CSE 311: Foundations of Computing I

Logical Equivalences Reference Sheet

Identity

$$p \wedge \mathsf{T} \equiv p$$
$$p \vee \mathsf{F} \equiv p$$

Domination

$$p \vee \mathsf{T} \equiv \mathsf{T}$$
$$p \wedge \mathsf{F} \equiv \mathsf{F}$$

Idempotency

$$p \vee p \equiv p$$
$$p \wedge p \equiv p$$

Commutativity

$$p \vee q \equiv q \vee p$$
$$p \wedge q \equiv q \wedge p$$

Associativity

$$(p \vee q) \vee r \equiv p \vee (q \vee r)$$
$$(p \wedge q) \wedge r \equiv p \wedge (q \wedge r)$$

Distributivity

$$p \wedge (q \vee r) \equiv (p \wedge q) \vee (p \wedge r)$$
$$p \vee (q \wedge r) \equiv (p \vee q) \wedge (p \vee r)$$

Absorption

$$p \vee (p \wedge q) \equiv p$$
$$p \wedge (p \vee q) \equiv p$$

Negation

$$p \vee \neg p \equiv \mathsf{T}$$
$$p \wedge \neg p \equiv \mathsf{F}$$

DeMorgan's Laws

$$\neg(p \vee q) \equiv \neg p \wedge \neg q$$
$$\neg(p \wedge q) \equiv \neg p \vee \neg q$$

Double Negation

$$\neg\neg p \equiv p$$

Law of Implication

$$p \to q \equiv \neg p \vee q$$

Contrapositive

$$p \to q \equiv \neg q \to \neg p$$