# CSE 143 Lecture 17 

## Binary Trees

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## Trees

- tree: A directed, acyclic structure of linked nodes.
- directed : Has one-way links between nodes.
- acyclic: No path wraps back around to the same node twice.
- A binary tree can be defined as either:
- empty (null), or
- a root node that contains:
- data,
- a left subtree, and
- a right subtree.
- (The left and/or right subtree could be empty.)



## Definition is recursive！

－The recursive definition lets us build any shape tree：


## Trees in computer science

－folders／files on a computer
－family genealogy；organizational charts
－AI：decision trees
－compilers：parse tree
$-\mathrm{a}=(\mathrm{b}+\mathrm{c}) *$ ；

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## Programming with trees

- Trees are a mixture of linked lists and recursion
- considered very elegant once understood
- difficult for novices to master
- Common student remark \#1:
- "My code doesn't work, and I don't know why."
- Common student remark \#2:
- "My code works, and I don't know why."


## Terminology

- root: topmost node of the tree
- leaf: node with no children



## Terminology

- child: Any node our node Looking at our 78 node: refers to


- sibling: another child of the parent of our node
- parent: the node that refers to our node
(82)
(16)
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## IntTreeNode Class

```
// An IntTreeNode object is one node in a binary tree of ints.
public class IntTreeNode {
    public int data; // data stored at this node
    public IntTreeNode left; // reference to left subtree
    public IntTreeNode right; // reference to right subtree
    // Constructs a leaf node with the given data.
    public IntTreeNode(int data) {
        this(data, null, null);
    }
    // Constructs a branch node with the given data and links.
    public IntTreeNode(int data, IntTreeNode left,
                        IntTreeNode right) {
        this.data = data;
        this.left = left;
        this.right = right;
    }
}
```


## IntTree class

// An IntTree object represents an entire binary tree of ints. public class IntTree \{ private IntTreeNode overallRoot; // null for an empty tree
<methods>
\}

- Client code talks to the Int Tree, not to the node objects inside it
- Methods of the IntTree create and manipulate the nodes, their data and links between them



## IntIree constructor

- Assume we have the following constructor:

```
public IntTree(int height)
```

that will create a tree and fill it with nodes with random data values from 1-100 until it is full at the given height.
IntTree tree $=$ new IntTree (3); overallRoot
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## Exercise

- Add a method print to the IntTree class that prints the elements of the tree, separated by spaces.
- A node's left subtree should be printed before it, and its right subtree should be printed after it.
- Example: tree.print();
$2941 \quad 6 \quad 1781940$



## Exercise solution

```
// An IntTree object represents an entire binary tree of ints.
public class IntTree {
    private IntTreeNode overallRoot; // null for an empty tree
    •••
    public void print() {
        print(overallRoot);
        System.out.println(); // end the line of output
    }
    private void print(IntTreeNode root) {
        // (base case is implicitly to do nothing on null)
        if (root != null) {
            // recursive case: print left, center, right
            print(root.left);
            System.out.print(root.data + " ");
            print(root.right);
        }
    }
}
```


## Template for tree methods

```
public class IntTree {
    private IntTreeNode overallRoot;
    ...
    public <type> <name>(<parameters>) {
        name(overallRoot, <parameters>);
    }
    private <type> <name>(IntTreeNode root, <parameters>) {
    }
}
```

- Tree methods are often implemented recursively
- with a public/private pair
- the private version accepts the root node to process


## Traversals

- traversal: An examination of the elements of a tree.
- But in what order? Root first? Left subtree first? ...
- Common orderings for traversals:
- pre-order: process root node, then its left/right subtrees
- in-order: process left subtree, then root node, then right
- post-order: process left/right subtrees, then root node



## Traversal example



- pre-order: 174129698140
- in-order: 294161781940
- post-order: 296418140917


## Sailboat Method

- To quickly generate a traversal:
- Trace a path around the tree.
- As you pass a node on the proper side, process it.
- pre-order: left side
- in-order: bottom
- post-order: right side

- pre-order: 174129698140
- in-order: 294161781940
- post-order: 296418140917


## Exercise

- Give pre-, in-, and post-order traversals for the following tree:



## Exercise

- Add a method named printSideways to the IntTree class that prints the tree in a sideways indented format, with right nodes above roots above left nodes, with each level 4 spaces more indented than the one above it.
- Example: Output from the tree below:



## Exercise solution

```
// Prints the tree in a sideways indented format.
public void printSideways() {
    printSideways(overallRoot, "");
}
private void printSideways(IntTreeNode root,
                                String indent) {
    if (root != null) {
        printSideways(root.right, indent + " ");
        System.out.println(indent + root.data);
        printSideways(root.left, indent + " ");
    }
}
```

