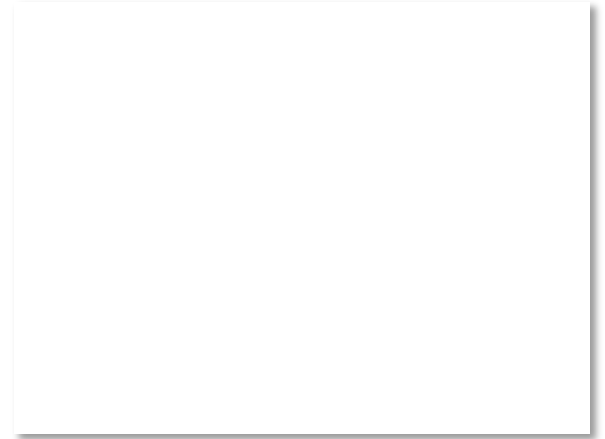
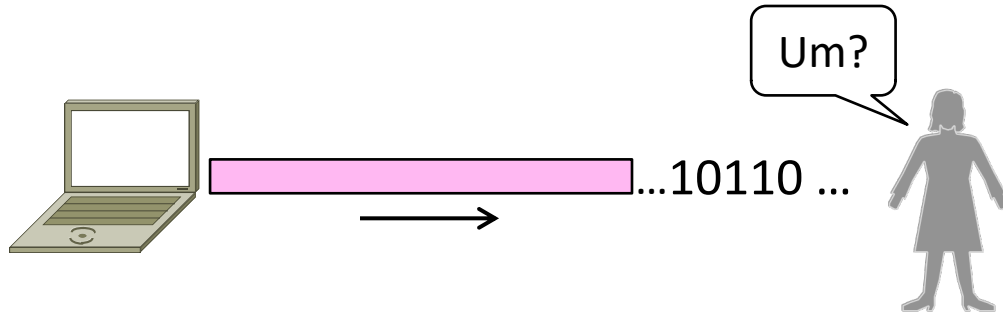


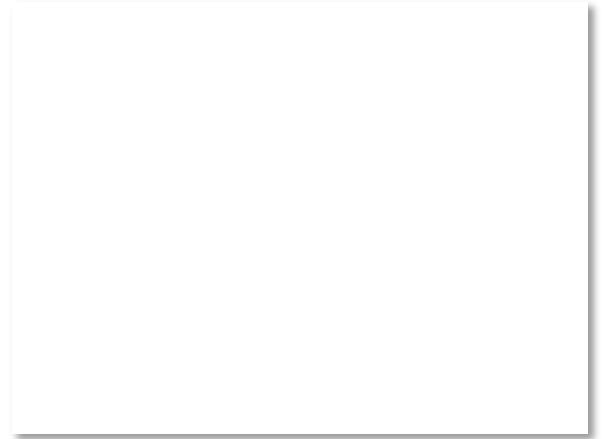
# Topic

- The Physical layer gives us a stream of bits. How do we interpret it as a sequence of frames?



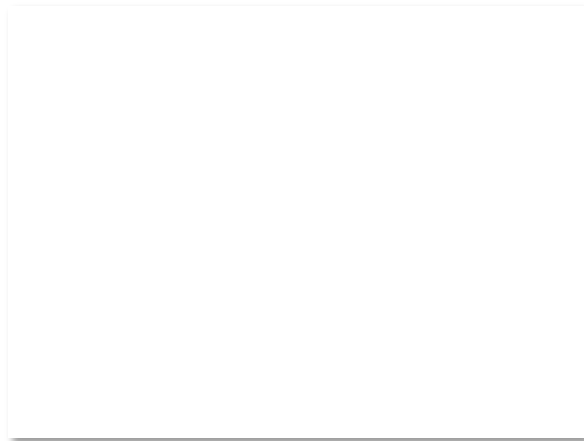
# Framing Methods

- We'll look at:
  - Byte count (motivation)»
  - Byte stuffing »
  - Bit stuffing »
- In practice, the physical layer often helps to identify frame boundaries
  - E.g., Ethernet, 802.11

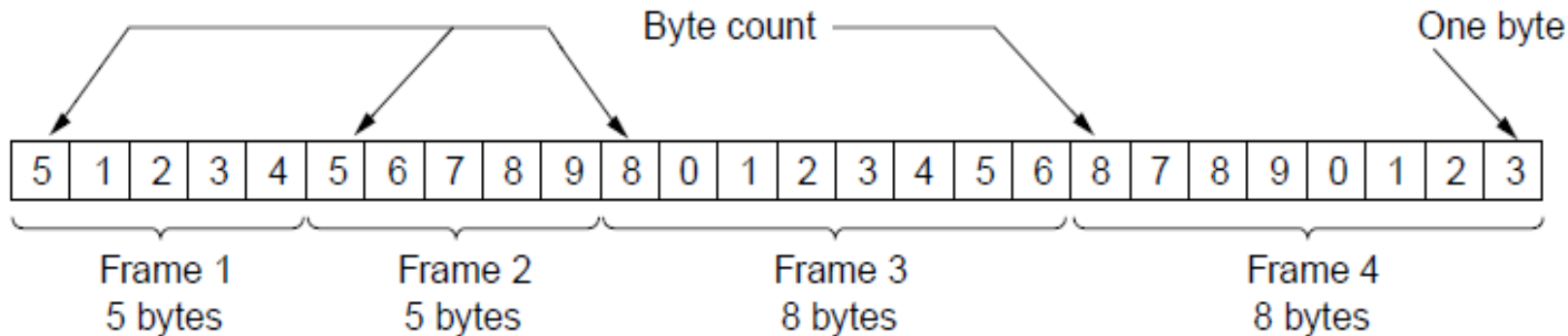


# Byte Count

- First try:
  - Let's start each frame with a length field!
  - It's simple, and hopefully good enough ...



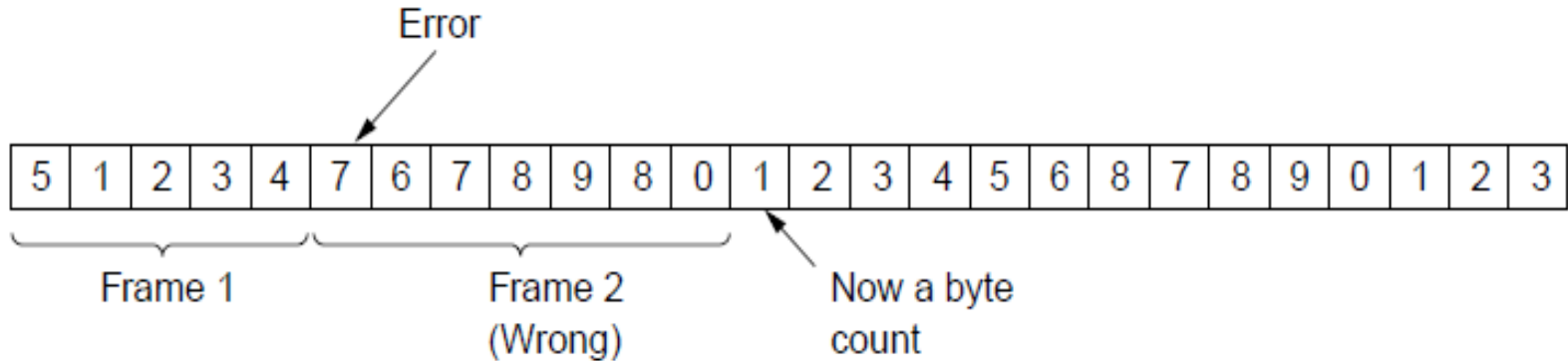
# Byte Count (2)



- How well do you think it works?

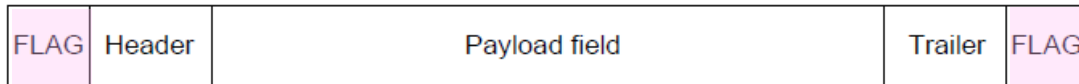
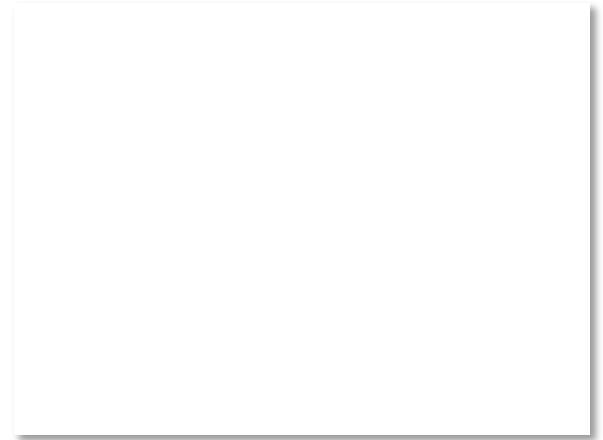
# Byte Count (3)

- Difficult to re-synchronize after framing error
  - Want a way to scan for a start of frame



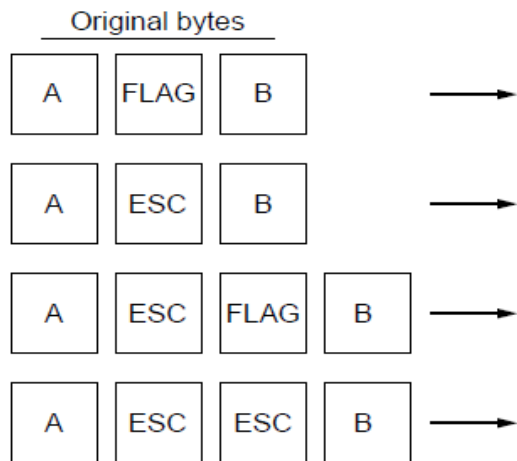
# Byte Stuffing

- Better idea:
  - Have a special flag byte value that means start/end of frame
  - Replace (“stuff”) the flag inside the frame with an escape code
  - Complication: have to escape the escape code too!



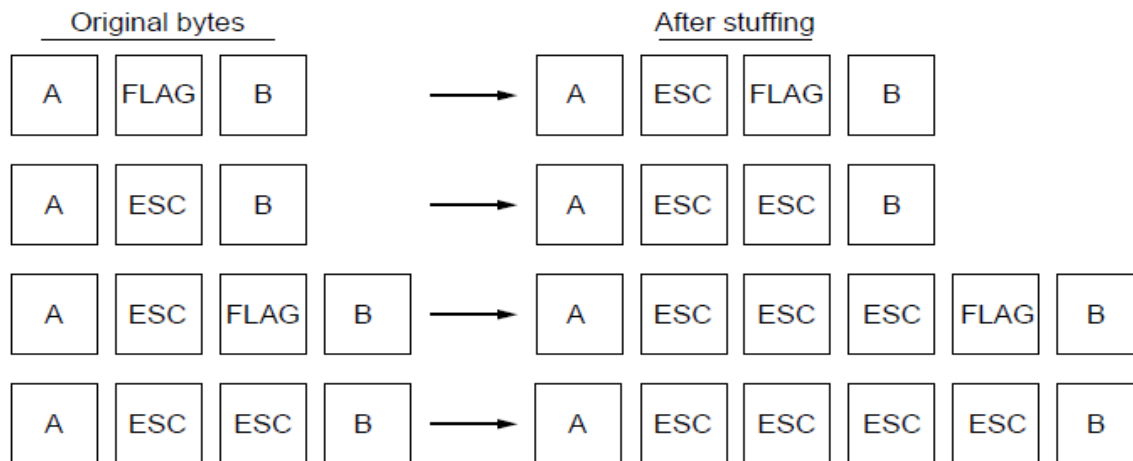
# Byte Stuffing (2)

- Rules:
  - Replace each FLAG in data with ESC FLAG
  - Replace each ESC in data with ESC ESC



# Byte Stuffing (3)

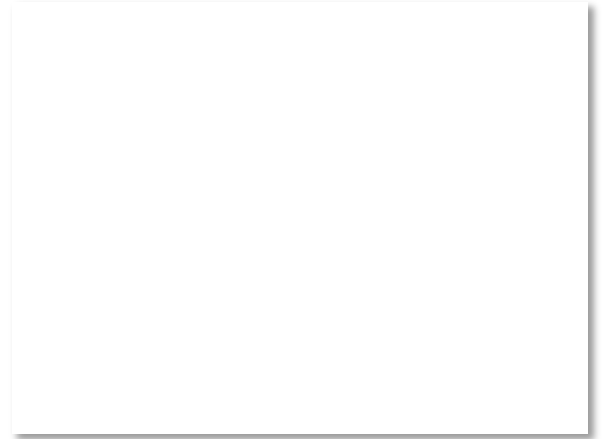
- Now any unescaped FLAG is the start/end of a frame





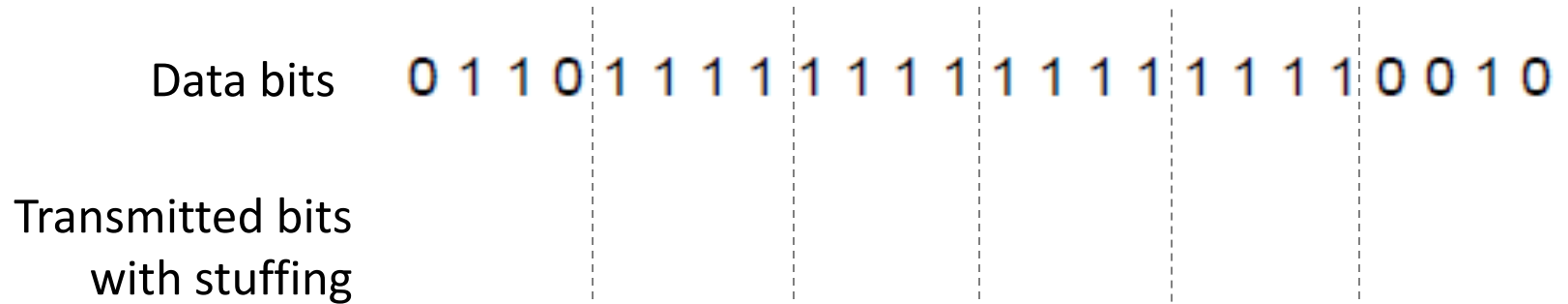
# Bit Stuffing

- Can stuff at the bit level too
  - Call a flag six consecutive 1s
  - On transmit, after five 1s in the data, insert a 0
  - On receive, a 0 after five 1s is deleted



# Bit Stuffing (2)

- Example:

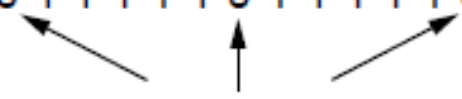


# Bit Stuffing (3)

- So how does it compare with byte stuffing?

Data bits    0 1 1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 0 0 1 0

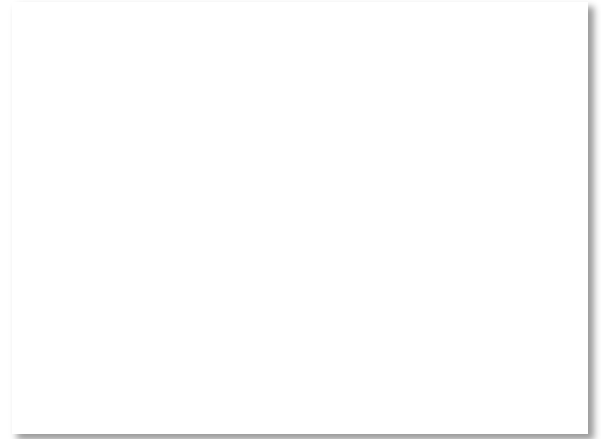
Transmitted bits  
with stuffing    0 1 1 0 1 1 1 1 1 0 1 1 1 1 1 0 1 1 1 1 1 0 1 0 0 1 0



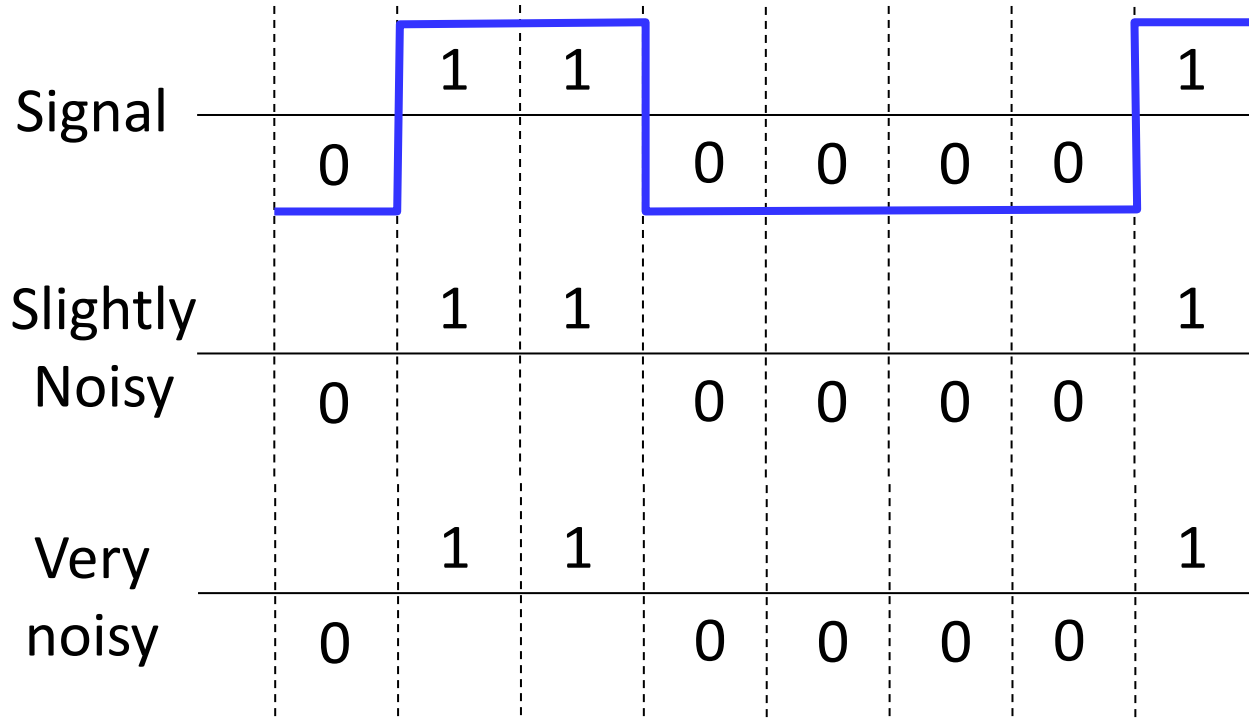
Stuffed bits

# Topic

- Some bits will be received in error due to noise. What can we do?
  - Detect errors with codes »
  - Correct errors with codes »
  - Retransmit lost frames ← Later
- Reliability is a concern that cuts across the layers – we'll see it again

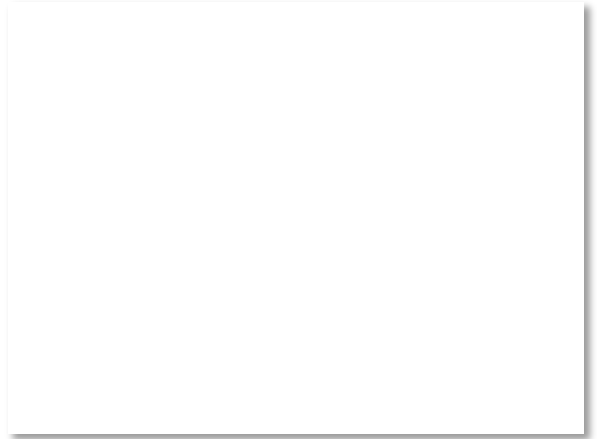


# Problem – Noise may flip received bits



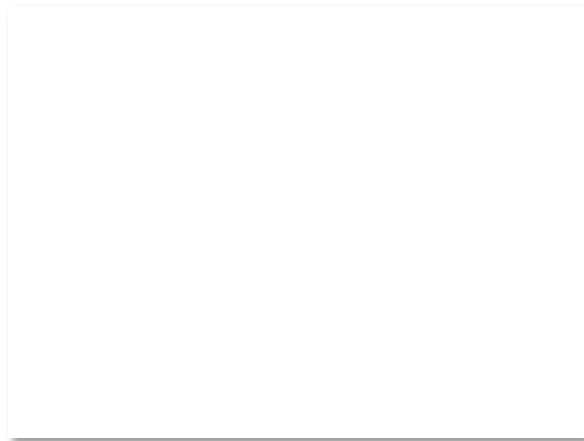
# Approach – Add Redundancy

- Error detection codes
  - Add check bits to the message bits to let some errors be detected
- Error correction codes
  - Add more check bits to let some errors be corrected
- Key issue is now to structure the code to detect many errors with few check bits and modest computation



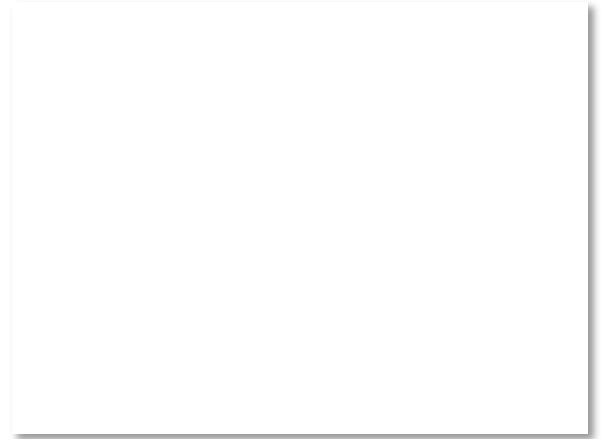
# Motivating Example

- A simple code to handle errors:
  - Send two copies! Error if different.
  
- How good is this code?
  - How many errors can it detect/correct?
  - How many errors will make it fail?



# Motivating Example (2)

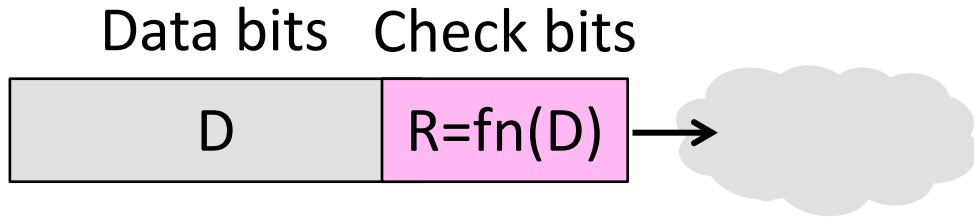
- We want to handle more errors with less overhead
  - Will look at better codes; they are applied mathematics
  - But, they can't handle all errors
  - And they focus on accidental errors (will look at secure hashes later)



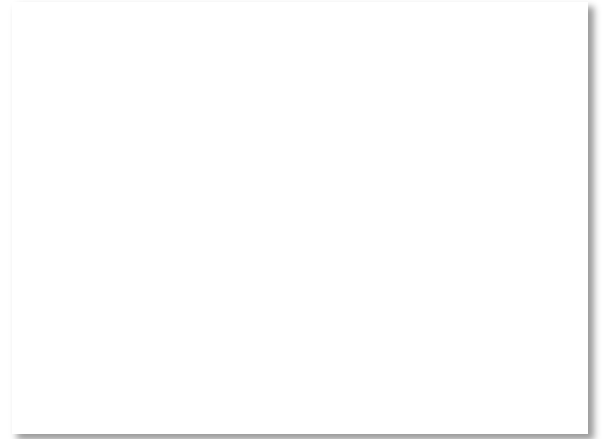


# Using Error Codes

- Codeword consists of  $D$  data plus  $R$  check bits (=systematic block code)

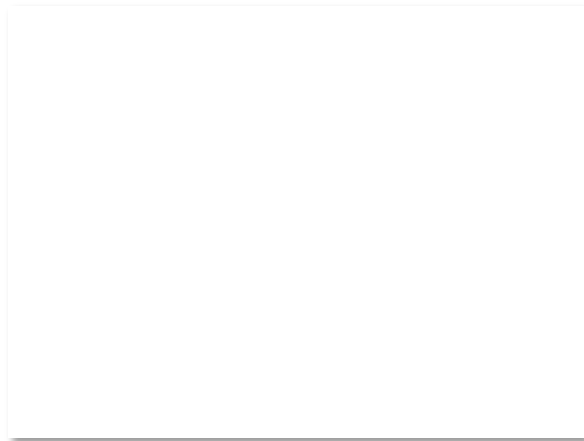
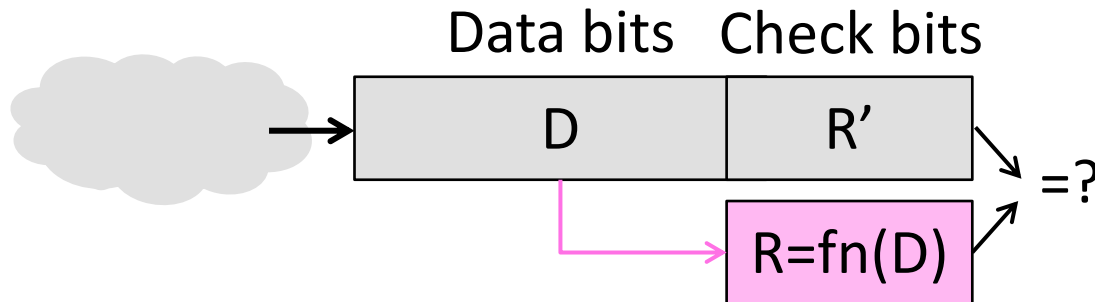


- Sender:
  - Compute  $R$  check bits based on the  $D$  data bits; send the codeword of  $D+R$  bits



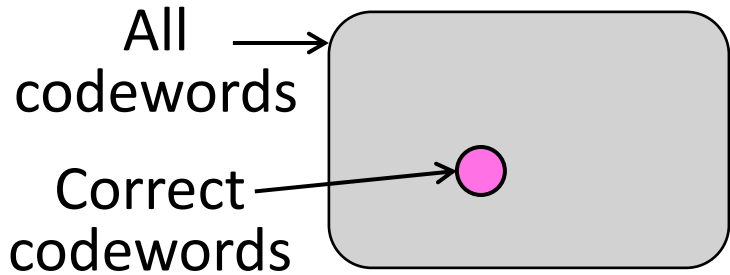
# Using Error Codes (2)

- Receiver:
  - Receive  $D+R$  bits with unknown errors
  - Recompute  $R$  check bits based on the  $D$  data bits; error if  $R$  doesn't match  $R'$



# Intuition for Error Codes

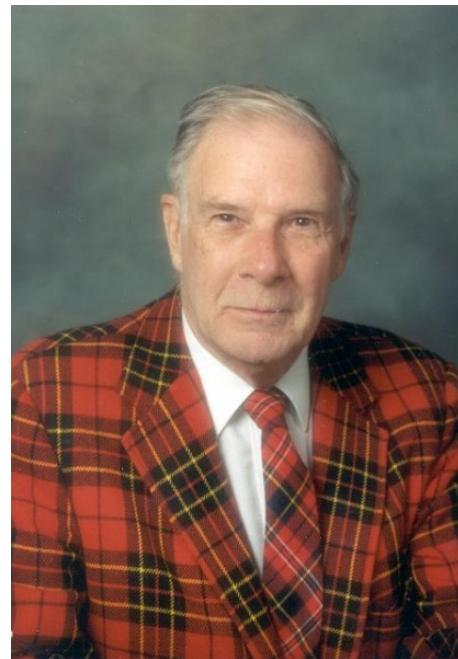
- For  $D$  data bits,  $R$  check bits:



- Randomly chosen codeword is unlikely to be correct; overhead is low

# R.W. Hamming (1915-1998)

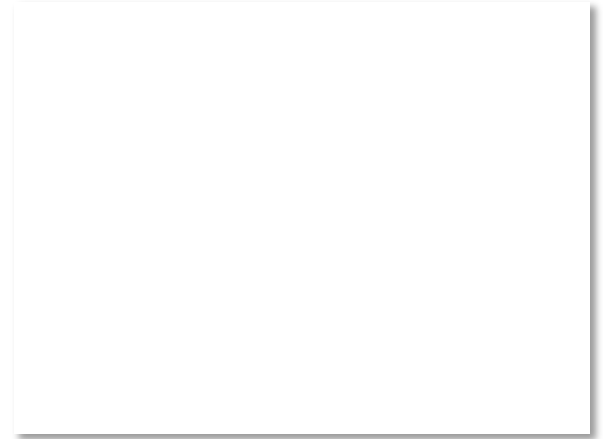
- Much early work on codes:
  - “Error Detecting and Error Correcting Codes”, BSTJ, 1950
- See also:
  - “You and Your Research”, 1986



Source: IEEE GHN, © 2009 IEEE

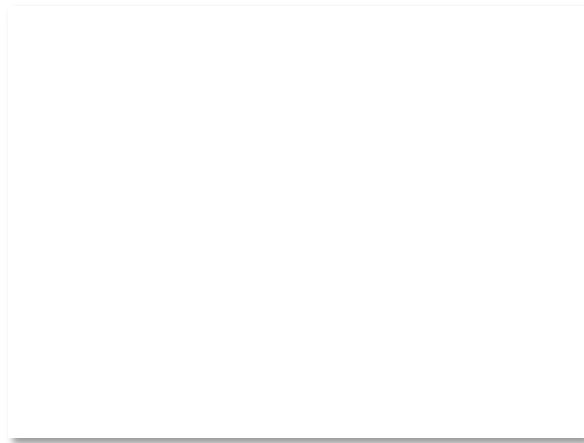
# Hamming Distance

- Distance is the number of bit flips needed to change  $D_1$  to  $D_2$
- Hamming distance of a code is the minimum distance between any pair of codewords



# Hamming Distance (2)

- Error detection:
  - For a code of distance  $d+1$ , up to  $d$  errors will always be detected



# Hamming Distance (3)

- Error correction:
  - For a code of distance  $2d+1$ , up to  $d$  errors can always be corrected by mapping to the closest codeword

