

Digital Representation of Information



Digital encoding of information means the data is stored in discrete units -- effectively numbers. Text is represented using one byte for each of the keyboard characters



Phone Numbers, SSNs, ISBNs, ...

- ❖ Dictionary says “digitize” means represent something using the ten decimal digits ... its more general
- ❖ Why use digits for phone numbers?
 - + Numerical properties unimportant
 - + Must only specify the sequence for pressing buttons
 - + Digits are familiar, have short names
- ❖ Adopt any symbols and relabel the buttons

1	2	3
4	5	6
7	8	9
0		

Standard

!	@	#
\$	%	^
&	*	(
)		

Shift

▶	▼	◀
▶▶	■	◀◀
▶▶▶	▲	◀◀◀

Player

800 325 3535

*)) # @ % # % # %

▲ || || ◀ ▼ ■ ◀ ■ ◀ ■

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Patterns to Symbols

- ❖ A die's patterns can make symbols
 - ❑ Use pattern once: 6 symbols
 - ❑ Use pattern in pairs: $6 \times 6 = 36$ symbols
 - ❑ Use pattern in triples: $6 \times 6 \times 6 = 216$
 - ❑ In general, using m patterns in sequences of n : m^n
- ❖ Fundamental pattern (*PandA*): The presence or absence of a phenomenon at a specific place/time
 - ❑ It's there or not -- Light: on/off, Water: flow/still,
 Magnetism: charged/neutral, Checkbox marked/empty,
 Door: closed/open, ...
 - ❑ The states must be discrete -- distinguishable, unambiguous
 - ❑ The two states represent one *bit* of information

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Representing Information

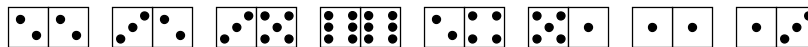
- ❖ Keyboard characters can be represented exactly
- ❖ Imagine you and your friend are prohibited from talking -- its too noisy? -- and so you use dice to encode the letters and punctuation to communicate

	•	••	•••	••••	•••••	••••••
•	A	G	M	S	Y	!
••	B	H	N	T	Z	-
•••	C	I	O	U	,	@
••••	D	J	P	V	.	(
•••••	E	K	Q	W	")
••••••	F	L	R	X	?	⌘

With two dice encode the 26 Latin letters and punctuation (spell numbers). So,

is UW

Order matters: row then col!



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Bits and Bytes

- ❖ It's customary to name the two possible patterns of a bit 1 and 0, though any names would be OK
- ❖ Sequences of 8 bits create a *byte*
- ❖ Two patterns in sequences of 8 ...
 $m = 2, n = 8, 2^8 = 256$ possibilities
 from 0000 0000 through 1111 1111
- ❖ The two pattern alternatives motivate the term *binary* for this representation

Names for Patterns	
Present	Absent
On	Off
Yes	No
1	0
True	False
+	-
Black	White
For	Against
Yin	Yang
Lisa	Bart
...	...

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Character Representations

- ❖ Keyboard characters are encoded into a byte or two
- ❖ ASCII is one of many byte encodings of characters

ASCII	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	
	0	0	0	0	1	1	1	1	0	0	0	0	1	1	1	1
	0	0	1	1	0	0	1	1	0	0	1	1	0	0	1	1
	0	1	0	1	0	1	0	1	0	1	0	1	0	1	0	1
0000	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%
0001	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%
0010		"	#	\$	%	&	'	()	*	+	,	-	.	/	
0011	0	1	2	3	4	5	6	7	8	9	:	;	<	=	>	?
0100	@	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
0101	P	Q	R	S	T	U	V	W	X	Y	Z	[\]	^	_
0110	`	a	b	c	d	e	f	g	h	i	j	k	l	m	n	o
0111	p	q	r	s	t	u	v	w	x	y	z	{		}	~	%
1000	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%
1001	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%	%
1010	%		¢	£	¤	¥	¦	§	-	©	®	«	-	»	™	-
1011	°	±	²	³	´	µ	¶	·	,	¸	»	¼	½	¾	¿	
1100	À	Á	Â	Ã	Ä	Å	Æ	Ç	È	É	Ê	Ë	Ì	Í	Î	Ï
1101	Ð	Ñ	Ò	Ó	Ô	Õ	×	Ø	Ù	Ú	Û	Ü	Ý	Þ	ß	
1110	à	á	â	ã	ä	å	æ	ç	è	é	ê	ë	ì	í	î	ï
1111	ð	ñ	ò	ó	ô	õ	÷	ø	ù	ú	û	ü	ý	þ	ÿ	

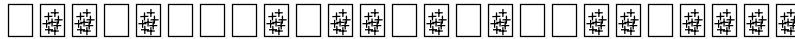
ASCII, pronounced AS-key, stands for American Standard Code for Information Interchange

A is represented 0100 0001
 B is represented 0100 0010
 C is represented 0100 0011
 ...

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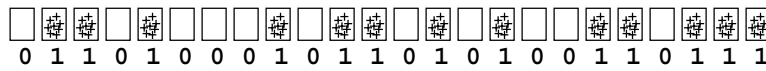
Storing Text

- ❖ Information is often stored by charge or magnetic field



Schematic diagram of magnetic spots, say on a disk

- ❖ Its presence or absence can be detected, leading to a natural association with 1 and 0 to charged/neutral states (alternatively, plus-charged / not plus charged)



Byte 0

Byte 1

Byte 2

- ❖ Text is stored as a sequence of keyboard characters

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Embellishing Text

- ❖ Often, text is to have specific properties, e.g be printed in a specific font, be italic, etc.
- ❖ To distinguish the text from the modifiers that describe its properties, tag the modifiers
 - + A tag is a text string, `<tag>` or `</tag>`, that modifies text
 - + Pairs of tags surround the tagged text, e.g. `<title>Gone with the Wind</title>`
 - + The “opening” and “closing” tags differ in that the close is indicated by a slash
 - + Not all tags have a “match”
- ❖ Software *interprets* the tags when the text is being processed, e.g. printed or displayed as a web page

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Numbers

- ❖ In addition to text computers must store numbers
- ❖ Numbers are sometimes stored as text characters:

0100 0110 0100 1001 0101 0100 0011 0001 0011 0000 0011 0000
 _ F _ _ I _ _ T _ _ 1 _ _ 0 _ _ 0

- ❖ Mostly numbers are stored directly using *binary notation*, since it has only two digits, 0 and 1
- ❖ Binary numbers and arithmetic are very much like decimal, except restricted to the two digits 0 and 1 ... what number is 1100100?

0
1
10
11
100
101
110
111
1000

Binary is counting on your fists instead of your fingers

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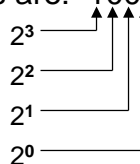
Decimal and Binary

❖	Decimal	Binary
Symbols:	0, 1, ..., 9	0, 1
Base	10	2
Number xyz	$x \cdot 10^2 + y \cdot 10^1 + z \cdot 10^0$	$x \cdot 2^2 + y \cdot 2^1 + z \cdot 2^0$
Ex: 101	$1 \cdot 10^2 + 0 \cdot 10^1 + 1 \cdot 10^0$	$1 \cdot 2^2 + 0 \cdot 2^1 + 1 \cdot 2^0$
Place Value	101	5
Powers	1, 10, 100, 1000, ...	1, 2, 4, 8, 16, 32, 64, ...

Binary works just like decimal, except that the base is 2

- ❖ What binary numbers are: 1000_2 , 1010_2 and 1111_2

Use a subscript to indicate the number base, e.g. $5_{10} = 101_2$



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Adding Is Familiar

- ❖ To add in binary use the same technique (algorithm), as decimal but restrict yourself to 0 and 1 ... everything else works the same way

$$\begin{array}{r}
 \begin{array}{ccccccc}
 & 1 & & 1 & & & \\
 & 1 & 1 & 0 & 0 & 1 & 1_2 \\
 \hline
 & 1 & 1 & 1 & 0 & 1 & 0_2 \\
 \hline
 1 & 1 & 0 & 1 & 1 & 0 & 1_2
 \end{array}
 & \begin{array}{r}
 1 \leftarrow \text{Carries} \\
 51 \\
 \hline
 58 \\
 \hline
 109
 \end{array}
 \end{array}$$

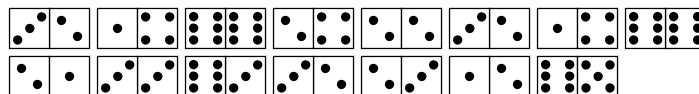
- ❖ Binary is pretty tedious for humans because there are so many digits ... circuitry benefits however because it uses the two states (on/off) efficiently

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Summary

- ❖ Patterns are used to create symbols, symbols are used to represent information
- ❖ The binary digits (bits) 0 and 1 are a natural way to interpret the presence or absence of a phenomenon
- ❖ Bytes are composed of 8 bits, ASCII represents text as one character per byte
- ❖ Binary numbers and arithmetic are like decimal except they are limited to the two numerals 0 and 1
- ❖ Tags are used to insert modifiers into text and keep it separated from the text



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