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| CSE 143 |  |
| Trees |  |
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| Overview |  |
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| - Topics <br> - Trees: Definitions and terminology <br> - Binary trees <br> - Tree traversals |  |
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## Trees

- Most of the structures we've looked at so far are linear


## Looking Ahead To An Old Goal

- Finding algorithms and data structures for fast searching - A key goal
- Arrays
- Linked lists
- There are many examples of structures that are not linear, e.g. hierarchical structures
- Sorted arrays are faster than unsorted arrays, for searching

Can use binary search algorithm
Not so easy to keep the array in orde

- LinkedLists were faster than arrays (or ArrayLists), for insertion and removal operations
The extra flexibility of the "next" pointers avoided the cost of sliding
But... LinkedLists are hard to search, even if sorted
- Book contents (chapters, sections, paragraphs)
- Class inheritance diagrams
- Trees can be used to represent hierarchical structures
- Is there an analogue of LinkedLists for sorted collections??
- The answer will be...Yes: a particular type of tree!


## Tree Definitions

- A tree is a collection of nodes connected by edges


## - A node contains

- Data (e.g. an Object)
- References (edges) to two or more subtrees or children
- Trees are hierarchical
- A node is said to be the parent of its children (subtrees)
- There is a single unique root node that has no parent
- Nodes with no children are called leaf nodes
- A tree with no nodes is said to be empty



## Subtrees

- A subtree in a tree is any node in the tree together with all of its descendants (its children, and their children, recursively)



## Binary Trees

- A binary tree is a tree each of whose nodes has no more than two children
- The two children are called the left child and right child
- The subtrees belonging to those children are called the left subtree and the right subtree


| Binary Tree Nodes |
| :---: |
| - A node for a binary tree holds the item and references to its subtrees <br> class BTNode \{ <br> public Object item; // data item in this node <br> public BTNode left; // left subtree, or null if none <br> public BTNode right; $/ /$ right subtree, or null if none <br> public BTNode(Object item, BTNode left, BTNode right) $\{\ldots\}$ <br> \} |
|  |

## Binary Tree Implementation

- The whole tree can be represented just by a pointer to the root node, or null if the tree is empty
public class BinTree \{ private BTNode root;
// root of tree, or null if empty public BinTree( ) $\{$ root = null; \}
\}


## Tree Algorithms

- The definition of a tree is naturally recursive:
- A tree is either null (empty),
or data + left (sub-)tree + right (sub-)tree
- Base case(s)?
- Recursive case(s)?
- Given a recursively defined data structure, recursion is often a very natural technique for algorithms on that data structure
- Don’t fight it!

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## Tree Traversal

- Functions like subtreeSize systematically "visit" each node in a tree
- This is called a traversal
- We also used this word in connection with lists
- Traversal is a common pattern in many algorithms
- The processing done during the "visit" varies with the algorithm
- What order should nodes be visited in?
- Many are possible
- Three have been singled out as particularly useful for binary trees: preorder, postorder, and inorder

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## A Typical Tree Algorithm: size()

## public class BinTree \{

${ }^{\text {/** }}$ Return the number of items in this tree */
public int size() \{
return subtreeSize(root)
\}
// Return the number of nodes in the (sub-)tree with root $n$
private int subtreeSize(BTNode n)
if ( $n==$ null) $\{$
return
\}else \{ return $\qquad$ _;
\}
\}
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## Traversals

- Preorder traversal:
- "Visit" the (current) node first
i.e., do what ever processing is to be done
- Then, (recursively) do preorder traversal on its children, left to right
- Postorder traversal:
- First, (recursively) do postorder traversals of children, left to right
- Visit the node itself last
- Inorder traversal:
- (Recursively) do inorder traversal of left child
- Then visit the (current) node
- Then (recursively) do inorder traversal of right child Footnote: pre- and postorder make sense for all trees; inorder only for binary trees

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## Example of Tree Traversal

In what order are the nodes visited, if we start the process at the root?


Preorder:
Inorder:
Postorder:
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## New Algorithm: contains

## - Return whether or not a value is an item in the tree

 public class BinTree/** Return whether item is in tree */
public boolean contains(Object item) \{
return subtreeContains(root, item),
\} $/ /$ Retu
Return whether item is in (sub-)tree with root $r$
private boolean subtreeContains(BTNode r, Object item) $\{$
if $(r==$ nuli) $\{$
return
\}else if (r.item.equals(item)) \{
return
\} else \{ $\qquad$ ;
\}
\}
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## More Practice

What about this tree?

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| Test |  |
| :--- | :--- |
| contains(d) | (c) 2001-5, University of wastington |

## Cost of contains

- Work done at each node:
- Number of nodes visited:
- Total cost:
- Can we do better?

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