

Section 5: HW6 and Midterm

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(with material from Alex Mariakakis,
Kellen Donohue, David Mailhot, and Hal Perkins)

Breadth-First Search (BFS)

Often used for discovering connectivity

Calculates the shortest path *if and only if* all edges have same positive or no weight

Depth-first search (DFS) is commonly mentioned with BFS

BFS looks “wide”, DFS looks “deep”

Can also be used for discovery, but not the shortest path

BFS Pseudocode

```
public boolean find(Node start, Node end) {
    put start node in a queue
    while (queue is not empty) {
        pop node N off queue
        if (N is goal)
            return true;
        else {
            for each node O that is child of N
                push O onto queue
        }
    }
    return false;
}
```

Breadth-First Search

START:

Q: <A>

Pop: A, Q: <>

Q: <B, C>

Pop: B, Q: <C>

Q: <C>

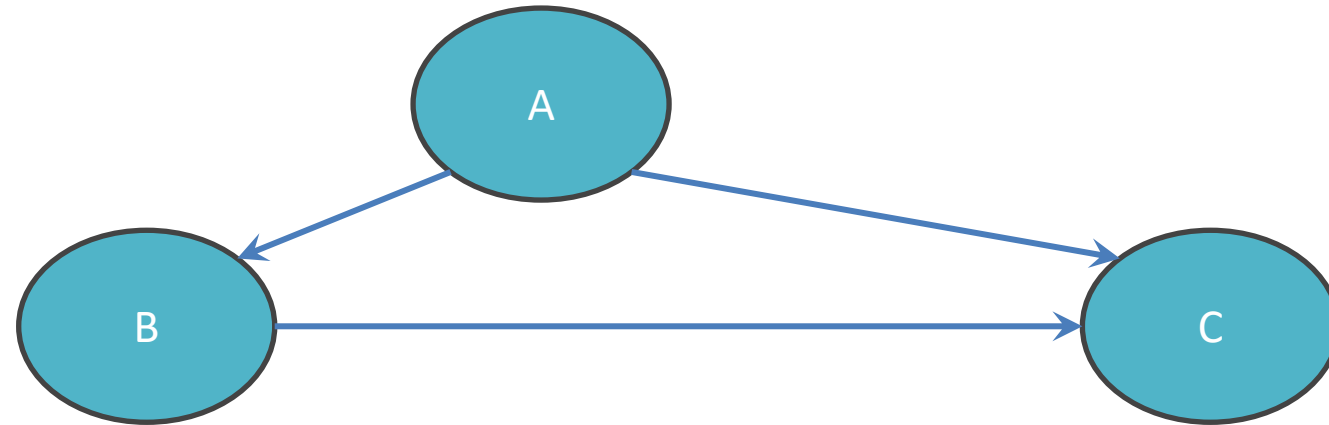
Pop: C, Q: <C>

Q: <>

DONE

Starting at A

Goal: Fully explore



Breadth-First Search with Cycle

START:

Q: <A>

Pop: A, Q: <>

Q:

Pop: B, Q: <>

Q: <C>

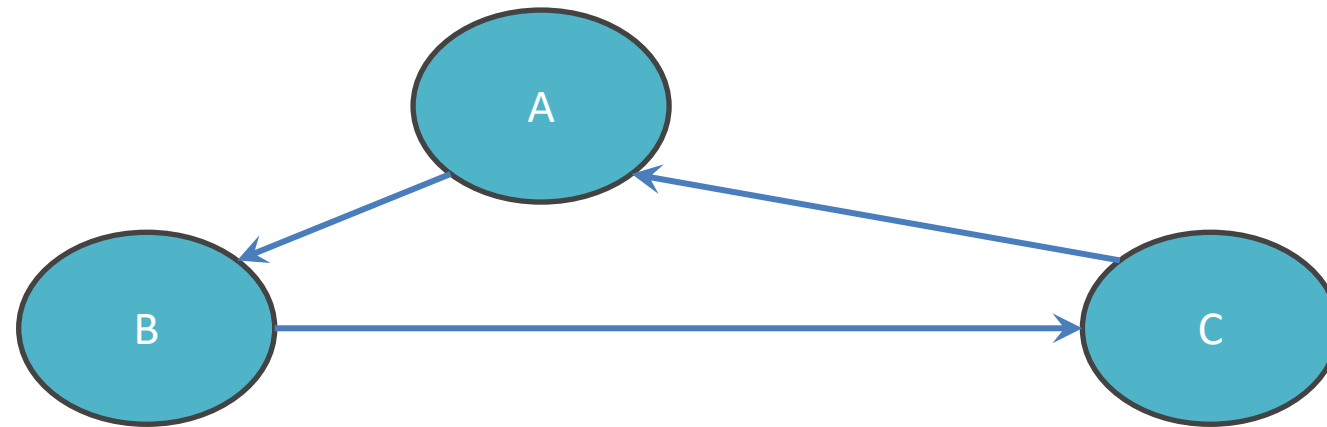
Pop: C, Q: <>

Q: <A>

NEVER DONE

Starting at A

Goal: Fully Explore



BFS Pseudocode

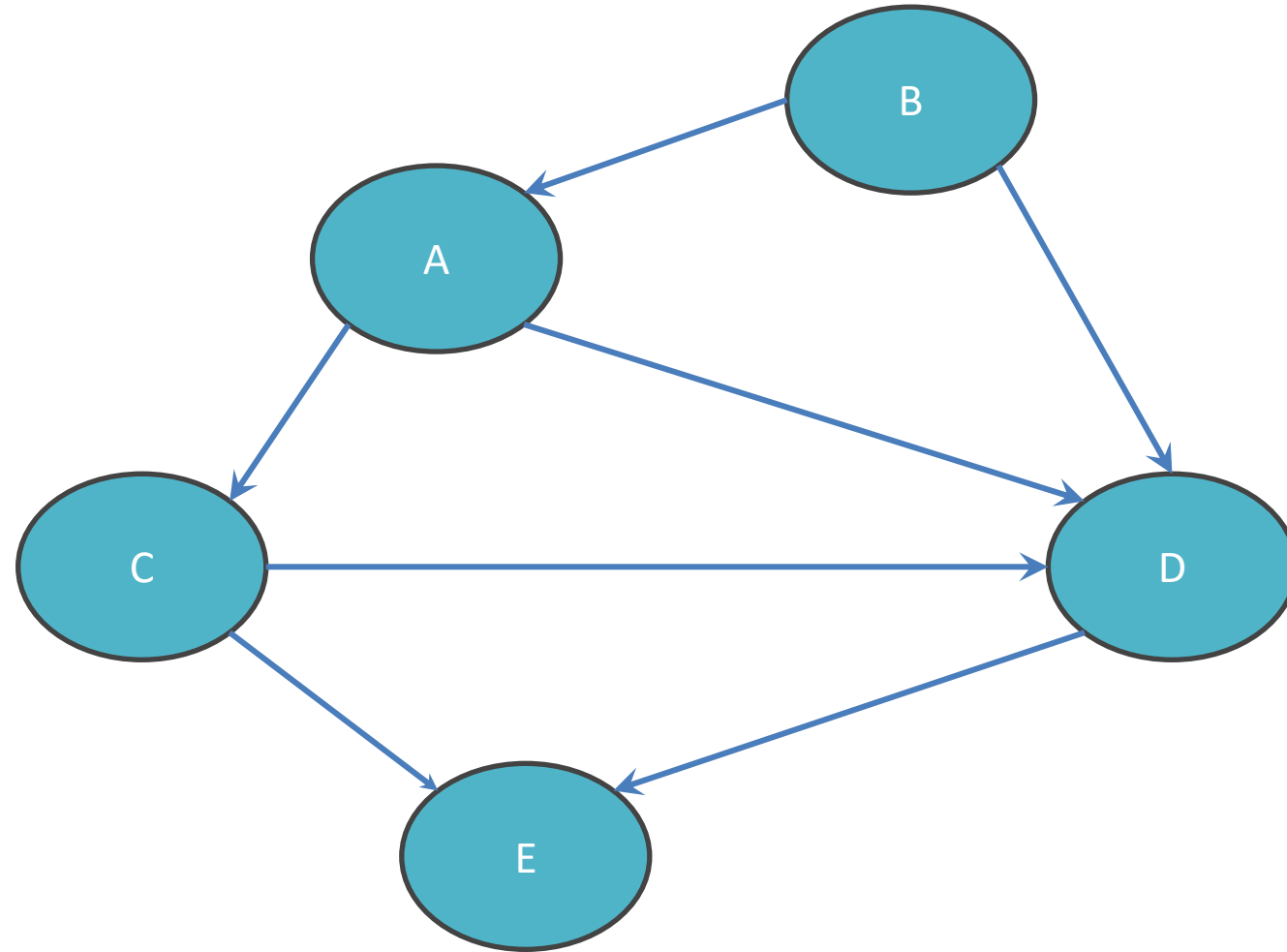
```
public boolean find(Node start, Node end) {
    put start node in a queue
    while (queue is not empty) {
        pop node N off queue
        mark node N as visited

        if (N is goal)
            return true;
        else {
            for each node O that is child of N
                if O is not marked visited
                    push O onto queue
        }
    }
    return false;
}
```

Mark the node as visited!

Breadth-First Search

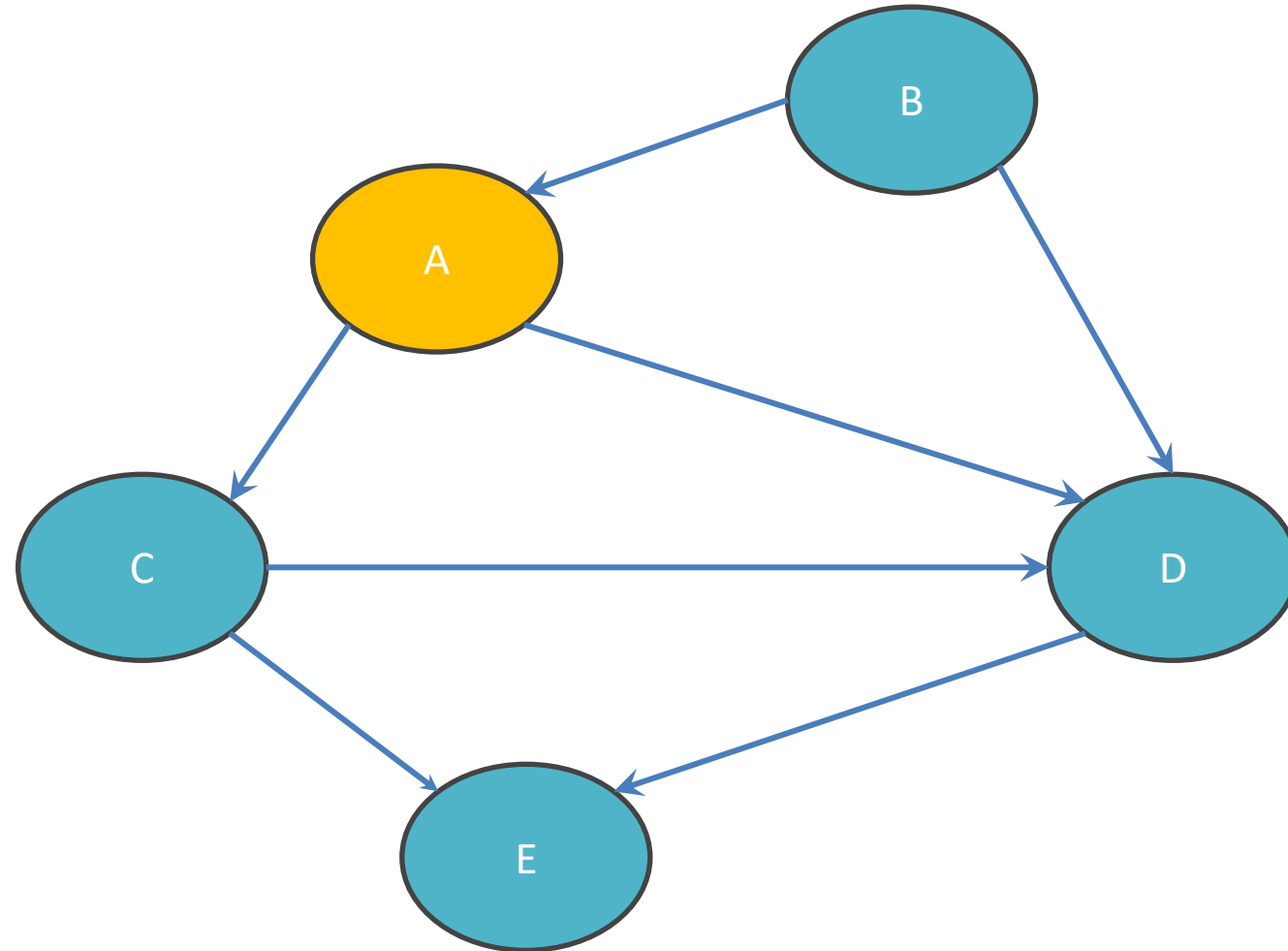
Q: <>



Breadth-First Search

Q: <>

Q: <A>

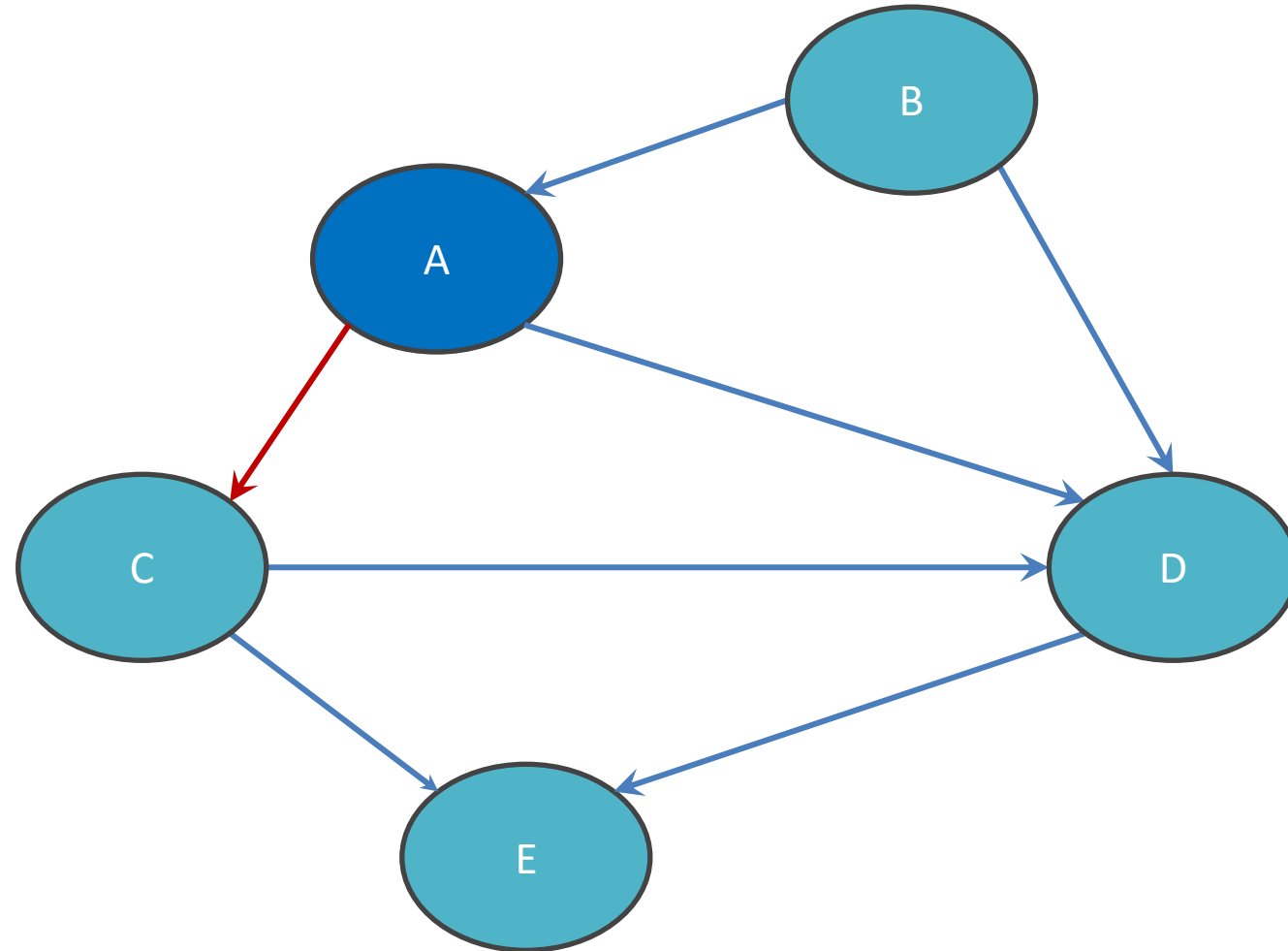


Breadth-First Search

Q: <>

Q: <A>

Q: <>



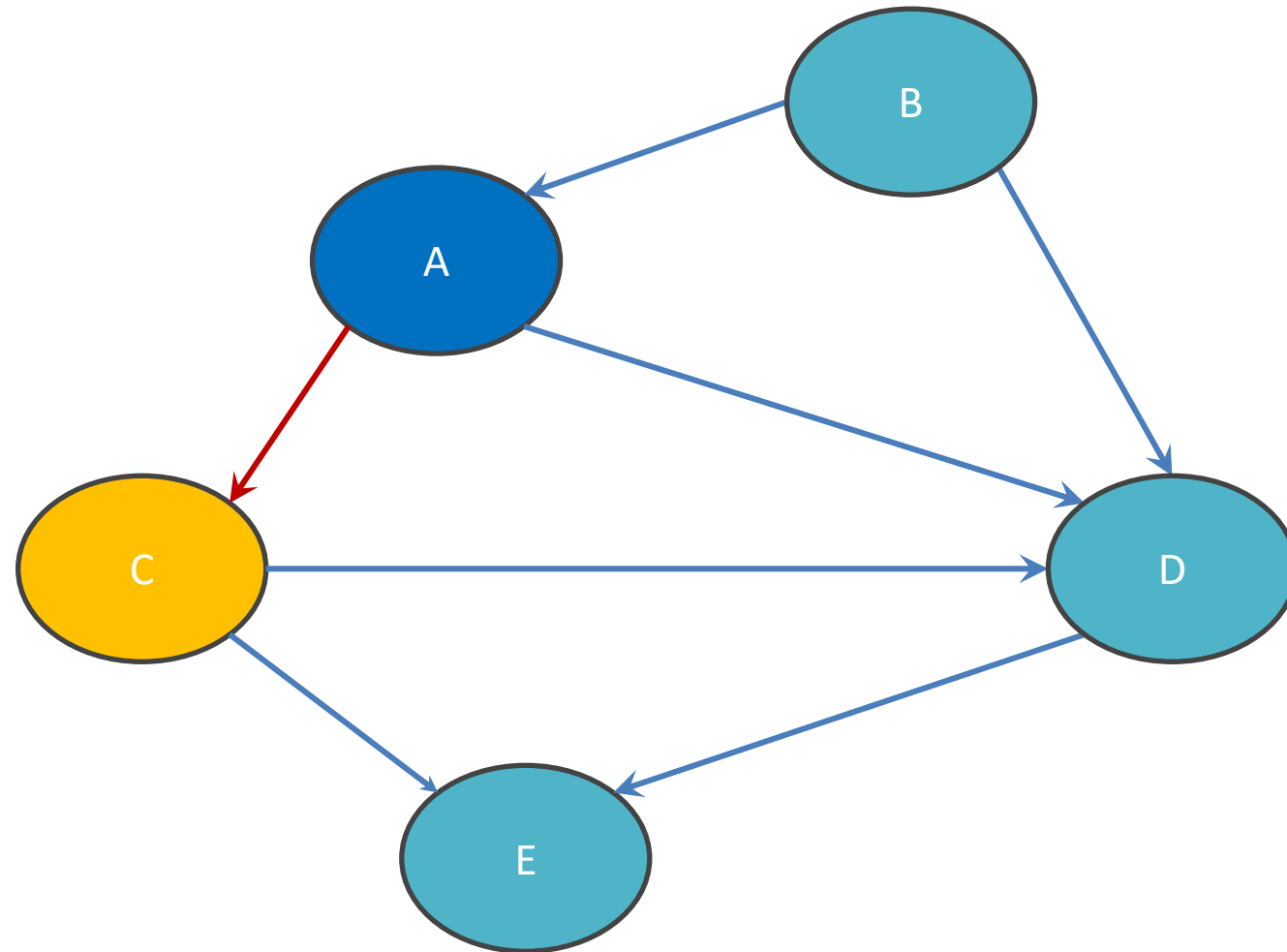
Breadth-First Search

Q: <>

Q: <A>

Q: <>

Q: <C>



Breadth-First Search

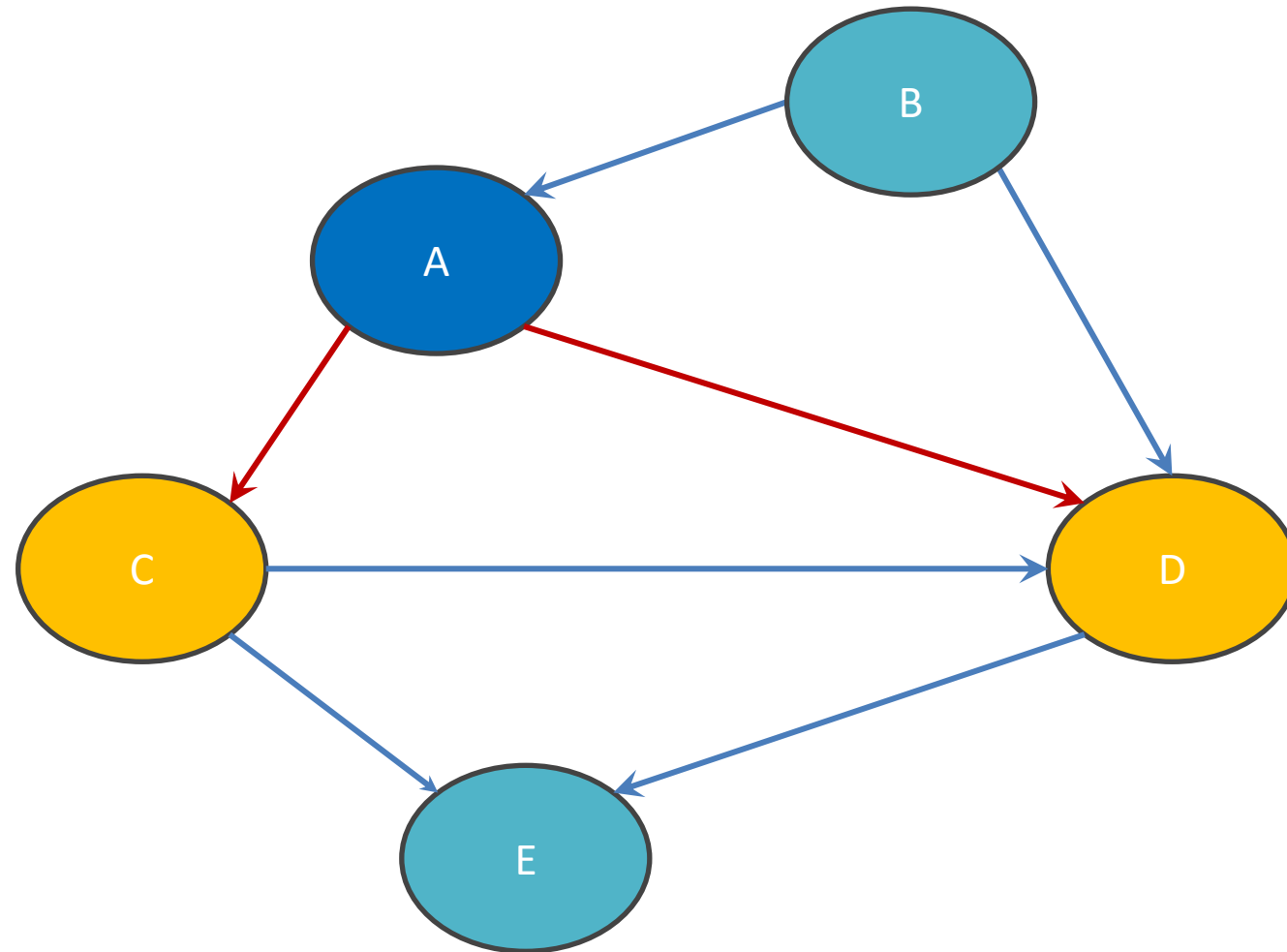
Q: <>

Q: <A>

Q: <>

Q: <C>

Q: <C ,D>



Breadth-First Search

Q: <>

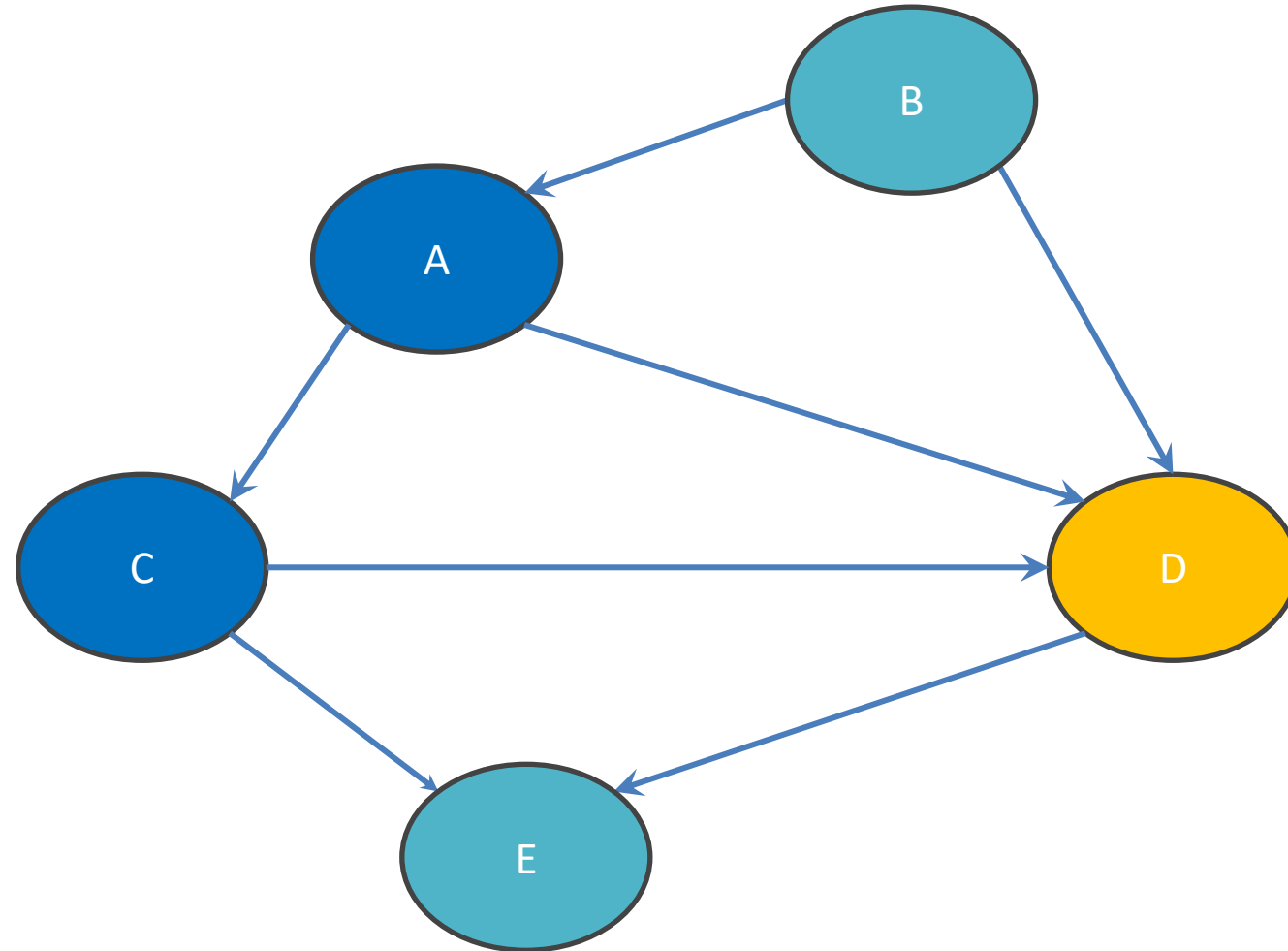
Q: <A>

Q: <>

Q: <C>

Q: <C ,D>

Q: <D>



Breadth-First Search

Q: <>

Q: <A>

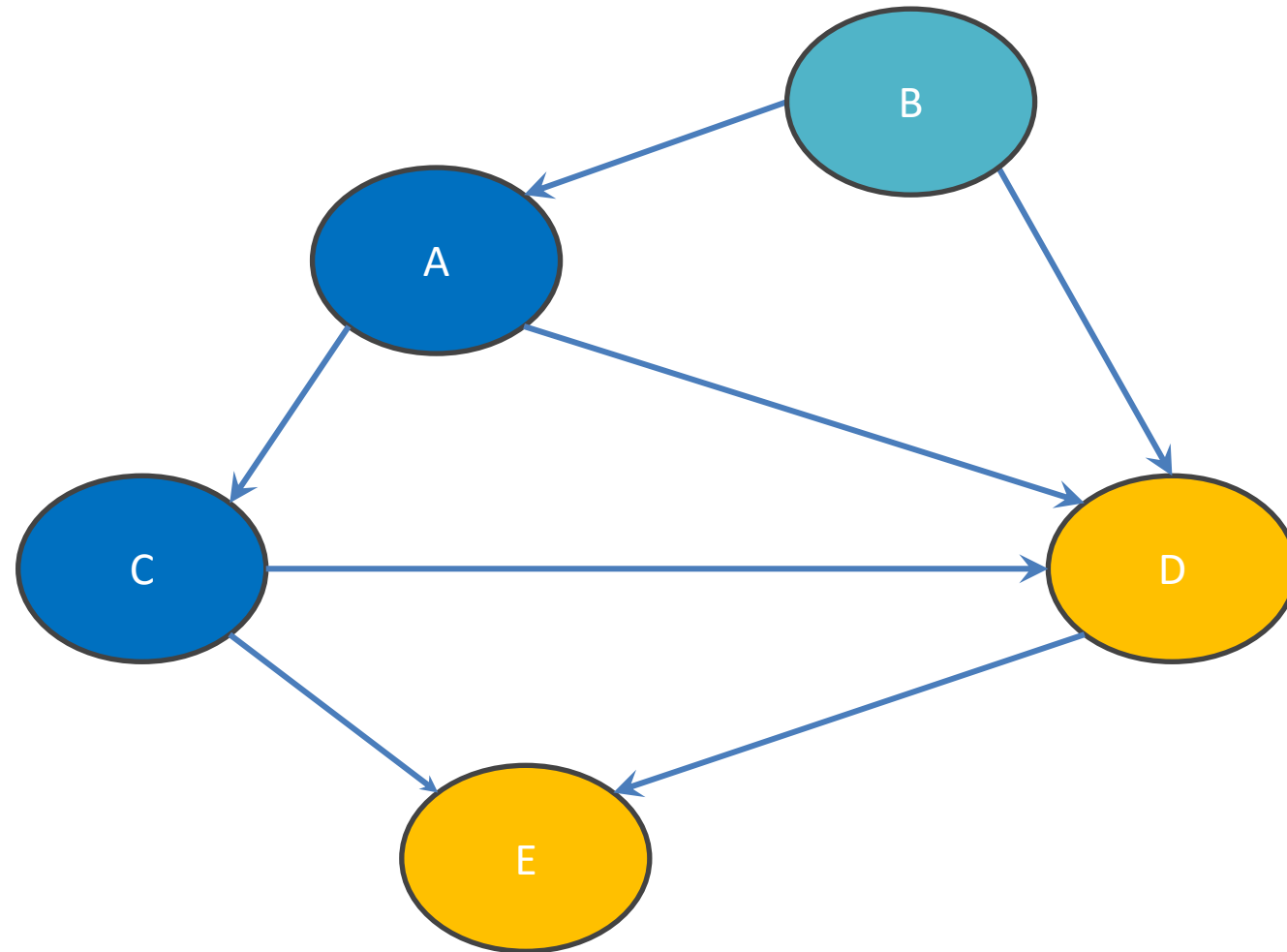
Q: <>

Q: <C>

Q: <C, D>

Q: <D>

Q: <D, E>



Breadth-First Search

Q: <>

Q: <A>

Q: <>

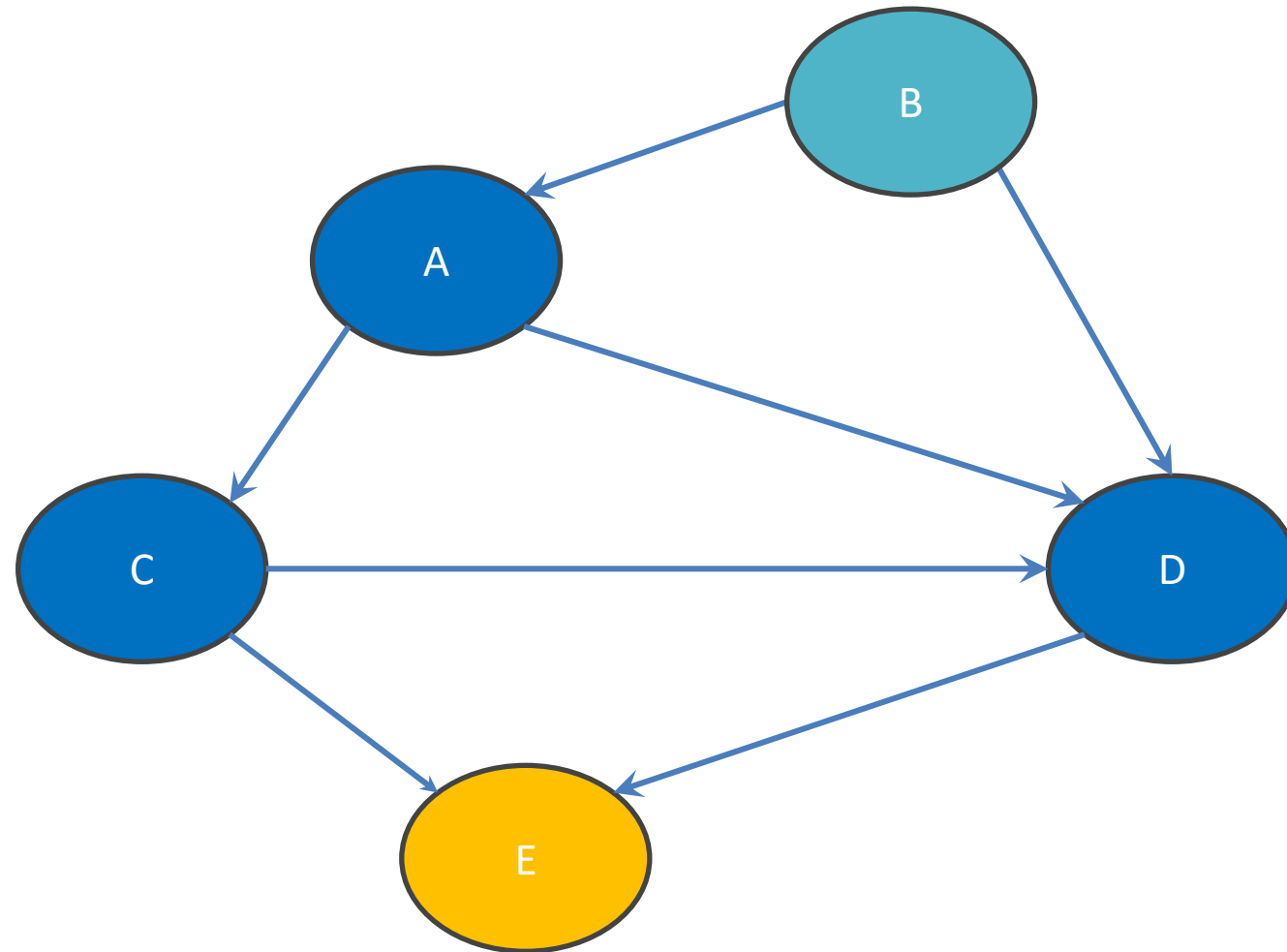
Q: <C>

Q: <C, D>

Q: <D>

Q: <D, E>

Q: <E>



Breadth-First Search

Q: <>

Q: <A>

Q: <>

Q: <C>

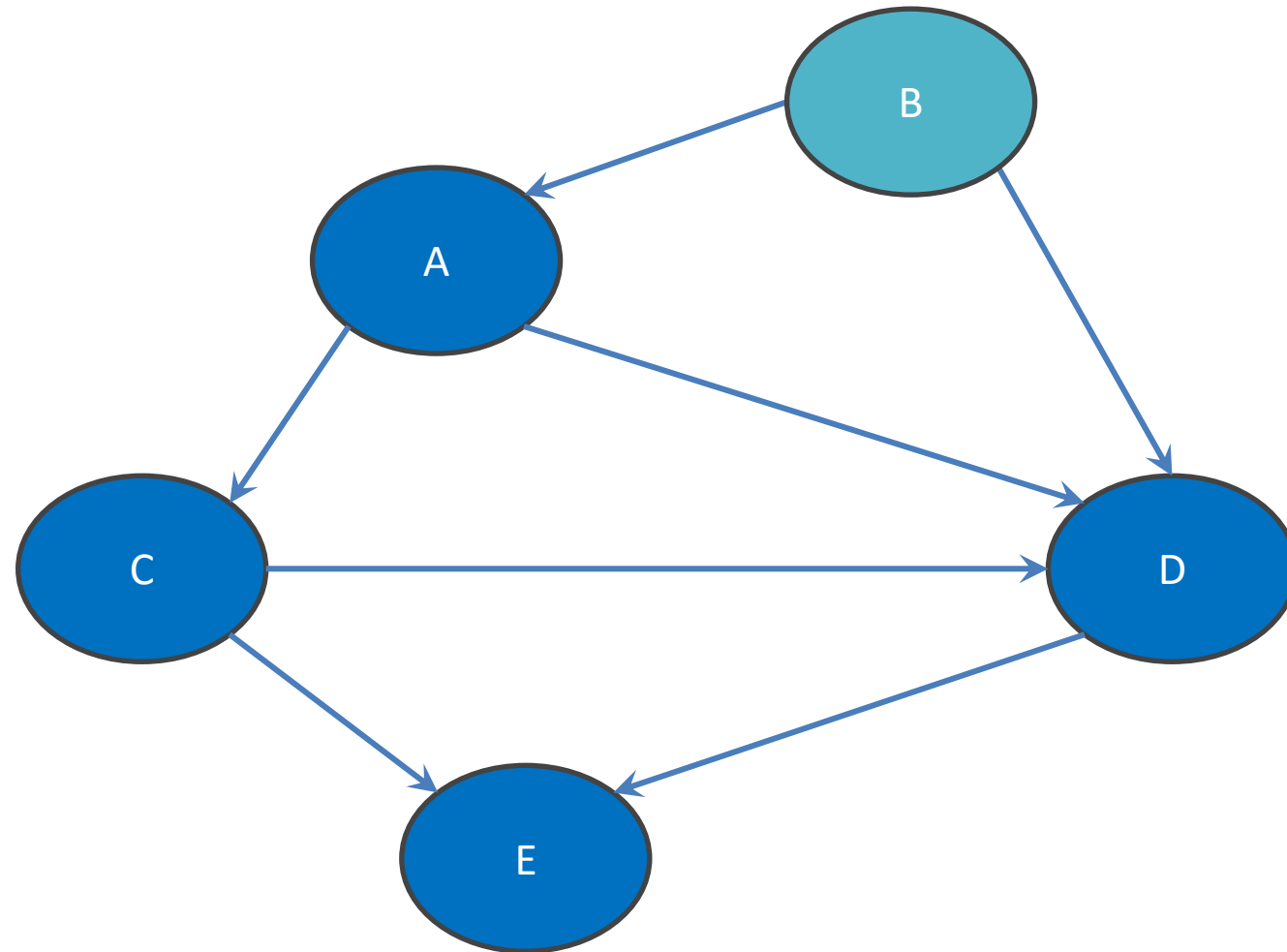
Q: <C, D>

Q: <D>

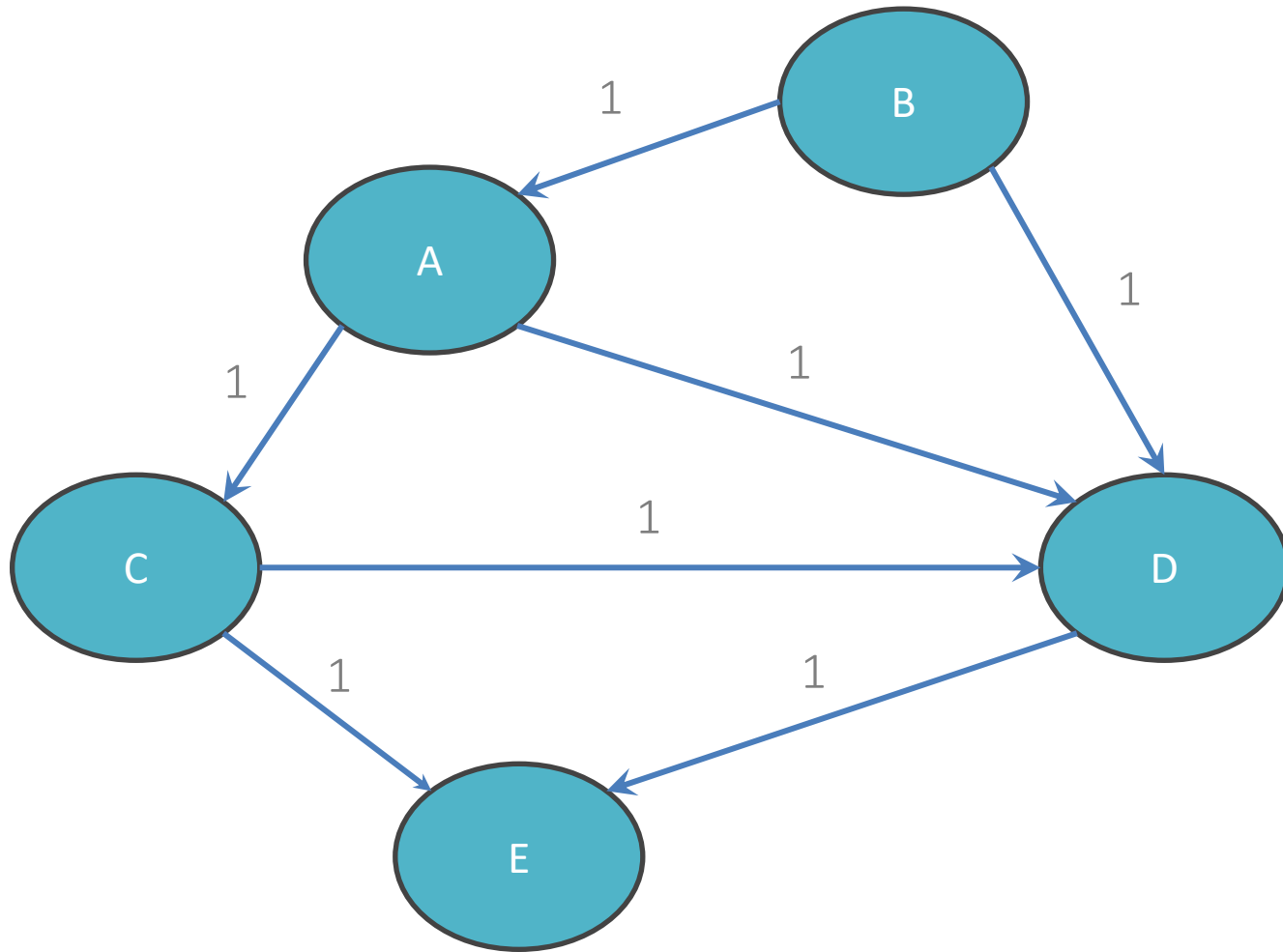
Q: <D, E>

Q: <E>

DONE



Shortest Paths with BFS

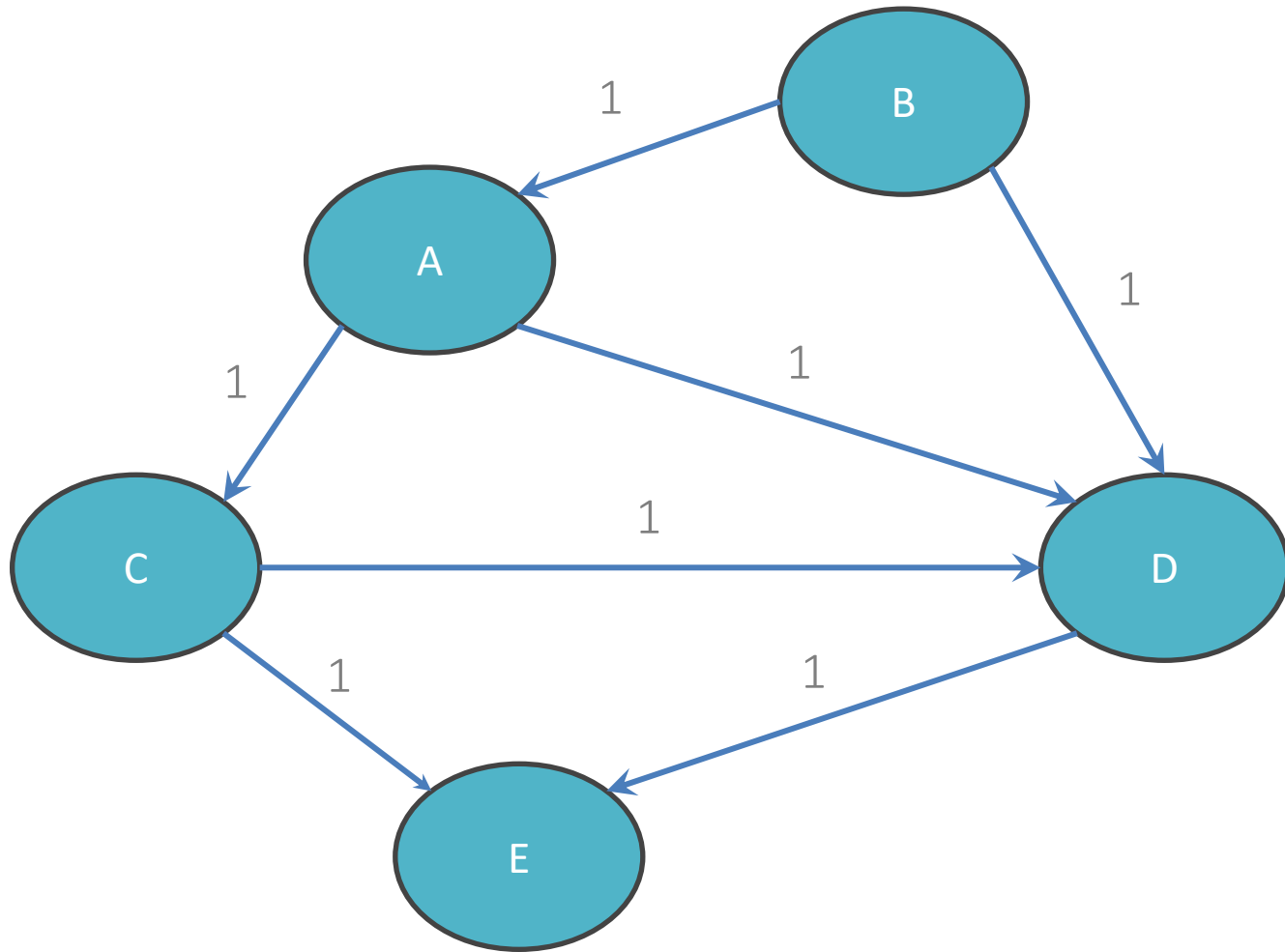


From Node B

Destination	Path	Cost
A	<B,A>	1
B		0
C	<B,A,C>	2
D		
E		

Shortest path to D? to E?
What are the costs?

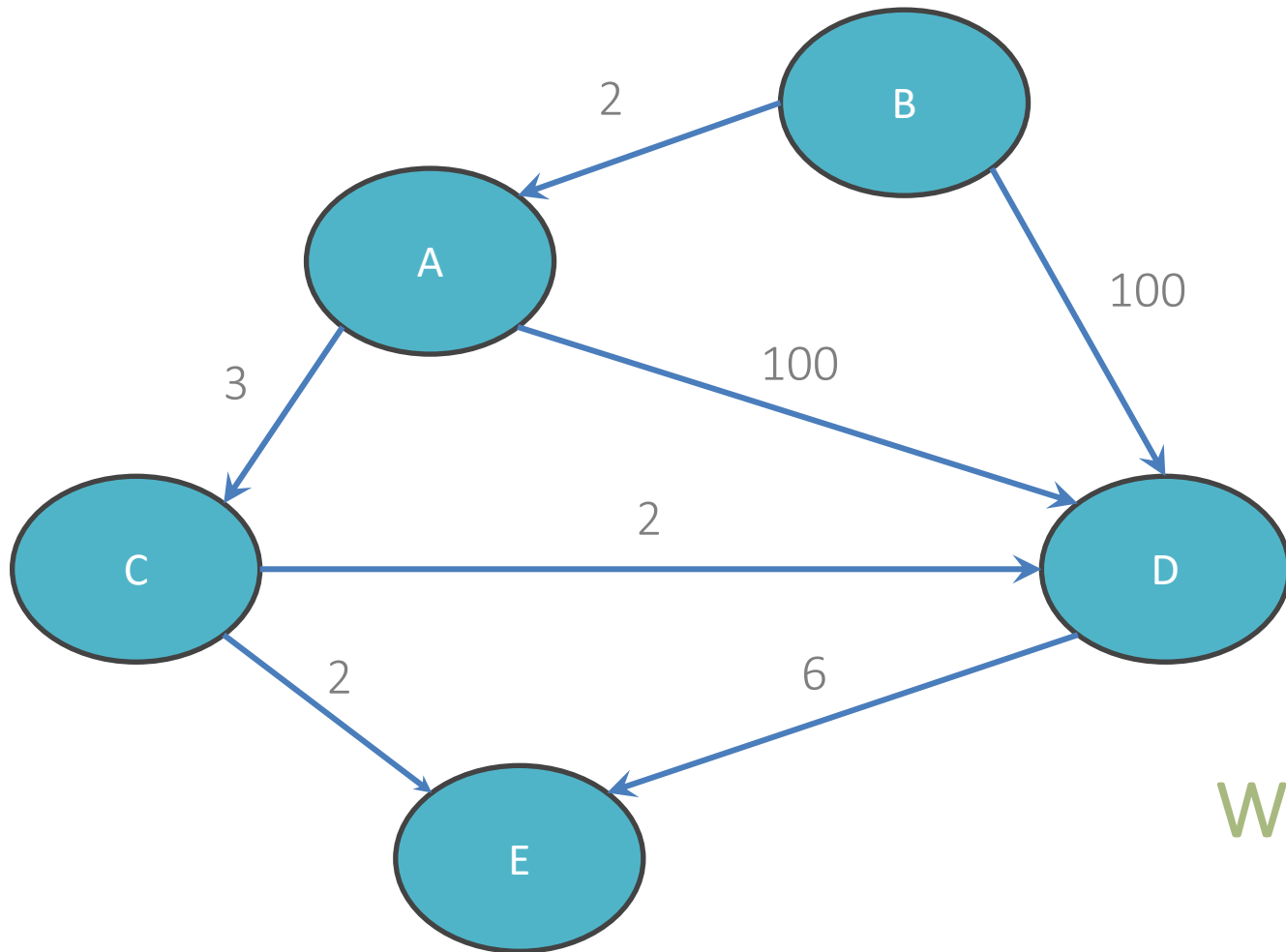
Shortest Paths with BFS



From Node B

Destination	Path	Cost
A	<B,A>	1
B		0
C	<B,A,C>	2
D	<B,D>	1
E	<B,D,E>	2

Shortest Paths with Weights

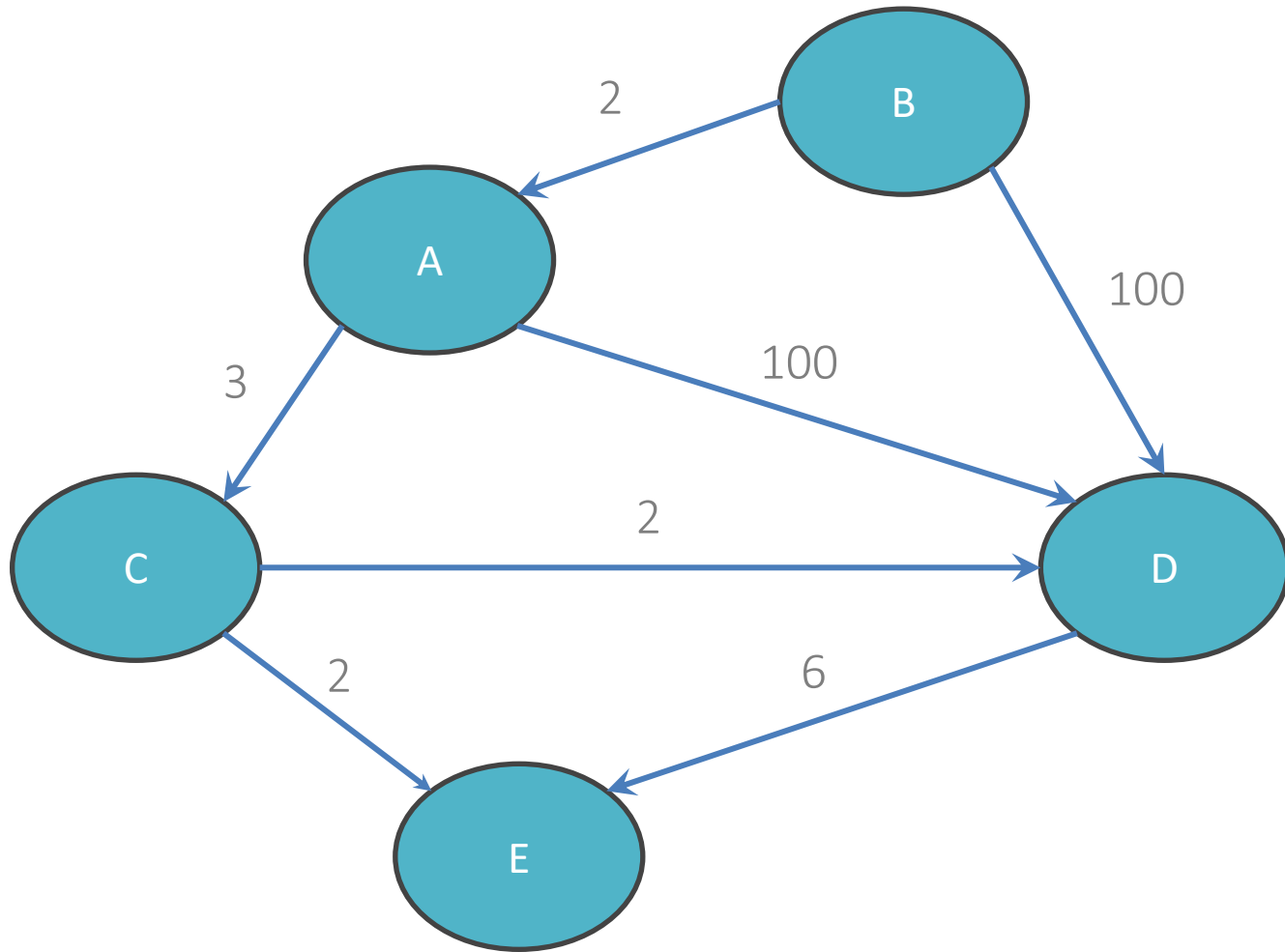


From Node B

Destination	Path	Cost
A	<B,A>	2
B		0
C	<B,A,C>	5
D		
E		

Weights are not the same!
Are the paths?

Shortest Paths with Weights



From Node B

Destination	Path	Cost
A	<B,A>	2
B		0
C	<B,A,C>	5
D	<B,A,C,D>	7
E	<B,A,C,E>	7

Midterm review

Midterm topics

Reasoning about code

Identity & equality

Specification vs. Implementation

Testing

Abstract Data Types (ADTs)

Reasoning about code 1

Using backwards reasoning, find the weakest precondition for each sequence of statements and postcondition below. Insert appropriate assertions in each blank line. You should simplify your answers if possible.

{_____}

`z = x + y;`

{_____}

`y = z - 3;`

{`x > y`}

Reasoning about code 1

Using backwards reasoning, find the weakest precondition for each sequence of statements and postcondition below. Insert appropriate assertions in each blank line. You should simplify your answers if possible.

{_____}

`z = x + y;`

`{x > z - 3}`

`y = z - 3;`

`{x > y}`

Reasoning about code 1

Using backwards reasoning, find the weakest precondition for each sequence of statements and postcondition below. Insert appropriate assertions in each blank line. You should simplify your answers if possible.

$\{x > x + y - 3 \Rightarrow y < 3\}$

$z = x + y;$

$\{x > z - 3\}$

$y = z - 3;$

$\{x > y\}$

Reasoning about code 1

Using backwards reasoning, find the weakest precondition for each sequence of statements and postcondition below. Insert appropriate assertions in each blank line. You should simplify your answers if possible.

{_____}

`p = a + b;`

{_____}

`q = a - b;`

{`p + q = 42`}

Reasoning about code 1

Using backwards reasoning, find the weakest precondition for each sequence of statements and postcondition below. Insert appropriate assertions in each blank line. You should simplify your answers if possible.

{_____}

`p = a + b;`

`{p + a - b = 42}`

`q = a - b;`

`{p + q = 42}`

Reasoning about code 1

Using backwards reasoning, find the weakest precondition for each sequence of statements and postcondition below. Insert appropriate assertions in each blank line. You should simplify your answers if possible.

$$\{a + b + a - b = 42 \Rightarrow a = 21\}$$

$$p = a + b;$$

$$\{p + a - b = 42\}$$

$$q = a - b;$$

$$\{p + q = 42\}$$

Specification vs. Implementation

Suppose we have a `BankAccount` class with instance variable `balance`. Consider the following specifications:

- A. `@effects` decreases `balance` by `amount`
- B. `@requires` `amount >= 0` and `amount <= balance`
`@effects` decreases `balance` by `amount`
- C. `@throws` `InsufficientFundsException`
 if `balance < amount`
`@effects` decreases `balance` by `amount`

Which specifications does this implementation meet?

- I.

```
void withdraw(int amount) {  
    balance -= amount;  
}
```

Another way to ask the question:

If the client does not know the implementation, will the method do what the client expects it to do based on the specification?

Specification vs. Implementation

Suppose we have a `BankAccount` class with instance variable `balance`. Consider the following specifications:

- A. `@effects` decreases `balance` by `amount` ✓ does exactly what the spec says
- B. `@requires` `amount >= 0` and `amount <= balance`
`@effects` decreases `balance` by `amount`
- C. `@throws` `InsufficientFundsException`
 if `balance < amount`
`@effects` decreases `balance` by `amount`

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void withdraw(int amount) {  
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Suppose we have a `BankAccount` class with instance variable `balance`. Consider the following specifications:

- A. `@effects` decreases `balance` by `amount` ✓ does exactly what the spec says
- B. `@requires` `amount >= 0` and `amount <= balance` ✓ If the client follows the `@requires`
 `@effects` decreases `balance` by `amount` precondition, the code will execute as expected
- C. `@throws` `InsufficientFundsException`
 if `balance < amount`
 `@effects` decreases `balance` by `amount`

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```
void withdraw(int amount) {  
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- C. `@throws` `InsufficientFundsException`
 if `balance < amount`
`@effects` decreases `balance` by `amount` ✗ Method never throws an exception

Which specifications does this implementation meet?

```
I. void withdraw(int amount) {  
    balance -= amount;  
}
```

Specification vs. Implementation

Suppose we have a `BankAccount` class with instance variable `balance`. Consider the following specifications:

- A. `@effects` decreases `balance` by `amount`
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- C. `@throws` `InsufficientFundsException`
 if `balance < amount`
`@effects` decreases `balance` by `amount`

Which specifications does this implementation meet?

```
II. void withdraw(int amount) {  
    if (balance >= amount) balance -= amount;  
}
```


Specification vs. Implementation

Suppose we have a `BankAccount` class with instance variable `balance`. Consider the following specifications:

- A. `@effects` decreases `balance` by `amount` ✗ `balance` does not always decrease
- B. `@requires` `amount >= 0` and `amount <= balance`
`@effects` decreases `balance` by `amount`
- C. `@throws` `InsufficientFundsException`
 if `balance < amount`
`@effects` decreases `balance` by `amount`

Which specifications does this implementation meet?

```
II. void withdraw(int amount) {  
    if (balance >= amount) balance -= amount;  
}
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 if `balance < amount`
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Which specifications does this implementation meet?

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 if `balance < amount`
`@effects` decreases `balance` by `amount`

Which specifications does this implementation meet?

```
III. void withdraw(int amount) {  
    if (amount < 0) throw new IllegalArgumentException();  
    balance -= amount;  
}
```

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- C. `@throws` `InsufficientFundsException`
 if `balance < amount`
`@effects` decreases `balance` by `amount`

Which specifications does this implementation meet?

```
III. void withdraw(int amount) {  
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- C. `@throws` `InsufficientFundsException`
 if `balance < amount`
`@effects` decreases `balance` by `amount` ✗ Method throws wrong exception for wrong reason

Which specifications does this implementation meet?

```
III. void withdraw(int amount) {  
    if (amount < 0) throw new IllegalArgumentException();  
    balance -= amount;  
}
```

Specification vs. Implementation

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 if `balance < amount`
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Which specifications does this implementation meet?

```
IV. void withdraw(int amount) throws InsufficientFundsException {  
    if (balance < amount) throw new InsufficientFundsException();  
    balance -= amount;  
}
```


Specification vs. Implementation

Suppose we have a `BankAccount` class with instance variable `balance`. Consider the following specifications:

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- B. `@requires` `amount >= 0` and `amount <= balance`
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- C. `@throws` `InsufficientFundsException`
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Which specifications does this implementation meet?

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- C. `@throws` `InsufficientFundsException`
 if `balance < amount`
`@effects` decreases `balance` by `amount` ✓ Method does what the spec says

Which specifications does this implementation meet?

```
IV. void withdraw(int amount) throws InsufficientFundsException {
    if (balance < amount) throw new InsufficientFundsException();
    balance -= amount;
}
```

Specifications 2

```
/**
 * An IntPoly is an immutable, integer-valued polynomial
 * with integer coefficients. A typical IntPoly value
 * is  $a_0 + a_1x + a_2x^2 + \dots + a_nx_n$ . An IntPoly
 * with degree  $n$  has coefficient  $a_n \neq 0$ , except that the
 * zero polynomial is represented as a polynomial of
 * degree 0 and  $a_0 = 0$  in that case.
 */

public class IntPoly {
    int a[];
    // AF(this) = a has  $n+1$  entries, and for each entry,
    //  $a[i] =$  coefficient  $a_i$  of the polynomial.
}
```

Specifications 2

```
/**  
 * Return a new IntPoly that is the sum of this and other  
 * @requires  
 * @modifies  
 * @effects  
 * @return  
 * @throws  
 */  
public IntPoly add(IntPoly other)
```

Specifications 2

```
/**  
 * Return a new IntPoly that is the sum of this and other  
 * @requires other != null  
 * @modifies none  
 * @effects none  
 * @return a new IntPoly representing the sum of this and other  
 * @throws none  
 */  
public IntPoly add(IntPoly other)
```

Representation invariants

*One of your colleagues is worried that this creates a potential representation exposure problem. Another colleague says there's no problem since an **IntPoly** is immutable. Is there a problem? Give a brief justification for your answer.*

```
public class IntPoly {
    int a[];
    // AF(this) = a has n+1 entries, and for each entry,
    // a[i] = coefficient a_i of the polynomial.

    // Return the coefficients of this IntPoly
    public int[] getCoeffs() {
        return a;
    }
}
```

Representation invariants

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    // Return the coefficients of this IntPoly
    public int[] getCoeffs() {
        return a;
    }
}
```

The return value is a reference to the same coefficient array stored in the **IntPoly** and the client code could alter those coefficients.

Representation invariants

If there is a representation exposure problem, give a new or repaired implementation of `getCoeffs` that fixes the problem but still returns the coefficients of the `IntPoly` to the client. If it saves time you can give a precise description of the changes needed instead of writing the detailed Java code.

```
public class IntPoly {
    int a[];
    // AF(this) = a has n+1 entries, and for each entry,
    // a[i] = coefficient a_i of the polynomial.

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```

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```
public int[] getCoeffs() {  
    int[] copyA = new int[a.length];  
    for (int i = 0; i < copyA.length; i++) {  
        copyA[i] = a[i]  
    }  
    return copyA  
}
```

Representation invariants

If there is a representation exposure problem, give a new or repaired implementation of `getCoeffs` that fixes the problem but still returns the coefficients of the `IntPoly` to the client. If it saves time you can give a precise description of the changes needed instead of writing the detailed Java code.

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    for (int i = 0; i < copyA.length; i++) {  
        copyA[i] = a[i]  
    }  
    return copyA  
}
```

1. Make a copy
2. Return the copy

Representation invariants

If there is a representation exposure problem, give a new or repaired implementation of `getCoeffs` that fixes the problem but still returns the coefficients of the `IntPoly` to the client. If it saves time you can give a precise description of the changes needed instead of writing the detailed Java code.

```
public int[] getCoeffs() {  
    int[] copyA = new int[a.length];  
    for (int i = 0; i < copyA.length; i++) {  
        copyA[i] = a[i]  
    }  
    return copyA  
}
```

1. Make a copy
2. Return the copy

Alternatively, we can just use...
`Arrays.copyOf(a, a.length)`

Reasoning about code 2

*We would like to add a method to this class that evaluates the **IntPoly** at a particular value x . In other words, given a value x , the method **valueAt(x)** should return $a_0 + a_1x + a_2x^2 + \dots + a_nx^n$, where a_0 through a_n are the coefficients of this **IntPoly**.*

For this problem, develop an implementation of this method and prove that your implementation is correct.

(see starter code on next slide)

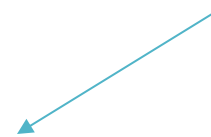
Reasoning about code 2

```
/** Return the value of this IntPoly at point x */
public int valueAt(int x) {
    int val = a[0];
    int xk = 1;
    int k = 0;
    int n = a.length-1; // degree of this, n >=0
    {_____}
    while (k != n) {
        {_____}
        xk = xk * x;
        {_____}
        val = val + a[k+1]*xk;
        {_____}
        k = k + 1;
        {_____}
    }
    {_____}
    return val;
}
```

Reasoning about code 2

```
/** Return the value of this IntPoly at point x */
public int valueAt(int x) {
    int val = a[0];
    int xk = 1;
    int k = 0;
    int n = a.length-1; // degree of this, n >=0
    {inv: xk = x^k && val = a[0] + a[1]*x + ... + a[k]*x^k}
    while (k != n) {
        {_____}
        xk = xk * x;
        {_____}
        val = val + a[k+1]*xk;
        {_____}
        k = k + 1;
        {_____}
    }
    {_____}
    return val;
}
```

This should come with the code...



Reasoning about code 2

```
/** Return the value of this IntPoly at point x */
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    int val = a[0];
    int xk = 1;
    int k = 0;
    int n = a.length-1; // degree of this, n >=0
    {inv: xk = x^k && val = a[0] + a[1]*x + ... + a[k]*x^k}
    while (k != n) {
        {inv && k != n}
        xk = xk * x;
        {_____}
        val = val + a[k+1]*xk;
        {_____}
        k = k + 1;
        {_____}
    }
    {_____}
    return val;
}
```


Reasoning about code 2

```
/** Return the value of this IntPoly at point x */
public int valueAt(int x) {
    int val = a[0];
    int xk = 1;
    int k = 0;
    int n = a.length-1; // degree of this, n >=0
    {inv:  $xk = x^k$  &&  $val = a[0] + a[1]*x + \dots + a[k]*x^k$ }
    while (k != n) {
        {inv &&  $k \neq n$ }
        xk = xk * x;
        { $xk = x^{(k+1)}$  &&  $val = a[0] + a[1]*x + \dots + a[k]*x^k$ }
        val = val + a[k+1]*xk;
        {_____}
        k = k + 1;
        {_____}
    }
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    return val;
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        { $xk = x^{(k+1)} \ \&\& \ val = a[0] + a[1]*x + \dots + a[k+1]*x^{(k+1)}$ }
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        val = val + a[k+1]*xk;
        {xk = x^(k+1) && val = a[0] + a[1]*x + ... + a[k+1]*x^(k+1)}
        k = k + 1;
        {inv}
    }
    {inv && k = n ⇒ val = a[0] + a[1]*x + ... + a[n]*x^n}
    return val;
}
```

Equality

*Suppose we are defining a class **StockItem** to represent items stocked by an online grocery store. Here is the start of the class definition, including the class name and instance variables:*

```
public class StockItem {  
    String name;  
    String size;  
    String description;  
    int quantity;  
  
    /* Construct a new StockItem */  
    public StockItem(...);  
}
```

Equality

A summer intern was asked to implement an `equals` function for this class that treats two `StockItem` objects as equal if their `name` and `size` fields match. Here's the result:

```
/** return true if the name and size fields match */  
public boolean equals(StockItem other) {  
    return name.equals(other.name) && size.equals(other.size);  
}
```

This `equals` method seems to work sometimes but not always. Give an example showing a situation when it fails.

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```
Object s1 = new StockItem("thing", 1, "stuff", 1);  
Object s2 = new StockItem("thing", 1, "stuff", 1);  
System.out.println(s1.equals(s2));
```

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/** return true if the name and size fields match */  
public boolean equals(StockItem other) { // equals is overloaded, not overridden  
    return name.equals(other.name) && size.equals(other.size);  
}
```

This `equals` method seems to work sometimes but not always. Give an example showing a situation when it fails.

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Object s1 = new StockItem("thing", 1, "stuff", 1);  
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Equality

Show how you would fix the `equals` method so it works properly (`StockItems` are equal if their names and `sizes` are equal)

```
/** return true if the name and size fields match */
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Equality

Show how you would fix the `equals` method so it works properly (`StockItems` are equal if their names and `sizes` are equal)

```
/** return true if the name and size fields match */  
@Override  
public boolean equals(Object o) {  
    if (!(o instanceof StockItem)) {  
        return false;  
    }  
    StockItem other = (StockItem) o;  
    return name.equals(other.name) && size.equals(other.size);  
}
```

hashCode

Which of the following implementations of `hashCode()` for the `StockItem` class are legal:

1. `return name.hashCode();`
2. `return name.hashCode() * 17 + size.hashCode();`
3. `return name.hashCode() * 17 + quantity;`
4. `return quantity;`

hashCode

Which of the following implementations of hashCode() for the StockItem class are legal:

1. `return name.hashCode();` ✓ legal
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3. `return name.hashCode() * 17 + quantity;` ✗ illegal!
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2. `return name.hashCode() * 17 + size.hashCode();` ✓ legal
3. `return name.hashCode() * 17 + quantity;` ✗ illegal!
4. `return quantity;` ✗ illegal!

The `equals` method does not care about `quantity`

hashCode

Which implementation do you prefer?

```
public int hashCode() {  
    return name.hashCode();  
}
```

```
public int hashCode() {  
    return name.hashCode()*17 + size.hashCode();  
}
```

hashCode

Which implementation do you prefer?

```
public int hashCode() {  
    return name.hashCode();  
}
```

```
public int hashCode() {  
    return name.hashCode()*17 + size.hashCode();  
}
```

(ii) will likely do the best job since it takes into account both the size and name fields. (i) is also legal but it gives the same **hashCode** for **StockItems** that have different sizes as long as they have the same name, so it doesn't differentiate between different **StockItems** as well as (ii).