#### Lecture 15: Texture Mapping

# Reading

• Hearn & Baker 14.8-14.9

#### Optional

• Paul S. Heckbert. Survey of texture mapping. *IEEE Computer Graphics and Applications* 6(11): 56-67, November 1986

### Texture mapping



Texture mapping allows you to take a simple polygon and give it the appearance of something much more complex

- Due to Ed Catmull, PhD thesis, 1974
- ensures that "all the right things" happen as a texture polygon is transformed and rendered

# Non-parametric texture mapping



With non parametric texture mapping:

- Texture size and orientation are fixed
- Unrelated to size and orientation of polygon
- Gives a cookie-cutter effect

#### Parametric texture mapping



With parametric texture mapping, texture size and orientation are tied to the polygon:

- Separate texture space and screen space
- Texture the polygon as before but in texture space
- Deform (render) the textured polygon into screen space

# Implementing texture mapping

Textures can be warped around many different surfaces:



Computing (u,v) coordinates in a ray tracer is fairly straightforward

# Implementing, cont.

- Texture mapping can also be handled in z-buffer algorithms
- Scan conversion is done in screen space, as usual
- Each pixel is colored according to the texture
- Texture coordinates are found by Gouraud-style interpolation  $(x_1, y_1, z_1)$



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# Antialiasing

• If you point-sample the texture map, you get aliasing:



• Proper antialiasing requires area averaging in the texture:



# Computing average color

Computationally difficult part is summing over the covered pixels:

Several methods have been used:

- 1. Brute force
  - Just sum
- 2. Mip maps
- 3. Summed Area Tables



- Lance Williams, 1983
- "multum in parvo" many things in a small place"
- Keep textures prefiltered at multiple resolutions
- Figure out two closest levels
- Linear interpolate between the two

## Computing average color, cont.



- 3. Summed area tables
- Frank Crow, 1984
- Keep sum of everything below and to the left
- Use four table lookups
- Requires more memory (2-4 times the original image)
- Gives less blurry textures

# Comparison of techniques



#### Solid textures

Q: what kinds of artifacts might you see from using a marble veneer instead of a real marble?



- One solution is to use solid textures
- Use model-space coordinates to index into a 3D texture
- Like "carving" the object from the material
  One difficulty of solid texturing is coming up with the textures...

## Procedural texture mapping

Instead of using texture coordinates to index into an image, use them to compute a function that defines the texture

#### Solid textures, cont.

Vase cut from a solid marble texture:



# Bump mapping

Textures can be used for more than just color

$$I = k_a I_a + \sum_i f(d_i) I_{li} \left( k_d (\mathbf{N} \cdot \mathbf{L}_i)_+ + k_s (\mathbf{V} \cdot \mathbf{R})_+^{n_s} \right)$$

In bump mapping, a texture is used to perturb the normal:

• The normal is perturbed in each parametric direction according to the partial derivatives of the texture



- These bumps "animate" with the surface
- **Q**: What artifacts in the images would reveal that bump mapping is fake?

# Displacement mapping

In displacement mapping, a texture is used to preturb the surface geometry itself:

- Silhouettes are correct
- Requires doing additional hidden surface calculations

#### Displacement mapping, cont.



# Bump mapping example



Original rendering

Rendering with bump map wrapped around a cylinder

# Environment mapping







- A.k.a. reflection mapping
- Use texture to model object's environment
- Rays are bounced off objects into environment to determine color of illumination
- Works well when there is just a single object
- With some simplifications can be implemented in hardware
- Raytracer can be extended to handle refractions as well

# Combining texture maps

• Using texture maps in combination give even better effects



## Combining texture maps, cont.



# Summary

What to take from this lecture:

- What texture mapping is and what is it good for
- Understanding the various approaches to antialiased textured mapping
  - Brute force
  - Mip maps
  - Summed area tables
- Additional effect with texture mapping techniques
  - Bump mapping
  - Displacement mapping
  - Environment mapping