# Reading

Jain, Kasturi, Schunck, *Machine Vision*. McGraw-Hill, 1995. Sections 4.2-4.4, 4.5(intro), 4.5.5, 4.5.6, 5.1-5.4. [online handut]

# **Image processing**

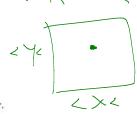
CSE 457 Winter 2014

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# What is an image?

We can think of an  $\boldsymbol{image}$  as a function, f, from  $R^2$  to R:

- f(x, y) gives the intensity of a channel at position (x, y)
- Realistically, we expect the image only to be defined over a rectangle, with a finite range:
  - $f: [a, b] \times [c, d] \rightarrow [0, 1]$



A color image is just three functions pasted together. We can write this as a "vector-valued" function:

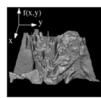
$$f(x,y) = \begin{bmatrix} r(x,y) \\ g(x,y) \\ b(x,y) \end{bmatrix}$$

#### **Images as functions**









#### What is a digital image?

In computer graphics, we usually operate on digital (discrete) images:

- Sample the space on a regular grid
- Quantize each sample (round to nearest integer)

If our samples are  $\Delta$  apart, we can write this as:

$$f[i,j] = \text{Quantize}\{f(i\Delta, j\Delta)\}$$









### **Image processing**

An image processing operation typically defines a new image g in terms of an existing image f.

The simplest operations are those that transform each pixel in isolation. These pixel-to-pixel operations can be written:

g(x,y) = t(f(x,y))

Examples: threshold, RGB → grayscale

Note: a typical choice for mapping to grayscale is to apply the YIQ television matrix and keep the Y.

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### Noise

Image processing is also useful for noise reduction and edge enhancement. We will focus on these applications for the remainder of the lecture...



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Common types of noise:

- Salt and pepper noise: contains random occurrences of black and white pixels
- Impulse noise: contains random occurrences of white pixels
- Gaussian noise: variations in intensity drawn from a Gaussian normal distribution

### Ideal noise reduction



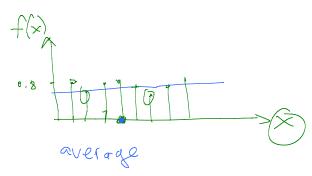
### Ideal noise reduction



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### Practical noise reduction

How can we "smooth" away noise in a single image?



Is there a more abstract way to represent this sort of operation? Of course there is!

### Discrete convolution

One of the most common methods for filtering an image is called **discrete convolution**. (We will just call this "convolution" from here on.)

In 1D, convolution is defined as:

g[n] = f[n] \* h[n]  $= \sum_{n} f[n']h[n-n]$ 

 $=\sum_{n}^{n}f[n']\tilde{h}[n'-n]$ 

where  $\tilde{h}[n] = h[-n]$ .

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### Some properties of discrete convolution

One can show that convolution has some convenient properties. Given functions a, b, c:

Commutativity 
$$a*b=b*a$$

$$(a*b)*c=a*(b*c)$$

$$a*(b+c)=a*b+a*c$$

$$d_1G_{V_1}$$

$$f_{V_2}$$

$$a*b=b*a$$

$$(a*b)*c = a*(b*c)$$

$$a*(b+c)=a*b+a*c$$

We'll make use of these properties later...

#### Convolution in 2D

In two dimensions, convolution becomes:

$$g[n,m] = f[n,m] * h[n,m]$$

$$= \sum \sum f[n',m']h[n-n',m-m']$$

$$= \sum_{m'} \sum_{n'} f[n',m'] h[n-n',m-m']$$

$$= \sum_{m'} \sum_{n'} f[n',m'] \tilde{h}[n'-n,m'-m]$$

where  $\tilde{h}[n,m] = h[-n,-m]$ .

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# **Convolution representation**

Since f and h are defined over finite regions, we can write them out in two-dimensional arrays:

128	54	9	78	100
145	98	240	233	86
89	177	246	228	127
67	90	255	237	95
106	111	128	167	20
221	154	97	123	0

X 0.1	X(0.1)	X 0.1
X 0.1	X 0.2	X(0.1)
X 0.1	X 0.1	X 0.1

Note: This is not matrix multiplication!

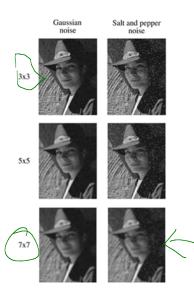
Q: What happens at the boundary of the image?

#### Mean filters

How can we represent our noise-reducing averaging as a convolution filter (know as a mean filter)?

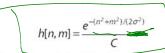
$$h = \frac{1}{NM} \begin{bmatrix} 1 & \cdots & 1 \\ 1 & \cdots & 1 \end{bmatrix} M$$

### **Effect of mean filters**



#### **Gaussian filters**

Gaussian filters weigh pixels based on their distance from the center of the convolution filter. In particular:



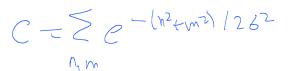
This does a decent job of blurring noise while preserving features of the image.

What parameter controls the width of the Gaussian?

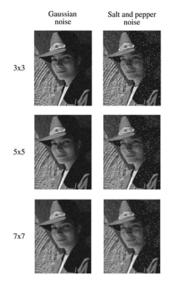
What happens to the image as the Gaussian filter kernel gets wider?

What is the constant C? What should we set it to?

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#### **Effect of Gaussian filters**

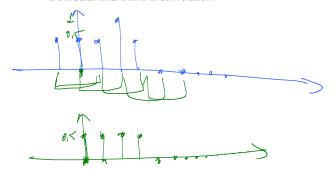


#### **Median filters**

A **median filter** operates over an  $m \times m$  region by selecting the median intensity in the region.

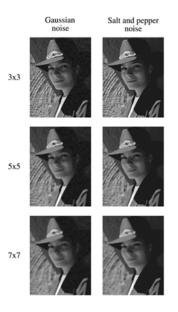
What advantage does a median filter have over a mean filter?

Is a median filter a kind of convolution?

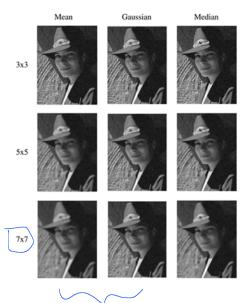


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### **Effect of median filters**



### Comparison: Gaussian noise

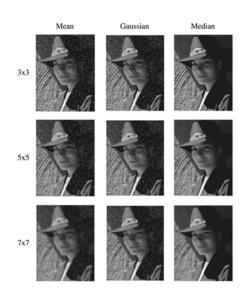


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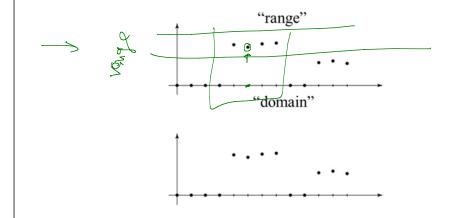
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# Comparison: salt and pepper noise



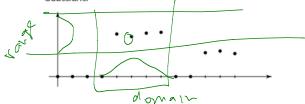
### **Bilateral filtering**

Bilateral filtering is a method to average together nearby samples only if they are similar in value.



### **Bilateral filtering**

We can also change the filter to something "nicer" like



Recall that convolution looked like this:

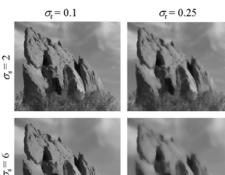
$$g[n] = \sum_{n'} f[n']h[n-n']$$

Bilateral filter is similar, but includes both range and domain filtering:

$$g[n] = 1/C\sum_{n'} f[n'] h_{\sigma_s}[n-n'] h_{\sigma_t}(f[n] - f[n'])$$
and you have to normalize as you go:

$$C = \sum_{n'} h_{\sigma_5}[n-n'] h_{\sigma_t}(f[n] - f[n'])$$





Paris, et al. SIGGRAPH course notes 2007

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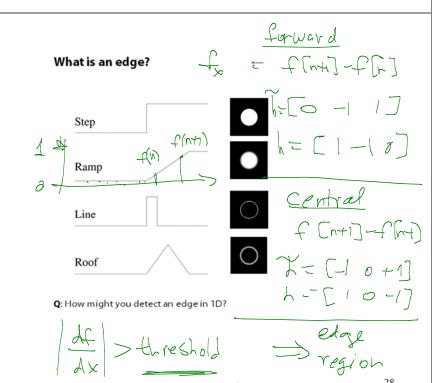
### **Edge detection**

One of the most important uses of image processing is edge detection:

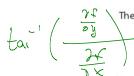
- Really easy for humans
- Really difficult for computers

- Fundamental in computer vision
- Important in many graphics applications

Aomain Knowledge



#### Gradients



The **gradient** is the 2D equivalent of the derivative:

Dequivalent of the derivative: 11 
$$\sqrt{+}$$
  $\sqrt{+}$   $\sqrt{-}$   $\sqrt$ 

Properties of the gradient

- · It's a vector
- Points in the direction of maximum increase of f
- · Magnitude is rate of increase

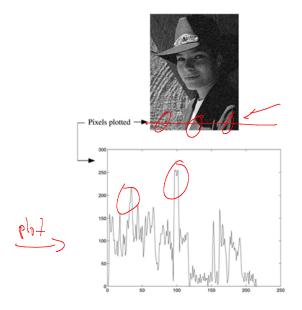
How can we approximate the gradient in a discrete

image?

$$f_{x} = f(n+1,m) - f(n,m) \qquad f_{x} = [1-10]$$

$$f_{y} = f(n,m+1) - f(n,m) \qquad f_{y} = [1-10]$$

#### Less than ideal edges



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## Steps in edge detection

Edge detection algorithms typically proceed in three or four steps:

- Filtering: cut down on noise
- Enhancement: amplify the difference between edges and non-edges
- Detection: use a threshold operation
- Localization (optional): estimate geometry of edges as 1D contours that can pass between pixels

### **Edge enhancement**

A popular gradient filter is the Sobel operator:

← prodien 1 Starring

We can then compute the magnitude of the vector  $(\tilde{s}_x, \tilde{s}_y)$ .

Note that these operators are conveniently "preflipped" for convolution, so you can directly slide these across an image without flipping first.











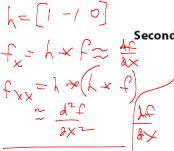


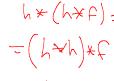




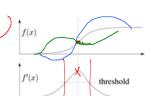
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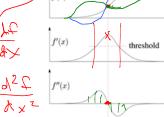
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Second derivative operators





The Sobel operator can produce thick edges. Ideally we're looking for infinitely thin boundaries.

An alternative approach is to look for local extrema in the first derivative: places where the change in the gradient is highest.

Q: A peak in the first derivative corresponds to what in the second derivative?

**Q**: How might we write this as a convolution filter?



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# (1-21)

# Localization with the Laplacian



An equivalent measure of the second derivative in 2D is the Laplacian:

(The symbol  $\Delta$  is often used to refer to the discrete Laplacian filter.)

Zero crossings in a Laplacian filtered image can be used to localize edges.

### Localization with the Laplacian





