

CSE 143

Lecture 13

Recursive Programming

reading: 12.2 - 12.3

slides created by Marty Stepp

<http://www.cs.washington.edu/143/>

Exercise

- Write a recursive method `pow` accepts an integer base and exponent and returns the base raised to that exponent.
 - Example: `pow(3, 4)` returns 81
 - Solve the problem recursively and without using loops.

pow solution

```
// Returns base ^ exponent.  
// Precondition: exponent >= 0  
public static int pow(int base, int exponent) {  
    if (exponent == 0) {  
        // base case; any number to 0th power is 1  
        return 1;  
    } else {  
        // recursive case:  $x^y = x * x^{(y-1)}$   
        return base * pow(base, exponent - 1);  
    }  
}
```

An optimization

- Notice the following mathematical property:

$$\begin{aligned} 3^{12} &= 531441 &= 9^6 \\ & &= (3^2)^6 \\ & & &= (9^2)^3 \\ & & &= ((3^2)^2)^3 \end{aligned}$$

- When does this "trick" work?
- How can we incorporate this optimization into our `pow` method?
- What is the benefit of this trick if the method already works?

pow solution 2

```
// Returns base ^ exponent.  
// Precondition: exponent >= 0  
public static int pow(int base, int exponent) {  
    if (exponent == 0) {  
        // base case; any number to 0th power is 1  
        return 1;  
    } else if (exponent % 2 == 0) {  
        // recursive case 1:  $x^y = (x^2)^{(y/2)}$   
        return pow(base * base, exponent / 2);  
    } else {  
        // recursive case 2:  $x^y = x * x^{(y-1)}$   
        return base * pow(base, exponent - 1);  
    }  
}
```

Exercise

- Write a recursive method `printBinary` that accepts an integer and prints that number's representation in binary (base 2).
 - Example: `printBinary(7)` prints `111`
 - Example: `printBinary(12)` prints `1100`
 - Example: `printBinary(42)` prints `101010`

place	10	1
value	4	2

32	16	8	4	2	1
1	0	1	0	1	0

- Write the method recursively and without using any loops.

Case analysis

- Recursion is about solving a small piece of a large problem.
 - What is 69743 in binary?
 - Do we know *anything* about its representation in binary?
 - Case analysis:
 - What is/are easy numbers to print in binary?
 - Can we express a larger number in terms of a smaller number(s)?
 - Suppose we are examining some arbitrary integer N .
 - if N 's binary representation is **10010101011**
 - $(N / 2)$'s binary representation is **1001010101**
 - $(N \% 2)$'s binary representation is **1**

printBinary solution

```
// Prints the given integer's binary representation.  
// Precondition: n >= 0  
public static void printBinary(int n) {  
    if (n < 2) {  
        // base case; same as base 10  
        System.out.println(n);  
    } else {  
        // recursive case; break number apart  
        printBinary(n / 2);  
        printBinary(n % 2);  
    }  
}
```

– Can we eliminate the precondition and deal with negatives?

printBinary solution 2

```
// Prints the given integer's binary representation.
public static void printBinary(int n) {
    if (n < 0) {
        // recursive case for negative numbers
        System.out.print("-");
        printBinary(-n);
    } else if (n < 2) {
        // base case; same as base 10
        System.out.println(n);
    } else {
        // recursive case; break number apart
        printBinary(n / 2);
        printBinary(n % 2);
    }
}
```

Exercise

- Write a recursive method `isPalindrome` accepts a `String` and returns `true` if it reads the same forwards as backwards.
 - `isPalindrome("madam")` → `true`
 - `isPalindrome("racecar")` → `true`
 - `isPalindrome("step on no pets")` → `true`
 - `isPalindrome("able was I ere I saw elba")` → `true`
 - `isPalindrome("Java")` → `false`
 - `isPalindrome("rotater")` → `false`
 - `isPalindrome("byebye")` → `false`
 - `isPalindrome("notion")` → `false`

Exercise solution

```
// Returns true if the given string reads the same
// forwards as backwards.
// Trivially true for empty or 1-letter strings.
public static boolean isPalindrome(String s) {
    if (s.length() < 2) {
        return true;    // base case
    } else {
        char first = s.charAt(0);
        char last  = s.charAt(s.length() - 1);
        if (first != last) {
            return false;
        }
        // recursive case
        String middle = s.substring(1, s.length() - 1);
        return isPalindrome(middle);
    }
}
```

Exercise solution 2

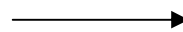
```
// Returns true if the given string reads the same
// forwards as backwards.
// Trivially true for empty or 1-letter strings.
public static boolean isPalindrome(String s) {
    if (s.length() < 2) {
        return true;    // base case
    } else {
        return s.charAt(0) == s.charAt(s.length() - 1)
            && isPalindrome(s.substring(1, s.length() - 1));
    }
}
```

Exercise

- Write a recursive method `reverseLines` that accepts a `file Scanner` and prints the lines of the file in reverse order.

– Example input file:

```
Roses are red,  
Violets are blue.  
All my base  
Are belong to you.
```



Expected console output:

```
Are belong to you.  
All my base  
Violets are blue.  
Roses are red,
```

- What are the cases to consider?
 - How can we solve a small part of the problem at a time?
 - What is a file that is very easy to reverse?

Reversal pseudocode

- Reversing the lines of a file:
 - Read a line L from the file.
 - Print the rest of the lines in reverse order.
 - Print the line L.

- If only we had a way to reverse the rest of the lines of the file....

Reversal solution

```
public static void reverseLines(Scanner input) {  
    if (input.hasNextLine()) {  
        // recursive case  
        String line = input.nextLine();  
        reverseLines(input);  
        System.out.println(line);  
    }  
}
```

- Where is the base case?

Tracing our algorithm

- **call stack:** The method invocations running at any one time.

```
reverseLines(new Scanner("poem.txt"));
```

```
public static void reverseLines(Scanner input) {  
    if (input.hasNextLine()) {  
        String line = input.nextLine(); // "Roses are red "  
public static void reverseLines(Scanner input) {  
    if (input.hasNextLine()) {  
        String line = input.nextLine(); // "Violets are blue "  
public static void reverseLines(Scanner input) {  
    if (input.hasNextLine()) {  
        String line = input.nextLine(); // "All my base"  
public static void reverseLines(Scanner input) {  
    if (input.hasNextLine()) {  
        String line = input.nextLine(); // "Are belong to you "  
public static void reverseLines(Scanner input) {  
    if (input.hasNextLine()) { // false  
        ...  
    }  
}
```

→ roses are red,
Violets are blue.
All my base
Are belong to you.

Are belong to you.
All my base
Violets are blue.
Roses are red,

Exercise

- Write a method `crawl` accepts a `File` parameter and prints information about that file.
 - If the `File` object represents a normal file, just print its name.
 - If the `File` object represents a directory, print its name and information about every file/directory inside it, indented.

```
cse143
  handouts
    syllabus.doc
    lecture_schedule.xls
  homework
    1-sortedintlist
      ArrayIntList.java
      SortedIntList.java
      index.html
      style.css
```

- **recursive data:** A directory can contain other directories.

File objects

- A `File` object (from the `java.io` package) represents a file or directory on the disk.

Constructor/method	Description
<code>File(String)</code>	creates <code>File</code> object representing file with given name
<code>canRead()</code>	returns whether file is able to be read
<code>delete()</code>	removes file from disk
<code>exists()</code>	whether this file exists on disk
<code>getName()</code>	returns file's name
<code>isDirectory()</code>	returns whether this object represents a directory
<code>length()</code>	returns number of bytes in file
<code>listFiles()</code>	returns a <code>File[]</code> representing files in this directory
<code>renameTo(File)</code>	changes name of file

Public/private pairs

- We cannot vary the indentation without an extra parameter:

```
public static void crawl(File f, String indent) {
```

- Often the parameters we need for our recursion do not match those the client will want to pass.

In these cases, we instead write a pair of methods:

- 1) a public, non-recursive one with the parameters the client wants
- 2) a private, recursive one with the parameters we really need

Exercise solution 2

```
// Prints information about this file,  
// and (if it is a directory) any files inside it.  
public static void crawl(File f) {  
    crawl(f, "");    // call private recursive helper  
}  
  
// Recursive helper to implement crawl/indent behavior.  
private static void crawl(File f, String indent) {  
    System.out.println(indent + f.getName());  
    if (f.isDirectory()) {  
        // recursive case; print contained files/dirs  
        for (File subFile : f.listFiles()) {  
            crawl(subFile, indent + "    ");  
        }  
    }  
}
```