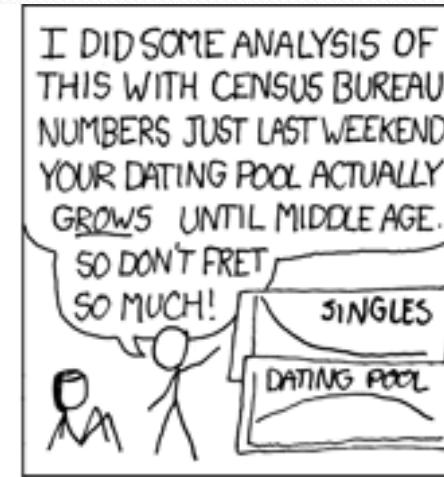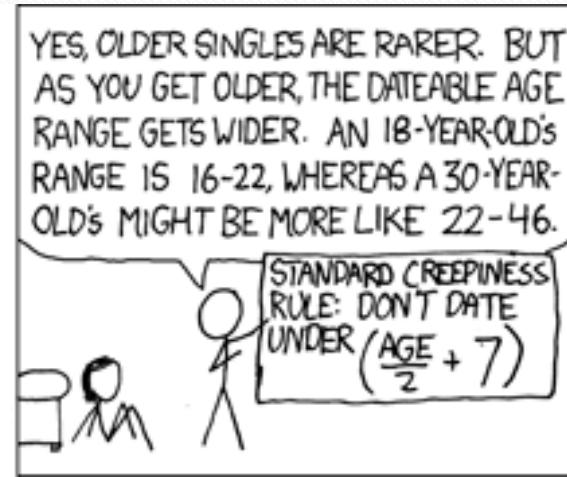# Building Java Programs

Chapter 3
Return values, `Math`, and `double`

reading: 3.2, 2.1 - 2.2

Java's `Math` class

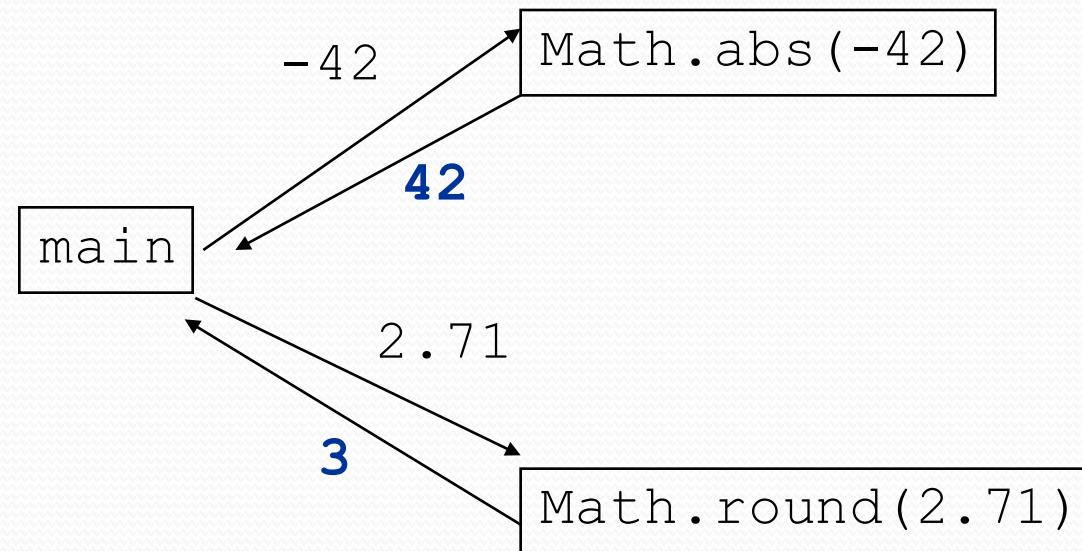| Method name	Description
`Math.abs(`*value*`)`	absolute value
`Math.ceil(`*value*`)`	rounds up
`Math.floor(`*value*`)`	rounds down
`Math.log10(`*value*`)`	logarithm, base 10
`Math.max(`*value1*`, `*value2*`)`	larger of two values
`Math.min(`*value1*`, `*value2*`)`	smaller of two values
`Math.pow(`*base*`, `*exp*`)`	*base* to the *exp* power
`Math.random()`	random `double` between 0 and 1
`Math.round(`*value*`)`	nearest whole number
`Math.sqrt(`*value*`)`	square root
`Math.sin(`*value*`)` `Math.cos(`*value*`)` `Math.tan(`*value*`)`	sine/cosine/tangent of an angle in radians
`Math.toDegrees(`*value*`)` `Math.toRadians(`*value*`)`	convert degrees to radians and back

Constant	Description
`Math.E`	2.7182818…
`Math.PI`	3.1415926…

No output?

- Simply calling these methods produces no visible result.
  - `Math.pow(3, 4);`   `// no output`

- Math method calls use a Java feature called *return values* that cause them to be treated as expressions.

- The program runs the method, computes the answer, and then "replaces" the call with its computed result value.
  - ~~`Math.pow(3, 4);`~~   `// no output`
    `81.0;`   `// no output`

- To see the result, we must print it or store it in a variable.
  - `double result = Math.pow(3, 4);`
  - `System.out.println(result);`   `// 81.0`

Return

- **return**: To send out a value as the result of a method.
  - Return values send information *out* from a method to its caller.
    - A call to the method can be used as part of an expression.
  - (Compare to parameters which send values *into* a method)

```
             -42      Math.abs(-42)

                    42
      main

                    2.71
        3
                     Math.round(2.71)
```

Math questions

- Evaluate the following expressions:
  - `Math.abs(-1.23)`
  - `Math.pow(3, 2)`
  - `Math.pow(10, -2)`
  - `Math.sqrt(121.0) - Math.sqrt(256.0)`
  - `Math.round(Math.PI) + Math.round(Math.E)`
  - `Math.ceil(6.022) + Math.floor(15.9994)`
  - `Math.abs(Math.min(-3, -5))`

- `Math.max` and `Math.min` can be used to bound numbers. Consider an `int` variable named `age`.
  - What statement would replace negative ages with 0?
  - What statement would cap the maximum age to 40?

Why return and not print?

- It might seem more useful for the `Math` methods to print their results rather than returning them. Why don't they?

- Answer: Returning is more flexible than printing.
  - We can compute several things before printing:
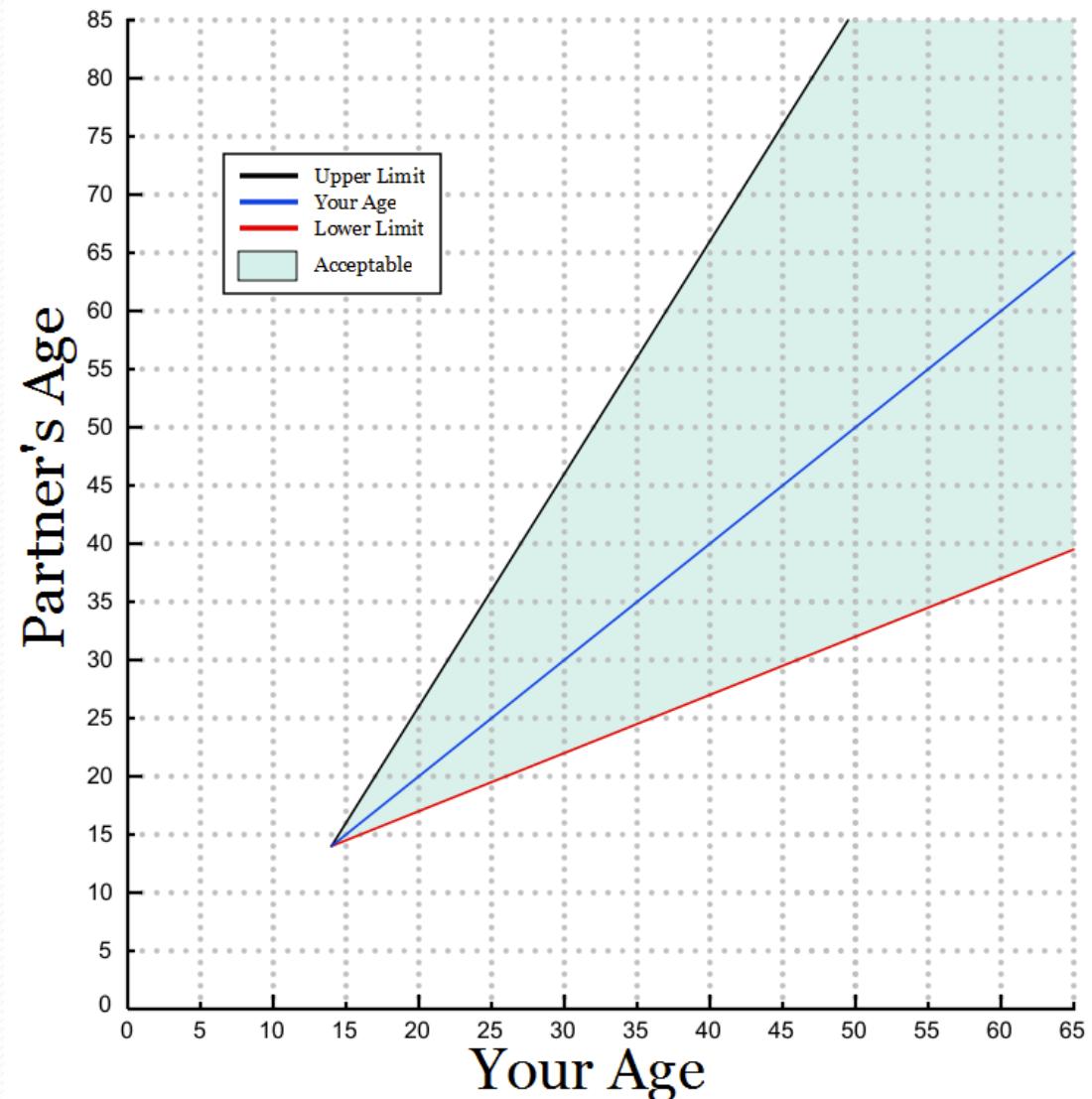   ```
    double pow1 = Math.pow(3, 4);
    double pow2 = Math.pow(10, 6);
    System.out.println("Powers are " + pow1 + " and " + pow2);
    ```

  - We can combine the results of many computations:
    ```
    double k = 13 * Math.pow(3, 4) + 5 - Math.sqrt(17.8);
    ```

# Write a method that, given an age, returns the minimum appropriate age to date

Minimum dating age = age / 2 + 7

# Returning a value

```
public static type name(parameters) {
    statements;

    ...

    return expression;

}
```

- When Java reaches a return statement:
  - it evaluates the expression
  - it substitutes the return value in place of the call
  - it goes back to the caller and continues after the method call

Return examples

```
// Calculates the minimum acceptable dating age.
public static int minimumDatingAge(int age) {
    int minimumAge = age / 2 + 7;
    return minimumAge;
}
```

- You can shorten the examples by returning an expression:

```
public static int minimumDatingAge(int age) {
    return age / 2 + 7;
}
```

More Return examples

```java
// Converts degrees Fahrenheit to Celsius.
public static double fToC(double degreesF) {
    double degreesC = 5.0 / 9.0 * (degreesF - 32);
    return degreesC;
}

// Computes triangle hypotenuse length given its side lengths.
public static double hypotenuse(int a, int b) {
    double c = Math.sqrt(a * a + b * b);
    return c;
}
```

- You can shorten the examples by returning an expression:

```java
public static double fToC(double degreesF) {
    return 5.0 / 9.0 * (degreesF - 32);
}
```

Common error: Not storing

- Many students incorrectly think that a `return` statement sends a variable's name back to the calling method.

```java
public static void main(String[] args) {
    slope(0, 0, 6, 3);
    System.out.println("The slope is " + result);   // ERROR:
}                                 // cannot find symbol: result

public static double slope(int x1, int x2, int y1, int y2) {
    double dy = y2 - y1;
    double dx = x2 - x1;
    double result = dy / dx;
    return result;
}
```

Fixing the common error

- Returning sends the variable's *value* back. Store the returned value into a variable or use it in an expression.

```java
public static void main(String[] args) {
    double s = slope(0, 0, 6, 3);
    System.out.println("The slope is " + s);
}

public static double slope(int x1, int x2, int y1, int y2) {
    double dy = y2 - y1;
    double dx = x2 - x1;
    double result = dy / dx;
    return result;
}
```

Quirks of real numbers

- Some `Math` methods return `double` or other non-`int` types.

  ```
  int x = Math.pow(10, 3);    // ERROR: incompat. types
  ```

- Some `double` values print poorly (too many digits).

  ```
  double result = 1.0 / 3.0;
  System.out.println(result);    // 0.3333333333333
  ```

- The computer represents `double`s in an imprecise way.

  ```
  System.out.println(0.1 + 0.2);
  ```

  - Instead of 0.3, the output is `0.30000000000000004`

Type casting

- **type cast**: A conversion from one type to another.
  - To promote an `int` into a `double` to get exact division from `/`
  - To truncate a `double` from a real number to an integer

- Syntax:

  (**type**) **expression**

  ```
  Examples:
  double result = (double) 19 / 5;      // 3.8
  int result2 = (int) result;           // 3
  int x = (int) Math.pow(10, 3);        // 1000
  ```

More about type casting

- Type casting has high precedence and only casts the item immediately next to it.

  - `double x = (double) 1 + 1 / 2;      // 1.0`
  - `double y = 1 + (double) 1 / 2;      // 1.5`

- You can use parentheses to force evaluation order.

  - `double average = (double) (a + b + c) / 3;`

- A conversion to `double` can be achieved in other ways.

  - `double average = 1.0 * (a + b + c) / 3;`

Exercise

- In physics, the *displacement* of a moving body represents its change in position over time while accelerating.
  - Given initial velocity v_0 in m/s, acceleration a in m/s^2, and elapsed time t in s, the displacement of the body is:

  - Displacement = $v_0\, t + \frac{1}{2}\, a\, t^2$

- Write a method `displacement` that accepts v_0, a, and t and computes and returns the change in position.
  - example: `displacement(3.0, 4.0, 5.0)` returns `65.0`

Exercise solution

```java
public static double displacement(double v0, double a, double t) {
    double d = v0 * t + 0.5 * a * Math.pow(t, 2);
    return d;
}
```

Exercise

- If you drop two balls, which will hit the ground first?
  - Ball 1: height of 600m, initial velocity = 25 m/sec downward
  - Ball 2: height of 500m, initial velocity = 15 m/sec downward

- Write a program that determines how long each ball takes to hit the ground (and draws each ball falling).

- Total time is based on the force of gravity on each ball.
  - Acceleration due to gravity $\cong$ 9.81 m/s^2, downward
  - Displacement = $v_0 t + \frac{1}{2} a t^2$

Ball solution

```java
// Simulates the dropping of two balls from various heights.
import java.awt.*;

public class Balls {
    public static void main(String[] args) {
        DrawingPanel panel = new DrawingPanel(600, 600);
        Graphics g = panel.getGraphics();

        int ball1x = 100,  ball1y =   0,  v01 = 25;
        int ball2x = 200,  ball2y = 100,  v02 = 15;

        // draw the balls at each time increment
        for (double t = 0; t <= 10.0; t = t + 0.1) {
            double disp1 = displacement(v01, t, 9.81);
            g.fillOval(ball1x, ball1y + (int) disp1, 10, 10);
            double disp2 = displacement(v02, t, 9.81);
            g.fillOval(ball2x, ball2y + (int) disp2, 10, 10);

            panel.sleep(50);    // pause for 50 ms
            panel.clear();
        }
    }
    ...
```