

Homework 9, Due Thursday, March 13, 2008

**Problem 1:**

Section 6.4, Problem 6. (5th edition: section 5.3, problem 6)

**Problem 2:**

Section 6.4, Problem 10. (5th edition: section 5.3, problem 10)

**Problem 3:**

Section 8.1, Problem 4. (5th edition: section 7.1, problem 4)

**Problem 4:**

Section 8.1, Problem 34 a, b, c, d. (5th edition: section 7.1, problem 34 a, b, c, d)

**Problem 5:**

Section 8.3, Problem 10 a, b, c. (5th edition: section 7.3, problem 10 a, b, c)

**Problem 6:**

Section 8.3, Problem 14 a, c, e. (5th edition: section 7.3, problem 14 a, c, e)

**Problem 7:**

For the relation  $R = \{(b, c), (b, e), (c, e), (d, a), (e, b), (e, c)\}$  on  $\{a, b, c, d, e\}$ , draw the following relations in directed graph form:

- a)  $R$
- b) The symmetric closure of  $R$
- c) The transitive closure of  $R$

**Problem 8:**

Let  $R$  be the relation on ordered pairs of positive integers such that  $((a, b), (c, d)) \in R$  if and only if  $ad = bc$ . Show that  $R$  is an equivalence relation. (Note that this is a relation on a set of ordered pairs. Think of the ordered pairs as fractions:  $(\frac{a}{b}, \frac{c}{d}) \in R$  if and only if  $ad = bc$ .)

**Extra Credit 9:**

For undirected simple graphs, prove that if  $G$  is disconnected, then  $\overline{G}$ , the complement of  $G$ , is connected. ( $\overline{G}$  is made up of the edges that are absent from  $G$ .)

**Extra Credit 10:**

Suppose that  $G$  is an undirected graph and every vertex has degree at least  $d$  for some  $d > 2$ . Prove that  $G$  must contain a (simple) cycle of length at least  $d + 1$ .