



Project Orientation

...the sequel

Krysta Yousoufian

CSE 331 Section, 2/9/2012

Announcements

- Email course staff if using late day for HW4
- Office hours switchup
 - Me: 4-5 today, CSE 002
 - Hal: 3:30-4:30 tomorrow, CSE 002(?)

HW5

- Build a route-finder between UW buildings
- Given data:
 - Map of campus (won't need for this HW5)
 - Names, pixel coords of buildings
 - Start, end coords of path segments
- Nodes: points on the graph
 - Buildings
 - Non-building path endpoints
- Edges: path segments between points
 - Cost: length of path

Comparability

- Multiple routes between buildings
- Want route with shortest distance
- Natural *ordering* to routes:
 - $\text{route1} < \text{route2}$ if route1 is faster
 - $\text{route1} == \text{route2}$ if same distance
 - $\text{route1} > \text{route2}$ if route1 is slower
- Routes are *comparable*

Comparable<E>

- Comparable<E>: Java interface for objects with a natural ordering
- Method: a.compareTo(b)
 - Returns < 0 if $a < b$
 - Returns 0 if a.equals(b)
 - Returns > 0 if $a > b$
- <http://docs.oracle.com/javase/6/docs/api/index.html?overview-summary.html>

Equality

- `compareTo()`
 - Classes with a natural ordering that implement `Comparable`
 - Should return 0 iff `equals()` returns true
- `equals()`
 - Defined in all classes
 - Default: `Object.equals()` – reference equality
 - Can be overridden:
`@Override`
`public void equals(Object other)`

HashMaps

- You've seen dictionaries/maps
 - Set of <Key, Value> pairs
 - Lookup by key, get corresponding value
 - Student directory: <name, contact info>
 - *Webster's Dictionary*: <word, definition>
 - Time schedule: <SLN, class information>
- **Hashmaps: $O(1)$ lookup of keys**
 - Lookup time is independent of size of map
 - Too good to be true?!
 - Java: HashMap or Hashtable (keys \rightarrow values), HashSet (just keys)

Hash functions

- Hash tables use a **hash function**
 - Function from key (any object) to hash value (int)
- Used to index into array storing <key, value> pairs
- If you don't find the key at this index (or nearby), assume it's not in the list
- If “equal” objects have different hash values, lookups will fail – incorrectly report that object is not present

public int hashCode()

- Method provided by all Java objects
- Returns object's hash value
- Inherited from Object: if $a == b$, then $a.hashCode() == b.hashCode()$
- More generally: if $a.equals(b)$, then $a.hashCode() == b.hashCode()$
 - If $!a.equals(b)$, then it doesn't strictly matter either way
- **If you override equals(), you must override hashCode()**
 - Equal objects must have same hash code

Parsing the Data

- You write the parser (probably)

- Buildings:

shortName longName xCoord yCoord

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- Paths:

- Map from coord. pairs \rightarrow connected coords.
and distance

$(x,y) \rightarrow \{ (x,y,dist), \dots \}$

Path data example

- $(1200, 1800) \rightarrow \{$
 $(1212, 1823): 10.5,$
 $(1250, 1795): 9.8,$
 $(1169, 1850): 12.4$
 $\}$

Path data example

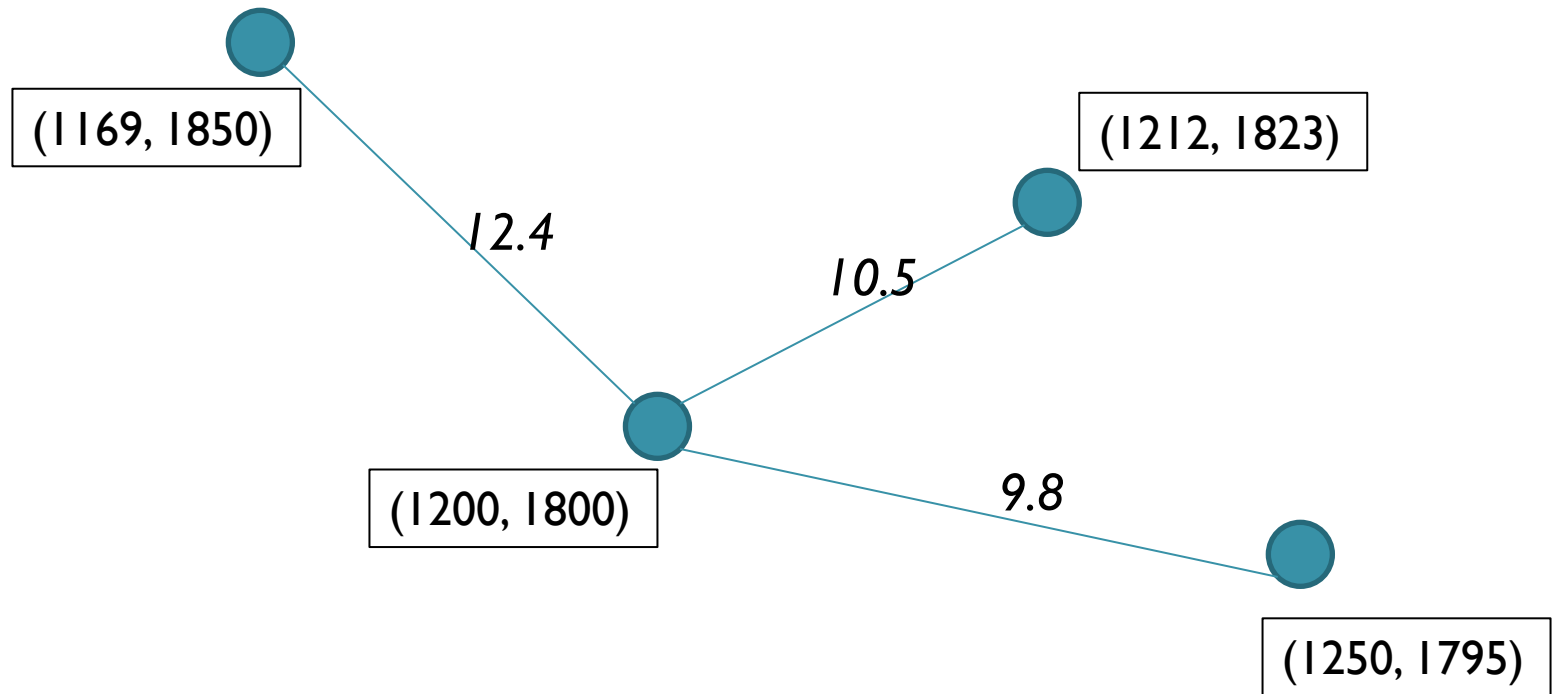
- $(1200, 1800) \rightarrow \{$
 $(1212, 1823): 10.5,$
 $(1250, 1795): 9.8,$
 $(1169, 1850): 12.4$
}

There is a path segment to this point...

...with this length

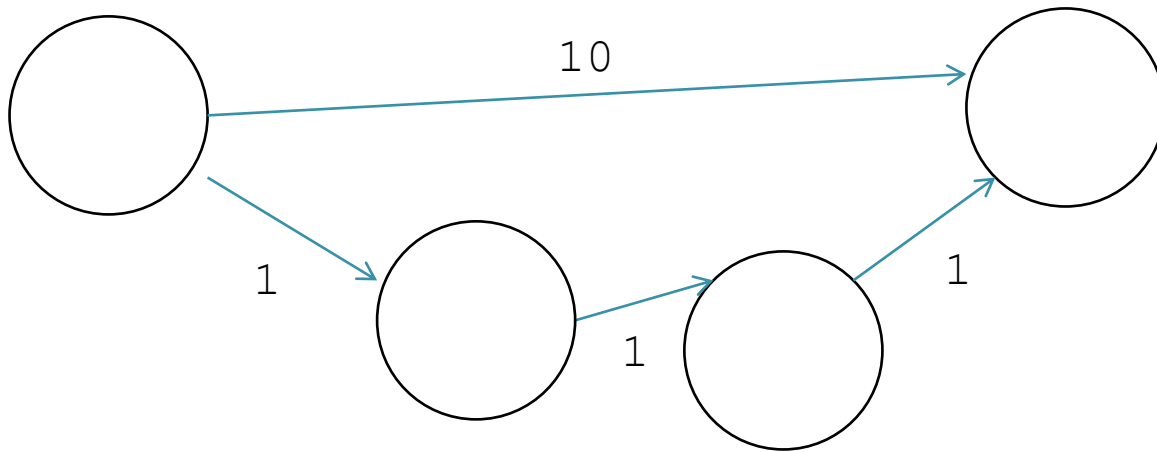
Visualization

(1200, 1800) → {
 (1212, 1823): 10.5,
 (1250, 1795): 9.8,
 (1169, 1850): 12.4
}

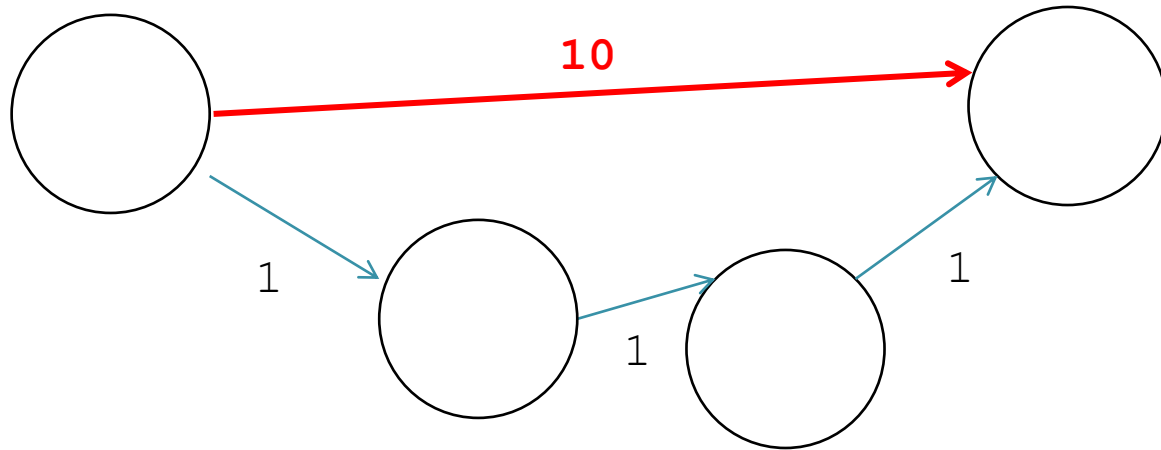


Minimum-Cost Paths

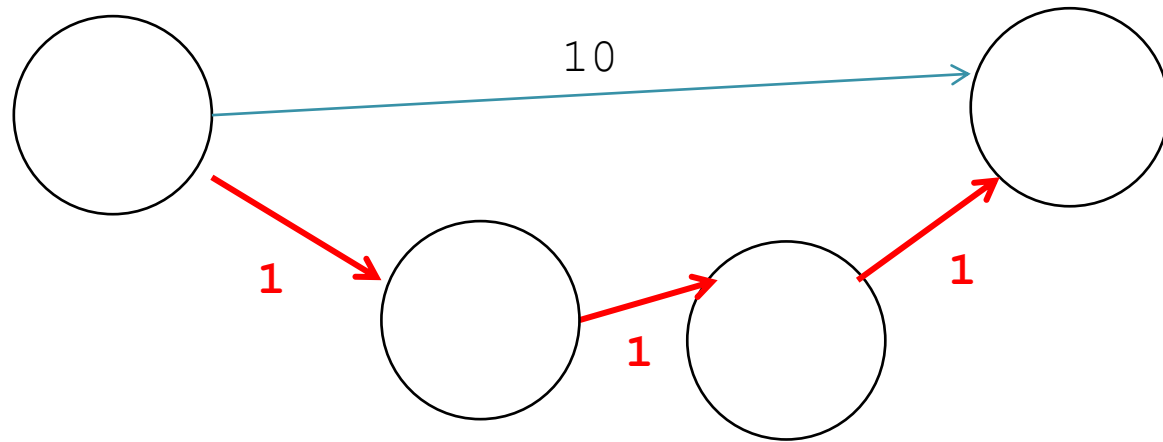
- Edge label is a *cost*
 - Money, time, ...
 - Here, cost represents distance
- Want to find minimum-cost path
 - Not necessarily shortest path (in # of edges)



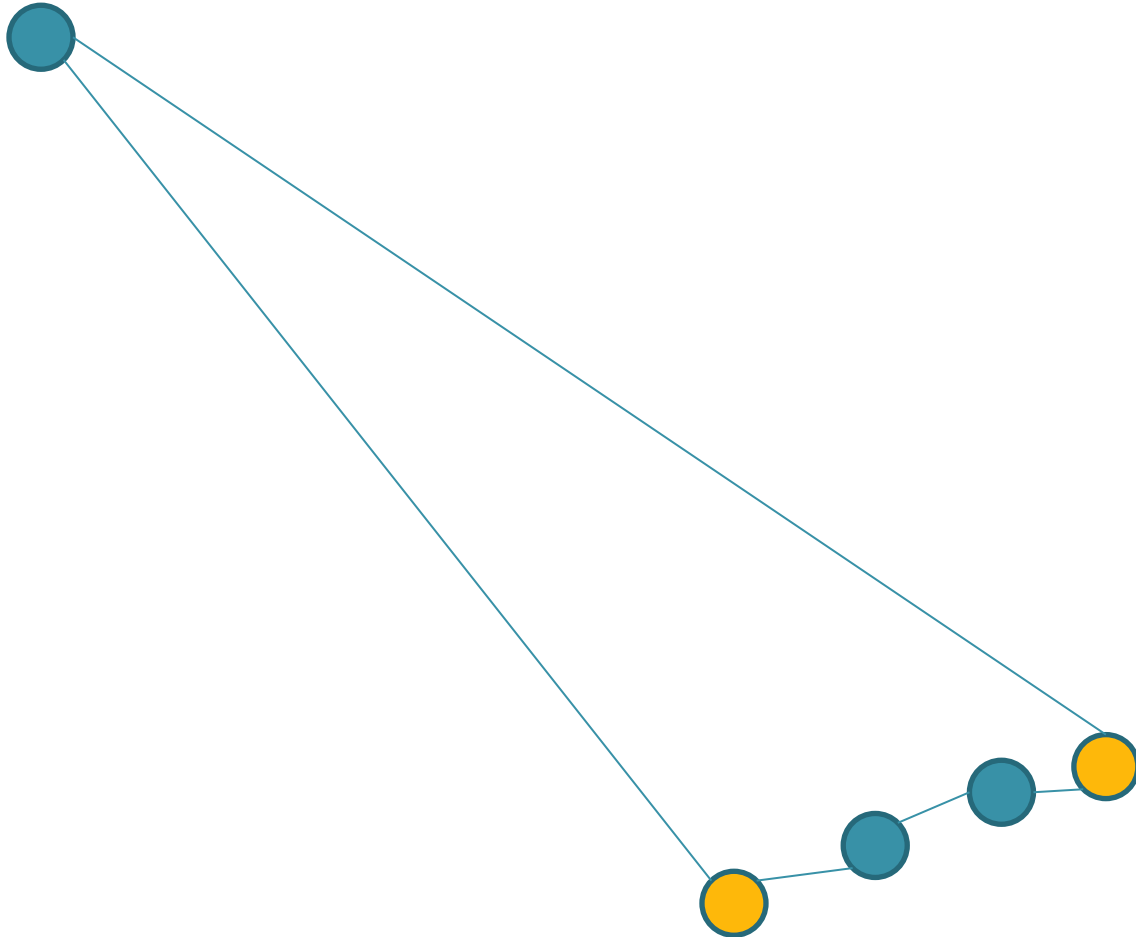
Shortest Path



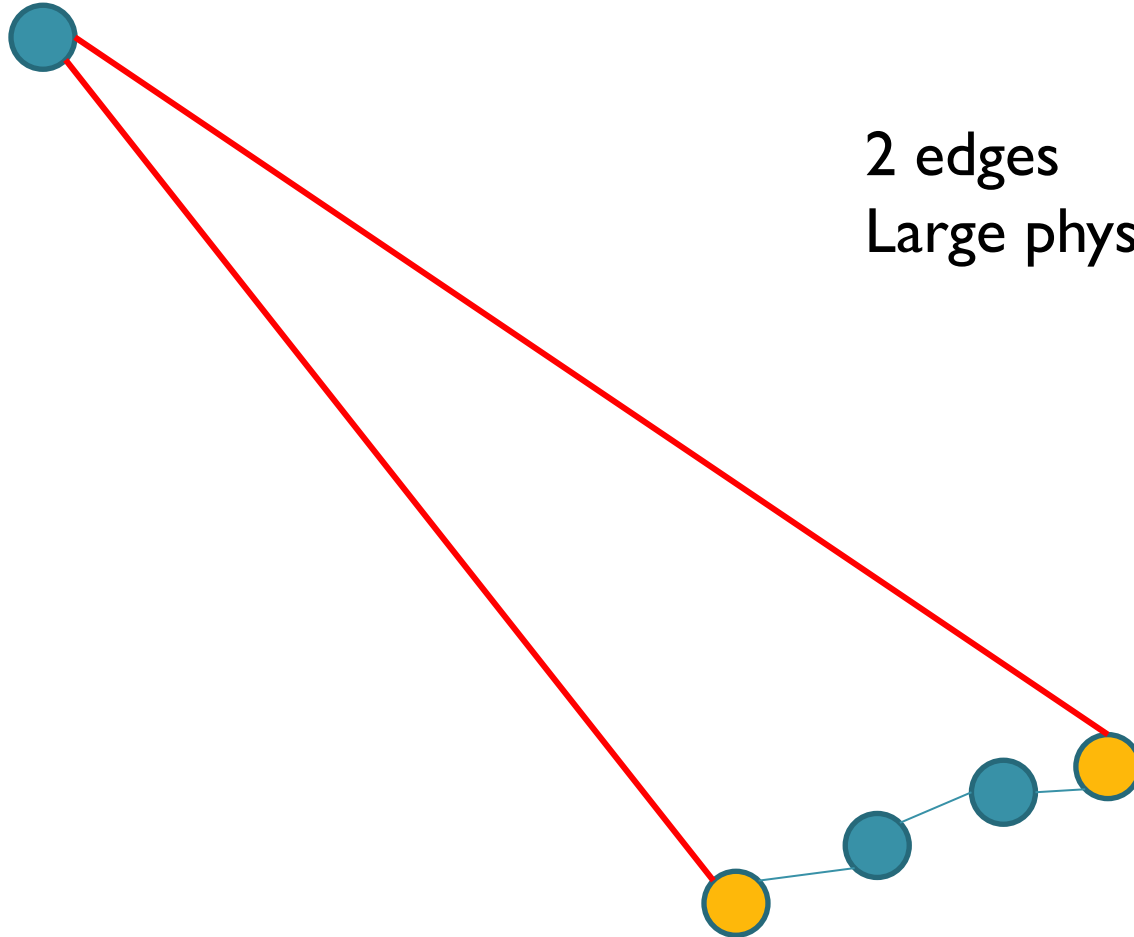
Min-Cost Path



Physical Map as Graph



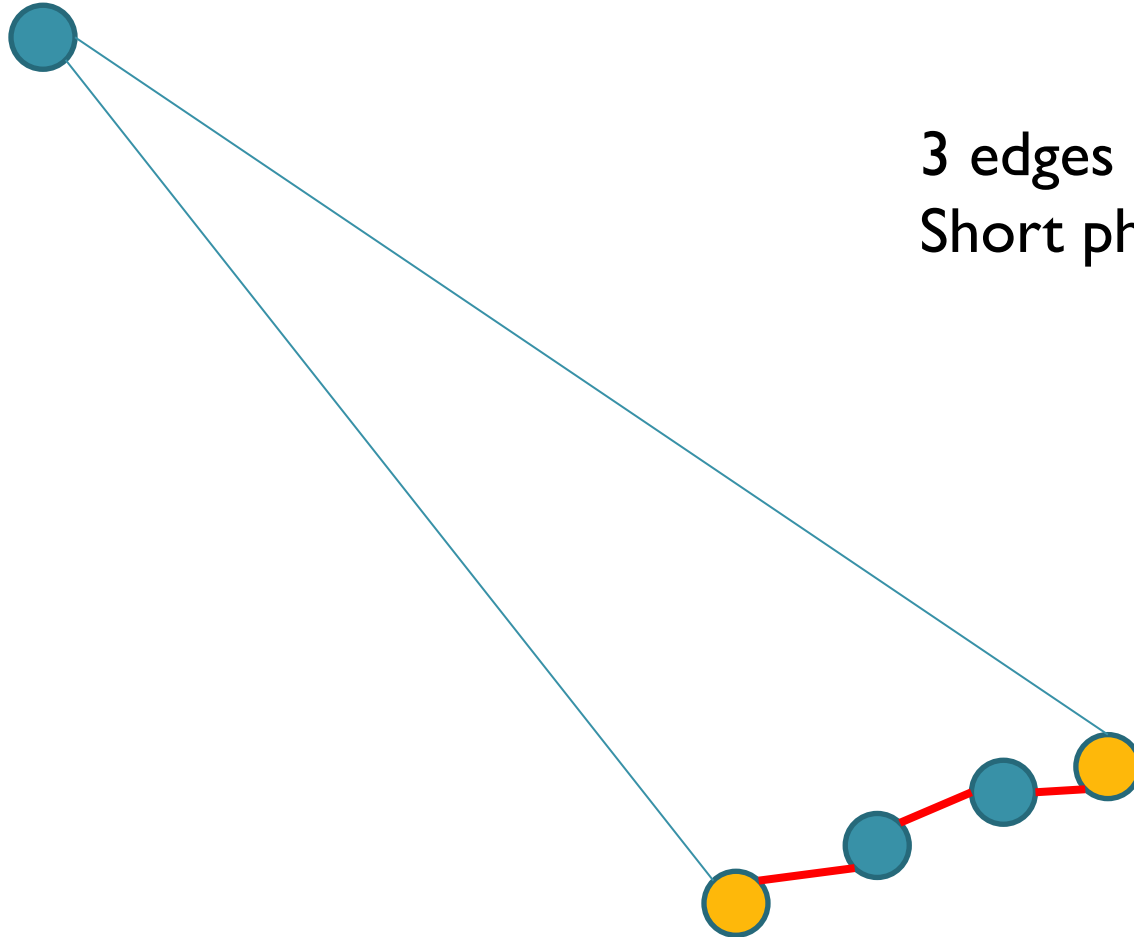
Physical Map as Graph



2 edges

Large physical distance

Physical Map as Graph



3 edges

Short physical distance

Priority Queues

- Set of objects with some ordering
- Knows the minimum object in the list
- Operations: add(), removeMin()
- (Assuming review; come to OH if not)

Priority Queues

- Application: Dijkstra's algorithm
 - Find min-cost path from source node s
 - Data: nodes
 - Ordering: min-cost path from s so far

- Java:

- PriorityQueue

<http://docs.oracle.com/javase/6/docs/api/index.html?overview-summary.html>

- Comparable

<http://docs.oracle.com/javase/6/docs/api/index.html?overview-summary.html>

- **Create** `PriorityQueue<MyClass>` **where**
`MyClass` implements `Comparable<MyClass>`

Dijkstra's Algorithm

- Want: min-cost path from s to t
- Get: min-cost path from s to all other nodes (traditionally)
- Optimized: stop when we find min-cost path for t

Dijkstra's Algorithm

Invariants:

- $p(s,n)$ = min-cost path known *so far* from s to n for any node n
- $c(s,n)$ = cost of $p(s,n)$
- `PriorityQueue active` = { n | we know *some* path $p(s,n)$, but maybe not optimal path }
- `active` ordered by $c(s,n)$
- Set `finished` = { n | we know optimal path ($s\dots n$) }

Initial setup:

$$c(s,s) = 0$$

$$c(s,n) = \text{infinity/unknown for } s \neq n$$

Insert s into `active`

Dijkstra's Algorithm

While `active` is not empty:

Remove the element `n` with minimum $c(s,n)$

For each neighbor `m` of `n`:

If `m` is not in `finished` (i.e. haven't found optimal path):

Let `e` denote the edge $\langle n,m \rangle$

If $c(s,m)$ is unknown or is $> c(s,n) + c(e)$

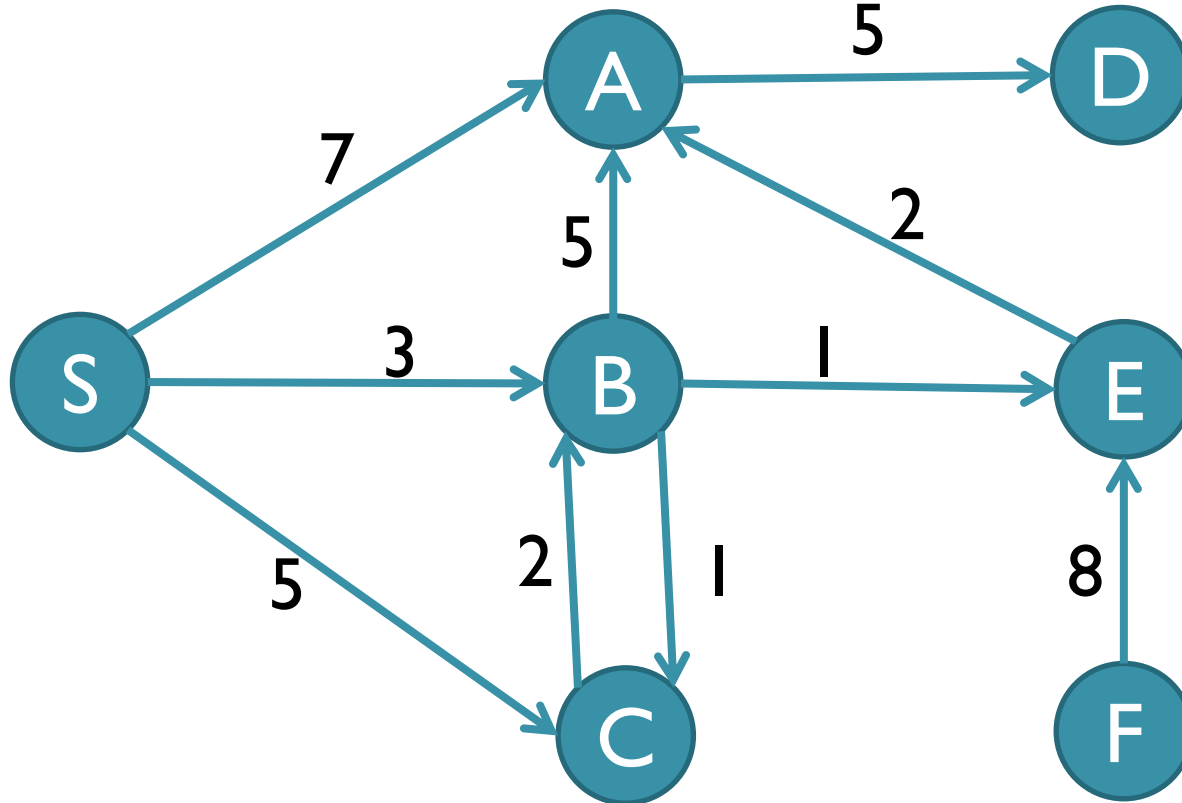
$$p(s,m) = p(s,n) + e$$

$$c(s,m) = c(s,n) + c(e)$$

Add or reorder `m` in `active`

Add `n` to `finished`

Example

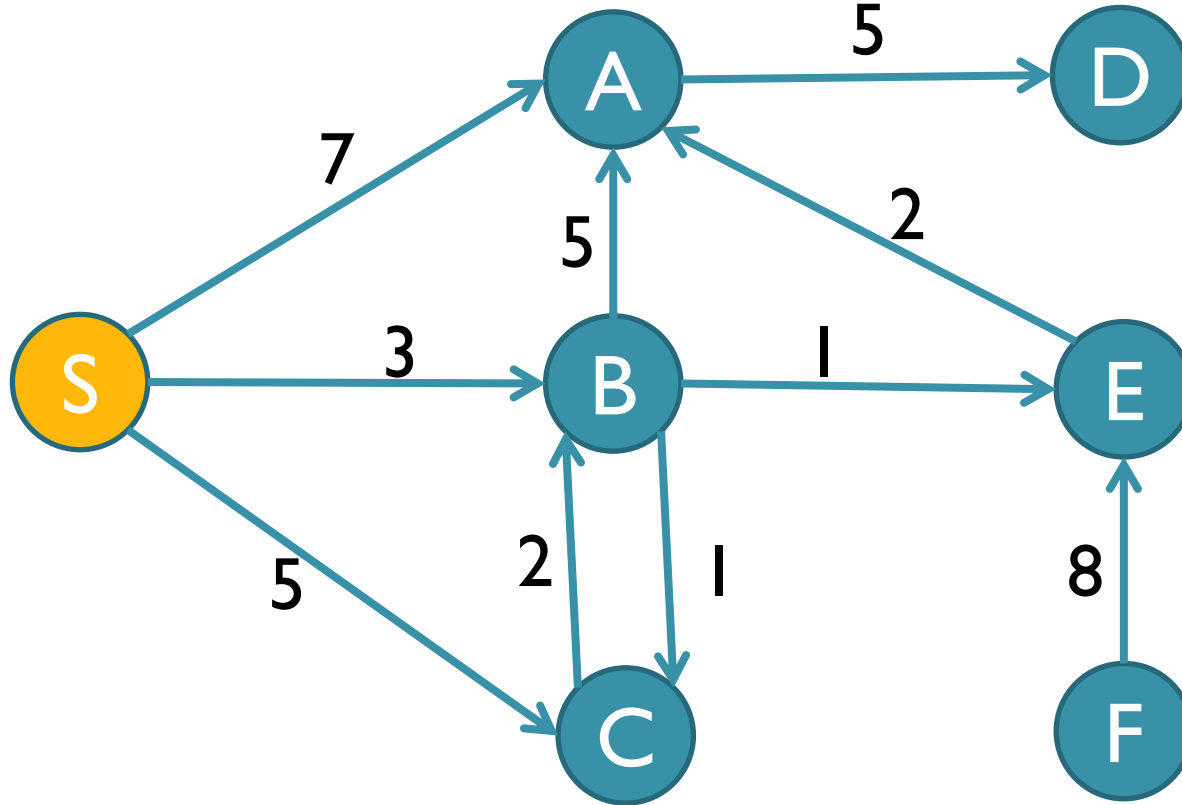


active = {S}
finished = { }
Min-cost paths:

A: ?
B: ?
C: ?
D: ?
E: ?
F: ?
S: 0

(from *Data Structures & Their Algorithms*, Lewis & Denenberg, 1991)

Example



active = {A,B,C}
finished = {S}

Min-cost paths:

A: ~~?~~ $0+7 = 7$

B: ~~?~~ $0+3 = 3$

C: ~~?~~ $0+5 = 5$

D: ?

E: ?

F: ?

S: 0

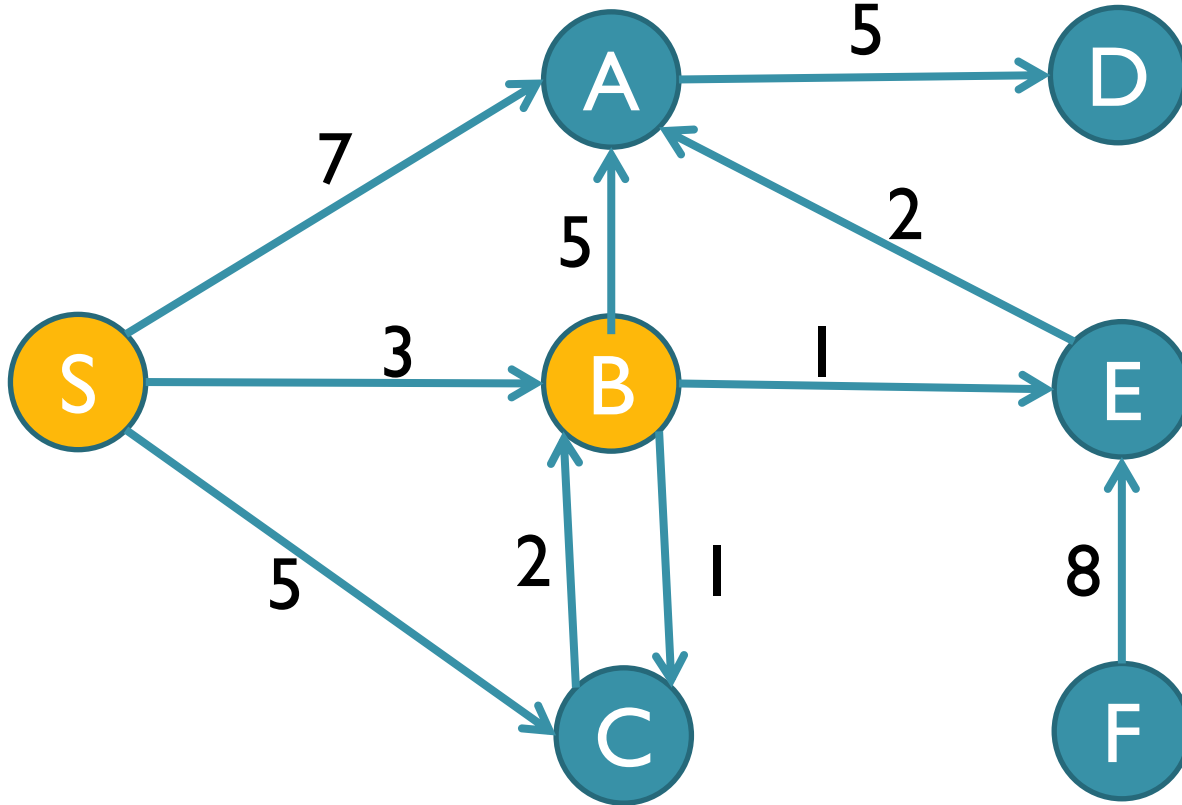
(from *Data Structures & Their Algorithms*, Lewis & Denenberg, 1991)

Example

active = {A,C,E}
finished = {B,S}

Min-cost paths:

A: 7
B: 3
C: ~~5~~ 3+1=4
D: ?
E: ~~2~~ 3+1=4
F: ?
S: 0



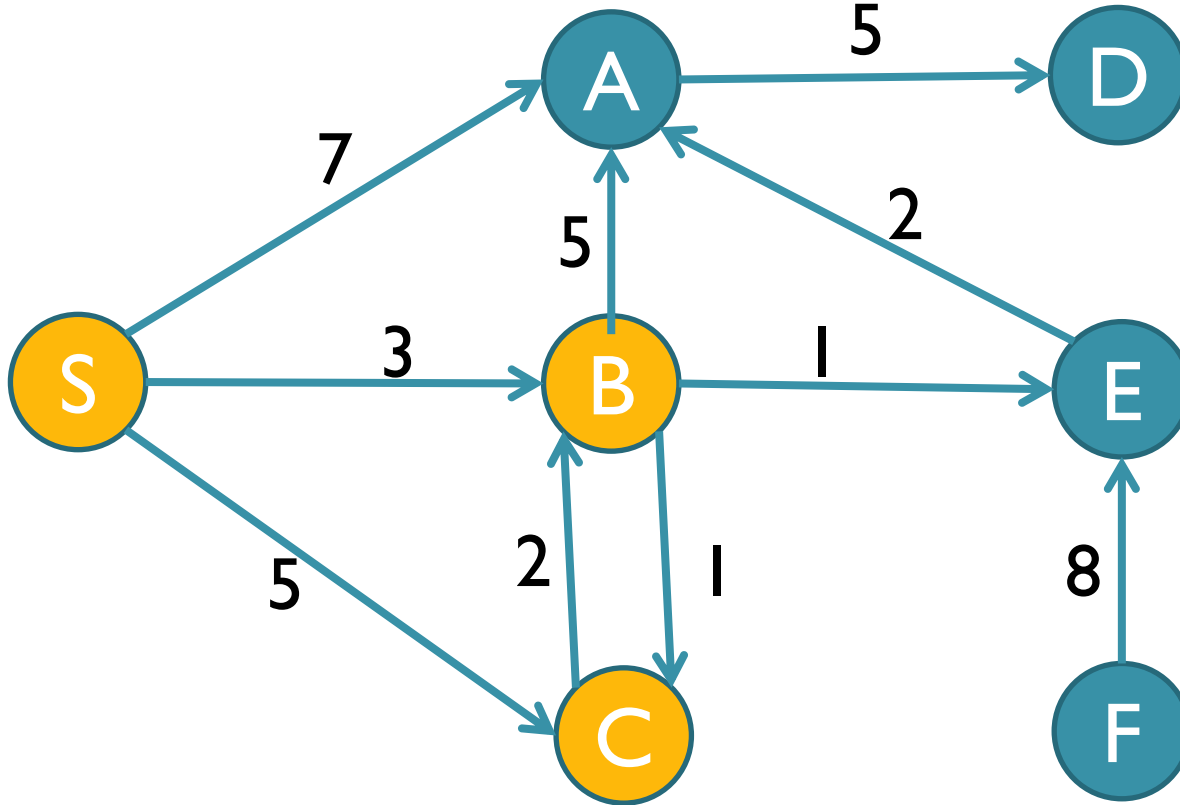
(from *Data Structures & Their Algorithms*, Lewis & Denenberg, 1991)

Example

active = {A,E}
finished = {B,C,S}

Min-cost paths:

A: 7
B: 3
C: 4
D: ?
E: 4
F: ?
S: 0



(from *Data Structures & Their Algorithms*, Lewis & Denenberg, 1991)

Example

active = {A}
finished = {B, C, E, S}

Min-cost paths:

A: 7 4+2=6

B: 3

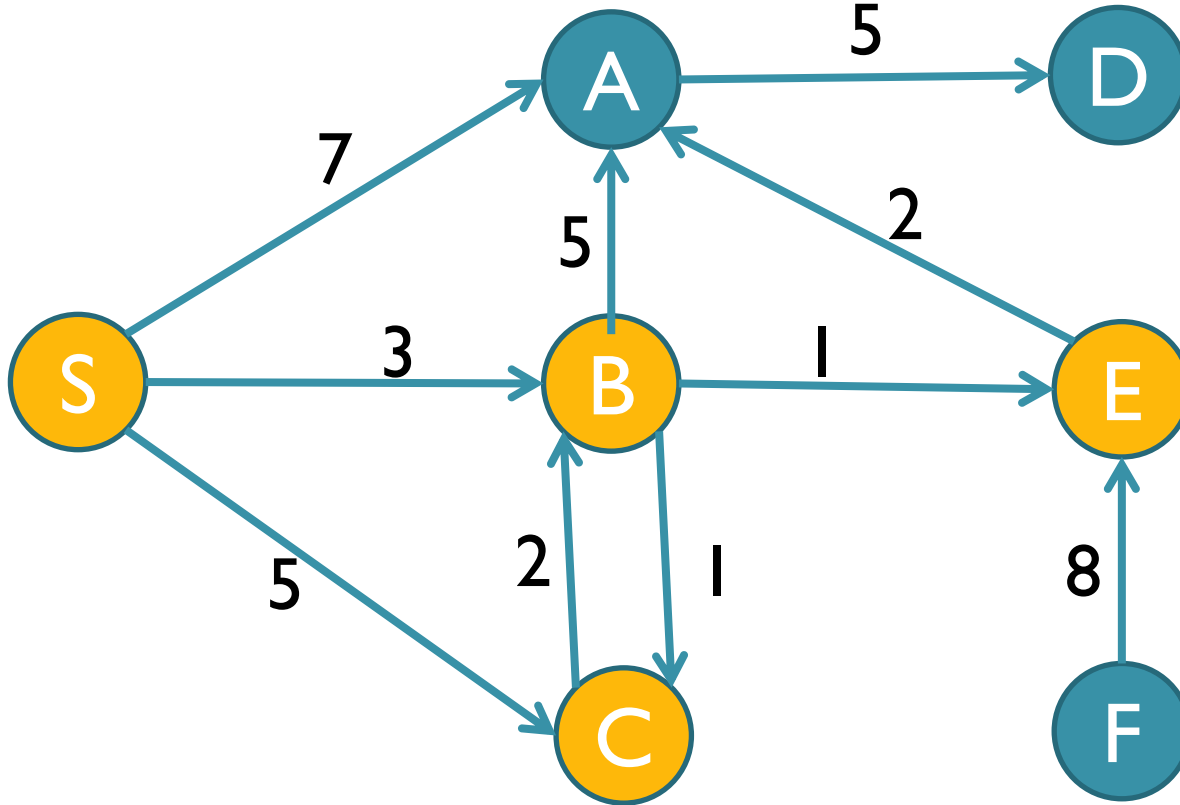
C: 4

D: ?

E: 4

F: ?

S: 0



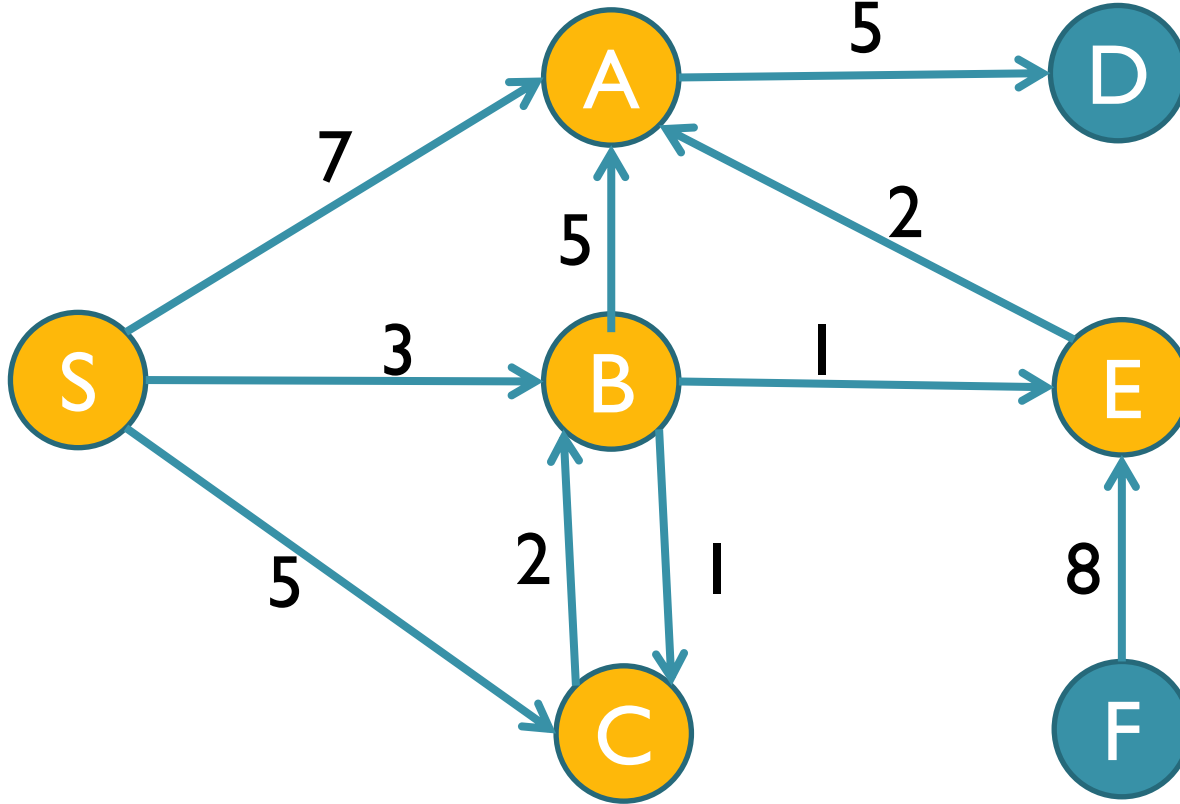
(from *Data Structures & Their Algorithms*, Lewis & Denenberg, 1991)

Example

active = {D}
finished = {A, B, C, E, S}

Min-cost paths:

A: 6
B: 3
C: 4
D: ? 6+5=12
E: 4
F: ?
S: 0



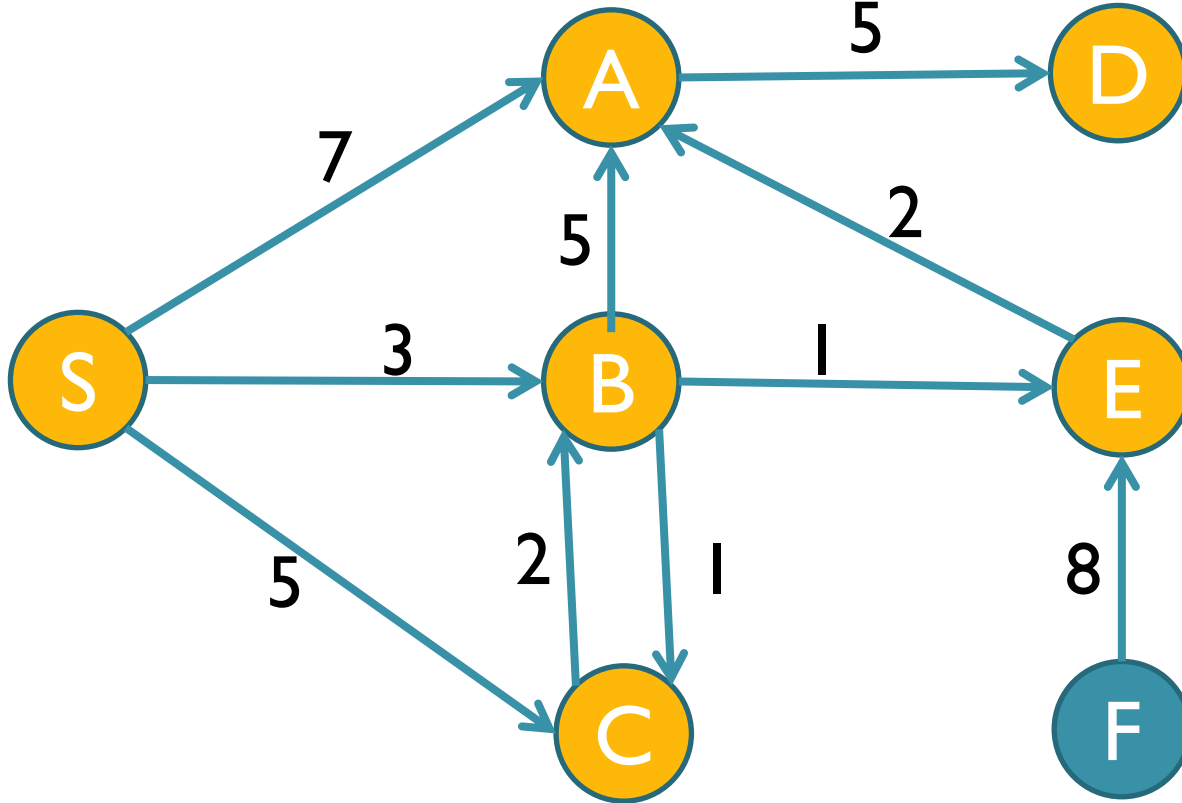
(from *Data Structures & Their Algorithms*, Lewis & Denenberg, 1991)

Example

active = {}
finished = {A, B, C, D, E, S}

Min-cost paths:

A: 6
B: 3
C: 4
D: 11
E: 4
F: ?
S: 0



(from *Data Structures & Their Algorithms*, Lewis & Denenberg, 1991)