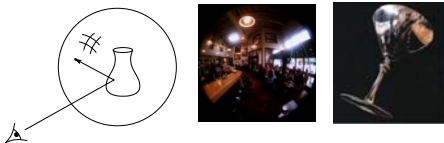
$$\text{out}(x,y,z) = \text{stripes}(x + \text{shift}(x,y,z))$$



Increasing K

14

## Environment mapping



In **environment mapping** (also known as **reflection mapping**), a texture is used to model an object's environment:

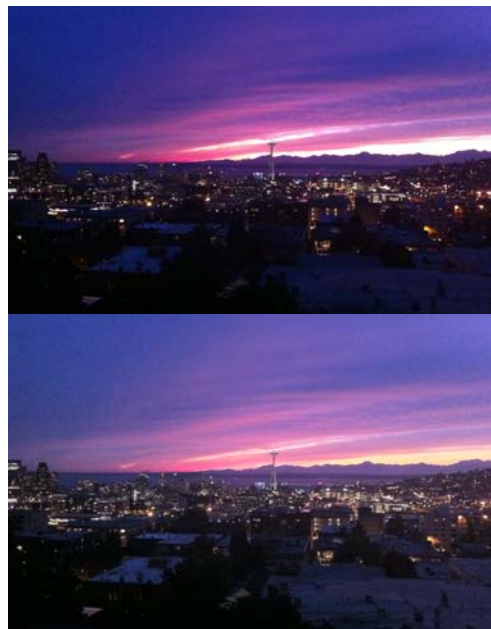
- ♦ Rays are bounced off objects into environment
- ♦ Color of the environment used to determine color of the illumination
- ♦ Environment mapping works well when there is just a single object – or in conjunction with ray tracing

This can be readily implemented (without interreflection) using a fragment shader, where the texture is stored in a "cube map" instead of a sphere.

With a ray tracer, the concept is easily extended to handle refraction as well as reflection (and interreflection).

15

## HDR Capture



16

## **Summary**

What to take home from this lecture:

1. The meaning of the boldfaced terms.
2. Familiarity with the various kinds of texture mapping, including their strengths and limitations.