Reading

Jain, Kasturi, Schunck, *Machine Vision*. McGraw-Hill, 1995. Sections 4.2-4.4, 4.5(intro), 4.5.5, 4.5.6, 5.1-5.4.

3. Image processing

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Image processing

An **image processing** operation typically defines a new image g in terms of an existing image f.

The simplest operations are those that transform each pixel in isolation. These pixel-to-pixel operations can be written:

$$g(x,y) = t(f(x,y))$$

Examples: threshold, RGB → grayscale

Note: a typical choice for mapping to grayscale is to apply the YIQ television matrix and keep the Y.

$$\begin{bmatrix} Y \\ I \\ Q \end{bmatrix} = \begin{bmatrix} 0.299 & 0.587 & 0.114 \\ 0.596 & -0.275 & -0.321 \\ 0.212 & -0.523 & 0.311 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

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Pixel movement

Some operations preserve intensities, but move pixels around in the image

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$$g(x, y) = f(\tilde{x}(x, y), \tilde{y}(x, y))$$

Examples: many amusing warps of images

[Show image sequence.]

Noise

Image processing is also useful for noise reduction and edge enhancement. We will focus on these applications for the remainder of the lecture...





Original

Salt and pepper noise





Impulse noise

Gaussian noise

Common types of noise:

- Salt and pepper noise: contains random occurrences of black and white pixels
- Impulse noise: contains random occurrences of white pixels
- Gaussian noise: variations in intensity drawn from a Gaussian normal distribution

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Ideal noise reduction



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Ideal noise reduction



Practical noise reduction

How can we "smooth" away noise in a single image?

Is there a more abstract way to represent this sort of operation? Of course there is!

Discrete convolution

For a digital signal, we define **discrete convolution** as:

$$g[i] = f[i] * h[i]$$

$$= \sum_{i'} f[i']h[i - i']$$

$$= \sum_{i'} f[i']\tilde{h}[i' - i]$$

where $\tilde{h}[i] = h[-i]$.

Discrete convolution in 2D

Similarly, discrete convolution in 2D becomes:

$$g[i,j] = f[i,j] * h[i,j]$$

$$= \sum_{j'} \sum_{i'} f[i',j'] h[i-i',j-j']$$

$$= \sum_{j'} \sum_{i'} f[i',j'] \tilde{h}[i'-i,j'-j]$$

where $\tilde{h}[i,j] = h[-i,-j]$.

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Convolution representation

Since f and h are defined over finite regions, we can write them out in two-dimensional arrays:

62	79	23	119	120	105	4	0
10	10	9	62	12	78	34	0
10	58	197	46	46	0	0	48
176	135	5	188	191	68	0	49
2	1	1	29	26	37	0	77
0	89	144	147	187	102	62	208
255	252	0	166	123	62	0	31
166	63	127	17	1	0	99	30

X .2	X 0	X .2
X 0	X .2	X 0
X .2	X 0	X .2

Note: This is not matrix multiplication!

Q: What happens at the edges?

Mean filters

How can we represent our noise-reducing averaging filter as a convolution diagram (know as a **mean filter**)?

Effect of mean filters



Gaussian



Salt and pepper









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Gaussian filters

Gaussian filters weigh pixels based on their distance from the center of the convolution filter. In particular:

$$h[i,j] = \frac{e^{-(i^2+j^2)/(2\sigma^2)}}{C}$$

This does a decent job of blurring noise while preserving features of the image.

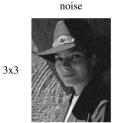
What parameter controls the width of the Gaussian?

What happens to the image as the Gaussian filter kernel gets wider?

What is the constant C? What should we set it to?

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Effect of Gaussian filters



Gaussian













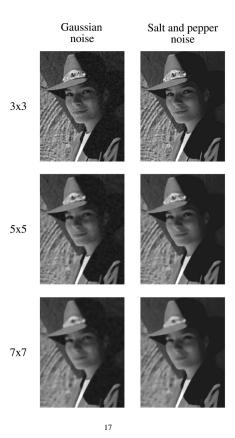
Median filters

A **median filter** operates over an $m \times m$ region by selecting the median intensity in the region.

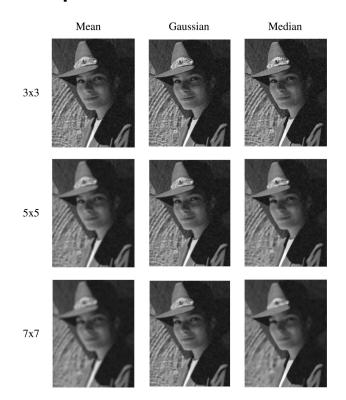
What advantage does a median filter have over a mean filter?

Is a median filter a kind of convolution?

Effect of median filters

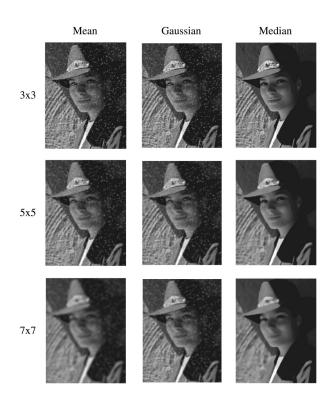


Comparison: Gaussian noise



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Comparison: salt and pepper noise



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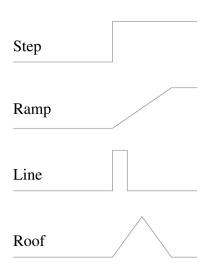
Edge detection

One of the most important uses of image processing is **edge detection:**

- Really easy for humans
- Really difficult for computers
- Fundamental in computer vision
- Important in many graphics applications

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What is an edge?



Q: How might you detect an edge in 1D?

Gradients

The **gradient** is the 2D equivalent of the derivative:

$$\nabla f(x,y) = \left(\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}\right)$$

Properties of the gradient

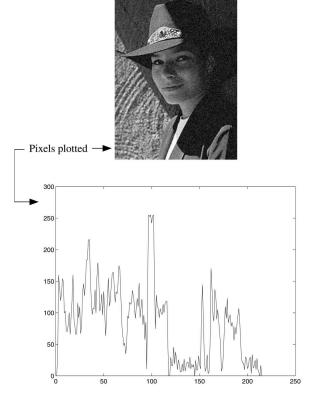
- It's a vector
- Points in the direction of maximum increase of *f*
- Magnitude is rate of increase

How can we approximate the gradient in a discrete image?

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Less than ideal edges



Steps in edge detection

Edge detection algorithms typically proceed in three or four steps:

- **Filtering**: cut down on noise
- **Enhancement**: amplify the difference between edges and non-edges
- **Detection**: use a threshold operation
- Localization (optional): estimate geometry of edges beyond pixels

Edge enhancement

A popular gradient magnitude computation is the **Sobel operator**:

$$s_x = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$

$$s_y = \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

We can then compute the magnitude of the vector (s_x, s_y) .

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Results of Sobel edge detection





Original

Smoothed





Sx + 128

Sy + 128





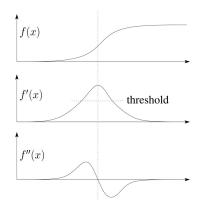


Magnitude

Threshold = 64

Threshold = 128

Second derivative operators



The Sobel operator can produce thick edges. Ideally, we're looking for infinitely thin boundaries.

An alternative approach is to look for local extrema in the first derivative: places where the change in the gradient is highest.

Q: A peak in the first derivative corresponds to what in the second derivative?

Q: How might we write this as a convolution filter?

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Localization with the Laplacian

An equivalent measure of the second derivative in 2D is the **Laplacian**:

$$\nabla^2 f(x, y) = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$$

Using the same arguments we used to compute the gradient filters, we can derive a Laplacian filter to be:

$$\Delta^2 = \begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

Zero crossings of this filter correspond to positions of maximum gradient. These zero crossings can be used to localize edges.

Localization with the Laplacian



Original



Smoothed

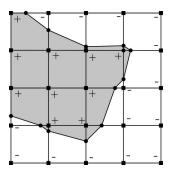


Laplacian (+128)

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Marching squares

We can convert these signed values into edge contours using a "marching squares" technique:



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Sharpening with the Laplacian



Original



Laplacian (+128)



Original + Laplacian



Original - Laplacian

Why does the sign make a difference?

How can you write each filter that makes each bottom image?

Spectral impact of sharpening

We can look at the impact of sharpening on the Fourier spectrum:

Spatial domain

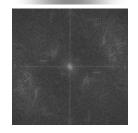




Frequency domain







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Summary

What you should take away from this lecture:

- The meanings of all the boldfaced terms.
- How noise reduction is done
- How discrete convolution filtering works
- The effect of mean, Gaussian, and median filters
- What an image gradient is and how it can be computed
- How edge detection is done
- What the Laplacian image is and how it is used in either edge detection or image sharpening