

CSE 331 21au Section 5 Worksheet

Consider the following class `IntStack`:

```
/* IntStack is a LIFO stack of integers with a fixed capacity.
 * The most recently added integer is the first to be removed.
 */
public class IntStack {
    private int[] vals; // stack
    private int top;    // top

    public IntStack(int capacity) {
        vals = new int[capacity];
        top = 0;
    }

    public boolean push(int x) {
        if (top == vals.length)
            return false;
        vals[top] = x;
        top++;
        return true;
    }

    public int pop() {
        if (top == 0)
            throw new NoSuchElementException();
        top--;
        return vals[top];
    }

    public int size() {
        return top;
    }
}
```

1. What might the rep invariant for this class be? What about the abstraction function?

`vals` is not null, $0 \leq \text{top} \leq \text{vals.length}$, and for $0 \leq k < \text{top}$, `vals[k]` has been initialized with stack elements. Note: it would be incorrect to say that `vals[k]` is not null, since `int` values cannot be null – they are not references.

`vals[0..top-1]` represents the stack of values, where `vals[0]` is the bottom element of the stack (`s0`), `vals[top-1]` is the top element on the stack (`sn`), and `top` is the number of items on the stack. If `top=0`, the stack is empty.

CSE 331 21au Section 5 Worksheet

2. Consider the following two classes. Write an RI and AF for the Sequence class.

```
class IntPair {
    int num;
    int count;
    public IntPair(int n, int c) { num = n; count = c; }
}
/* Sequence represents a non-decreasing sequence of ints. Numbers
 * can only be added to the end of the sequence.
 */
public class Sequence {
    private List<IntPair> list;
    private int length;

    public Sequence(int i) {
        list = new ArrayList<IntPair>();
        list.add(new IntPair(i, 1));
        length = 1;
    }

    public boolean add(int x) {
        int max = list.get(list.size() - 1).num;
        if (x < max) {
            return false;
        } else if (x == max) {
            list.get(list.size() - 1).count += 1;
        } else {
            list.add(new IntPair(x, 1));
        }
        length++;
        return true;
    }

    public int get(int i) { // exclude bound checks
        int j = -1;
        while (i >= 0) {
            j++;
            i -= list.get(j).count;
        }
        return list.get(j).num;
    }

    public int getCount(int n) {
        for (int i = 0; i < list.size(); i++) {
            if (list.get(i).num == n) {
                return list.get(i).count;
            } else if (list.get(i).num > n) {
                return 0;
            }
        }
        return 0;
    }
}
```

CSE 331 21au Section 5 Worksheet

list is sorted by `IntPair.num`, each element of list has a unique `IntPair.num`

list is not null

for each element `list.get(i)`, `list.get(i) != null` and `list.get(i).count > 0`

`length = sum of list.get(i).count for all $0 \leq i < list.size()$`

`list.get(i).num` represents the *i*th distinct integer appearing in the sequence, where

`list.get(i).count` is the number of times it appears in the sequence

`length` is the number of integers in the non-decreasing sequence