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# CSE 331

## Software Design & Implementation

Topic: Rep. Exposure; Abstraction Functions

🗨 **Discussion:** Any plans for the July 4<sup>th</sup> holiday?

# Reminders

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- Tomorrow is a national holiday!
  - Won't hold Tanay's office hours
- Slight delay in HW2 grading

# Upcoming Deadlines

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- Prep. Quiz: HW3                      due Monday (7/3)
- HW3                                      due Thursday (7/6)

## Last Time...

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- Abstract Data Types
- ADTs in Java
  - overview
  - abstract state
  - creators
  - observers
  - producers
  - mutators
- Representation Invariants

## Today's Agenda

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- Representation Exposure
- Abstraction Functions
- Intro to Testing

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# Recap: ADTs and RIs

# Abstract Data Type (ADT)

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ADT abstracts from the *organization* to *meaning* of data

- details of data structures are hidden from the client
- allows us to *delay* decisions about data structures

Often best to start your design by designing data

- first, what **operations** will be permitted on the data (for clients)
- next, decide how data be **organized** (data structures)
  - see CSE 332 & CSE 344
- lastly, write the **code**

Then use **reasoning** to verify the operations are correct

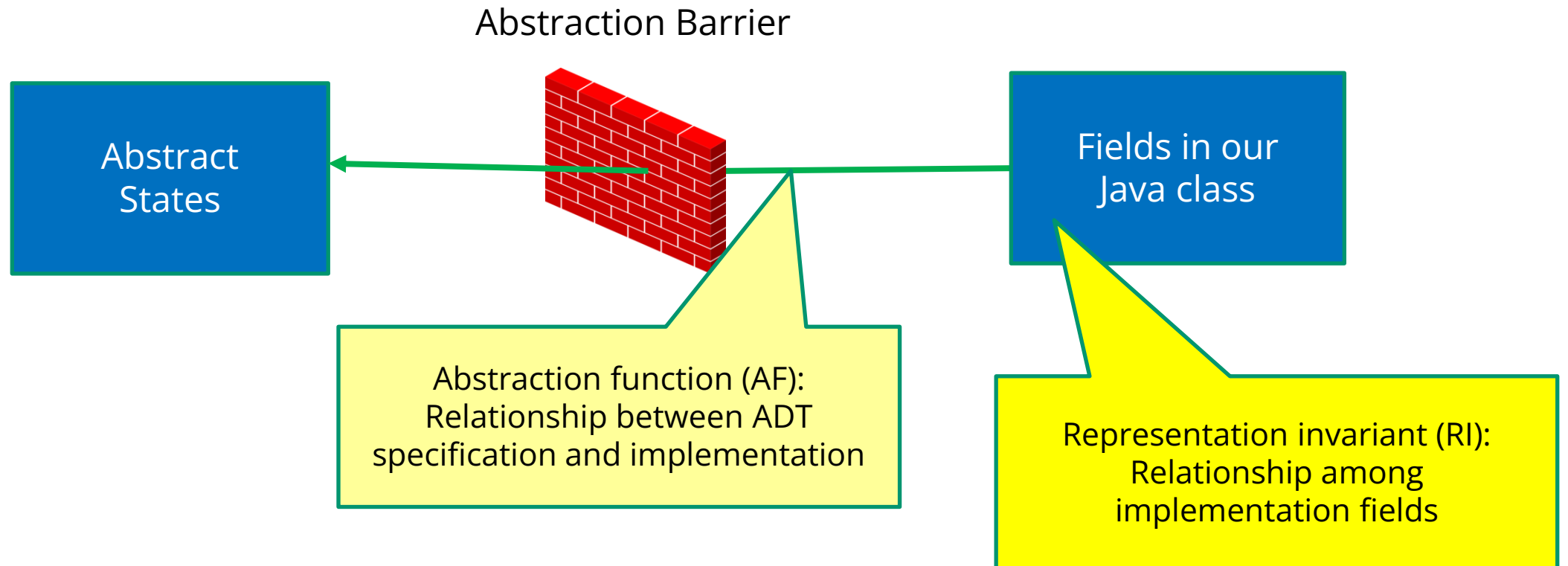
- two intellectual tools are helpful for this...

# Data abstraction outline

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## ADT specification

## ADT implementation



# Connecting implementations to specs

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**For implementers / debuggers / maintainers of the implementation:**

***Representation Invariant***: maps Object  $\rightarrow$  boolean

- defines the set of valid concrete values
- **no object should ever violate the rep invariant**
  - such an object has no useful meaning

***Abstraction Function***: maps Object  $\rightarrow$  abstract state

- we'll discuss this later today!

# Example: Circle 2

---

```
/** Represents a mutable circle in the plane. For example,  
 * it can be a circle with center (0,0) and radius 1. */  
public class Circle {  
  
    // Rep invariant: center != null and edge != null  
    //   and !center.equals(edge)  
    private Point center, edge;  
  
    // Abstraction function:  
    // AF(this) = a circle with center at this.center  
    //   and radius this.center.distanceTo(this.edge)  
  
    // ...  
}
```



# Example: Polynomial 2

---

```
/** An immutable polynomial with integer coefficients.
 * Examples include 0, 2x, and x + 3x^2 + 5x. */
public class IntPoly {

    // Rep invariant: terms != null and
    //     no two terms have the same degree and
    //     terms is sorted in descending order by degree
    private final LinkedList<IntTerm> terms;

    // Abstraction function:
    // AF(this) = sum of monomials in this.terms

    // ... coeff, degree, etc.
```

---

# Defensive Programming with ADTs

# Checking rep invariants

---

Should you write code to check that the rep invariant holds?

# Checking rep invariants

---

Should you write code to check that the rep invariant holds?

- Yes, if it's inexpensive [same as preconditions]

# Checking rep invariants

---

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- Yes, if it's inexpensive [same as preconditions]
- Yes, for debugging [even when it's expensive]

# Checking rep invariants

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Should you write code to check that the rep invariant holds?

- Yes, if it's inexpensive [same as preconditions]
- Yes, for debugging [even when it's expensive]

Often hard to justify turning the safety checks off...

- make the code run faster (rare)
- make the code easier to understand

# Checking rep invariants

---

Should you write code to check that the rep invariant holds?

- Yes, if it's inexpensive [same as preconditions]
- Yes, for debugging [even when it's expensive]

Often hard to justify turning the safety checks off...

- make the code run faster (rare)
- make the code easier to understand

**Where should you check that the rep invariant holds?**

# Example: String

---

```
public class String {  
  
    // Rep invariant: arr != null  
    private char[] arr;  
  
    // Some operations supported by the ADT  
    public bool isEmpty() { return arr.length() == 0; }  
    public bool startsWith(char c) { return arr[0] == c; }  
    public void yikes() { arr = null; }  
}
```



# Checking rep invariants

---

Since representation invariants hold before and after each method in the public specification, we can introduce a great debugging technique:

*Catch bugs by implementing and using a function to check the rep. invariant*

Note: only needed for public methods.

# Example: CharSet ADT

---

```
// Overview: A CharSet is a finite mutable set of Characters
// @effects: creates a fresh, empty CharSet
public CharSet() {...}

// @modifies: this
// @effects: this changed to this + {c}
public void insert(Character c) {...}

// @modifies: this
// @effects: this changed to this - {c}
public void delete(Character c) {...}

// @return: true iff c is in this set
public boolean member(Character c) {...}

// @return: cardinality of this set
public int size() {...}
```

# Example: CharSet Representation

---

```
// Rep invariant: elts != null and  
//             elts has no nulls and no dups  
private List<Character> elts;
```

# Checking the rep invariant

---

How do we check whether this invariant holds?

```
public void delete(Character c) {  
  
    elts.remove(c); // removes 0 or 1 copies of c  
  
}
```

# Checking the rep invariant

---

Rule of thumb: check on entry *and* on exit (why?)

```
public void delete(Character c) {
    checkRep();
    elts.remove(c); // removes 0 or 1 copies of c
    checkRep();
}

// Verify that elts contains no nulls or dups
private void checkRep() {
    assert elts != null;
    for (int i = 0; i < elts.size(); i++) {
        assert elts.get(i) != null;
        assert elts.indexOf(elts.get(i)) == i;
    }
}
```

# Practice *defensive programming*

---

- Question is not: will you make mistakes? You will.
- Question is: will you **catch** those mistakes before users do?
- Write and incorporate code designed to catch the errors you make
  - check rep invariant on entry (of mutators)
  - check rep invariant on exit (of mutators and creators)
  - check preconditions (don't trust other programmers)
  - check postconditions (don't trust yourself either)
- Checking the rep invariant helps *discover* errors while testing
- Reasoning about the rep invariant helps *discover* errors while coding

# Practice *defensive programming*

---

Focus on defensive programming against **subtle bugs**

- obvious bugs (e.g., crashing every time) will be caught in testing
- subtle bugs that only occasionally cause problems can sneak out
- be especially defensive against (and scared of) these

# Listing the elements of a CharSet

---

Consider adding the following method to `CharSet`

```
// returns: a List containing the members of this  
public List<Character> getElts();
```

Consider this implementation:

```
public List<Character> getElts() { return elts; }
```

Does this implementation preserve the rep invariant?

***Can't say!***



# Representation exposure

---

Consider this client code (outside the `CharSet` implementation):

```
CharSet s = new CharSet();  
Character a = new Character('a');  
  
s.insert(a);  
List<Character> elts = s.getElts();  
s.delete(a);  
bool isMember = s.member(a);
```

We expect that `isMember` is false.

# Representation exposure

---

Consider this client code (outside the `CharSet` implementation):

```
CharSet s = new CharSet();  
Character a = new Character('a');  
  
s.insert(a);  
s.insert(a);  
List<Character> elts = s.getElts();  
s.delete(a);  
bool isMember = s.member(a);
```

We *still* expect that `isMember` is false.

# Representation exposure

---

Consider this client code (outside the `CharSet` implementation):

```
CharSet s = new CharSet();  
Character a = new Character('a');  
  
s.insert(a);  
s.insert(a);  
List<Character> elts = s.getElts();  
s.delete(a);  
bool isMember = s.member(a);
```

We *still* expect that `isMember` is false.

# Representation exposure

---

Consider this client code (outside the `CharSet` implementation):

```
CharSet s = new CharSet();
Character a = new Character('a');

s.insert(a);
List<Character> elts = s.getElts();
elts.add(a); // yikes!
s.delete(a);
bool isMember = s.member(a);
```

- Suddenly, we see that `isMember` is true.
- [Representation exposure](#) is allowing clients to access the internal rep

# Avoiding representation exposure

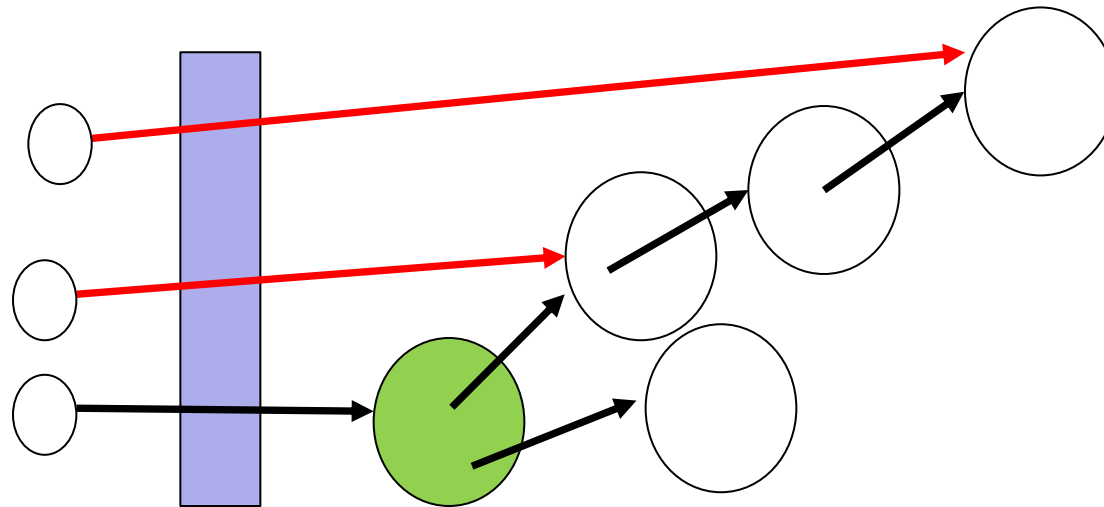
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- *Understand* what representation exposure is
- *Design* ADT implementations to make sure it doesn't happen
- Treat rep exposure as a bug: *fix* your bugs
  - absolutely must avoid in libraries with many clients
- *Test* for it with *adversarial clients*:
  - pass values to methods and then mutate them
  - mutate values returned from methods

# private is not enough

---

- Making fields **private** does *not* suffice to prevent rep exposure
  - see our example
  - issue is *aliasing of mutable data outside the abstraction*



- So **private** is a hint to you: no aliases outside abstraction to references to mutable data reachable from **private** fields
- Three general ways to avoid representation exposure...

# Avoiding rep exposure (way #1)

---

- One way to avoid rep exposure is to make **copies** of all data that cross the abstraction barrier
  - Copy in [parameters that become part of the implementation]
  - Copy out [results that are part of the implementation]
- Examples of copying (assume **Point** is a mutable ADT):

```
class Line {
    private Point s, e;
    public Line(Point s, Point e) {
        this.s = new Point(s.x, s.y);
        this.e = new Point(e.x, e.y);
    }
    public Point getStart() {
        return new Point(this.s.x, this.s.y);
    }
}
```

...

# Avoiding rep exposure (way #2)

---

- One way to avoid rep exposure is to exploit the **immutability** of (other) ADTs the implementation uses
  - aliasing is no problem if nobody can change data
    - have to mutate the rep to break the rep invariant

- Examples (assuming `Point` is an *immutable* ADT):

```
class Line {
    private Point s, e;
    public Line(Point s, Point e) {
        this.s = s;
        this.e = e;
    }
    public Point getStart() {
        return this.s;
    }
}
```

...



# Alternative #3

---

```
// returns: elts currently in the set
public List<Character> getElts() { // version 1
    return new ArrayList<Character>(elts); //copy out!
}

public List<Character> getElts() { // version 2
    return Collections.unmodifiableList(elts);
}
```

From the JavaDoc for `Collections.unmodifiableList`:

*Returns an unmodifiable view of the specified list. This method allows modules to provide users with "read-only" access to internal lists. Query operations on the returned list "read through" to the specified list, and attempts to modify the returned list... result in an **UnsupportedOperationException**.*

# The good news

---

```
public List<Character> getElts() { // version 2
    return Collections.unmodifiableList(elts);
}
```

- Clients cannot *modify (mutate)* the rep
  - cannot break the rep invariant
- (For long lists) more efficient than copy out
- Uses standard libraries

# The bad news

---

```
public List<Character> getElts() { // version 1
    return new ArrayList<Character>(elts); //copy out!
}
```

```
public List<Character> getElts() { // version 2
    return Collections.unmodifiableList(elts);
}
```

The two implementations do not do the same thing!

- both avoid allowing clients to break the rep invariant
- both return a list containing the elements

But consider:

```
xs = s.getElts();
s.insert('a');
xs.contains('a');
```

Version 2 is *observing* an exposed rep, leading to different behavior

# Different specifications

---

Ambiguity of “returns a list containing the current set elements”

“returns a fresh mutable list containing the elements in the set *at the time of the call*”

vs.

“returns read-only access to a list that the ADT *continues to update to hold the current elements in the set*”

A third spec weaker than both [but less simple and useful!]

“returns a list containing the current set elements. *Behavior is unspecified (!) if client attempts to mutate the list or to access the list after the set’s elements are changed*”

Also note: Version 2’s spec also makes changing the rep later harder

- only “simple” to implement with rep as a **List**

# Suggestions

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Best options for implementing `getElt()`

- if  $O(n)$  time is acceptable for relevant use cases, copy the list
  - safest option
  - best option for changeability
- if  $O(1)$  time is required, then return an unmodifiable list
  - prevents breaking rep invariant
  - clearly document that behavior is unspecified after mutation
  - ideally, write your own unmodifiable view of the list that throws an exception on all operations after mutation
- if  $O(1)$  time is required and there is no unmodifiable version and you don't have time to write one, expose rep and feel very, very guilty

---

# Abstraction Functions

# Specifying an ADT

---

Different types of operations:

1. **creators**
2. **observers**
3. **producers**
4. **mutators** (if mutable)

Described in terms of how they change the **abstract state**

- abstract description of what the object means
  - difficult (unless concept is already familiar) but vital
- specs have no information about concrete representation
  - leaves us free to change those in the future

# Connecting implementations to specs

---

**For implementers / debuggers / maintainers of the implementation:**

***Representation Invariant***: maps Object  $\rightarrow$  boolean

- we saw this earlier!

***Abstraction Function***: maps Object  $\rightarrow$  abstract state

- says what the data structure *means* in vocabulary of the ADT
- maps the fields to the abstract state they represent
  - can check that the abstract value after each method meets the postcondition described in the specification



# Example: Circle

---

```
/** Represents a mutable circle in the plane. For example,  
 * it can be a circle with center (0,0) and radius 1. */  
public class Circle {  
  
    // Rep invariant: center != null and rad > 0  
    private Point center;  
    private double rad;  
  
    // Abstraction function:  
    // AF(this) = a circle with center at this.center  
    //   and radius this.rad  
  
    // ...  
}
```

# Example: Circle 2

---

```
/** Represents a mutable circle in the plane. For example,  
 * it can be a circle with center (0,0) and radius 1. */  
public class Circle {  
  
    // Rep invariant: center != null and edge != null  
    //   and !center.equals(edge)  
    private Point center, edge;  
  
    // Abstraction function:  
    // AF(this) = a circle with center at this.center  
    //   and radius this.center.distanceTo(this.edge)  
  
    // ...  
}
```

# Example: Polynomial

---

```
/** An immutable polynomial with integer coefficients.
 * Examples include 0, 2x, and x + 3x^2 + 5x. */
public class IntPoly {

    // Rep invariant: coeffs != null
    private final int[] coeffs;

    // Abstraction function:
    // AF(this) = sum of this.coeffs[i] * x^i
    //   for i = 0 .. this.coeffs.length

    // ... coeff, degree, etc.
```

# Example: Polynomial 2

---

```
/** An immutable polynomial with integer coefficients.
 * Examples include 0, 2x, and x + 3x^2 + 5x. */
public class IntPoly {

    // Rep invariant: terms != null and
    //     no two terms have the same degree and
    //     terms is sorted in descending order by degree
    private final LinkedList<IntTerm> terms;

    // Abstraction function:
    // AF(this) = sum of monomials in this.terms

    // ... coeff, degree, etc.
```

# The abstraction function

---

- Purely conceptual (not a Java function)
- Allows us to check correctness
  - use reasoning to show that the method leaves the abstract state such that it satisfies the postcondition

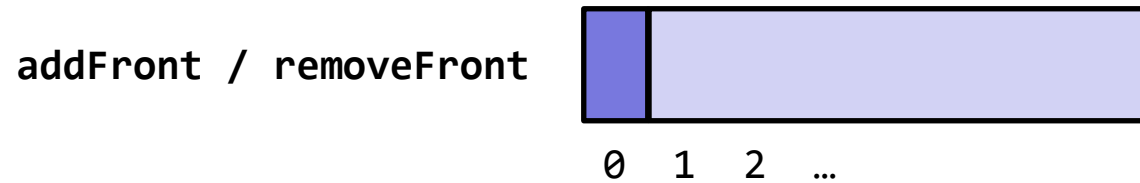
# Example: IntDeque

---

// List that only allows insert/remove at ends.



**addLast / removeLast**



**addFront / removeFront**

# Example: IntDeque

---

// List that only allows insert/remove at ends.

**addLast**



**removeFront**



# Example: IntDeque

---

// List that only allows insert/remove at ends.



**addLast + removeFront**



**addLast + removeFront**



**addLast + removeFront**

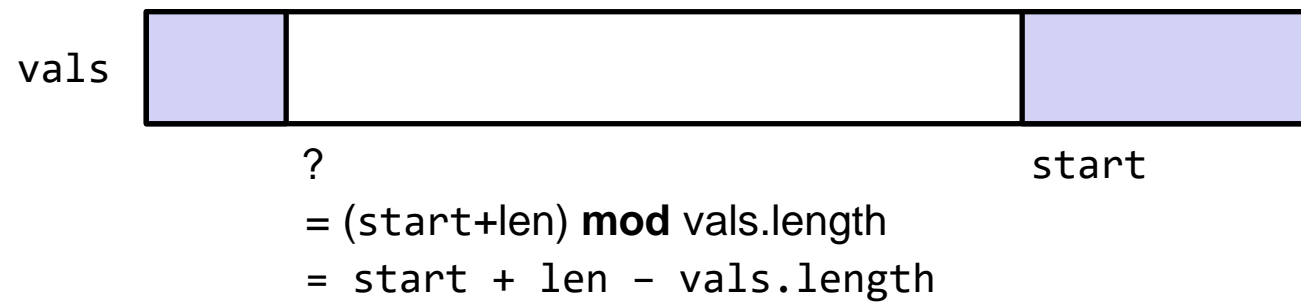
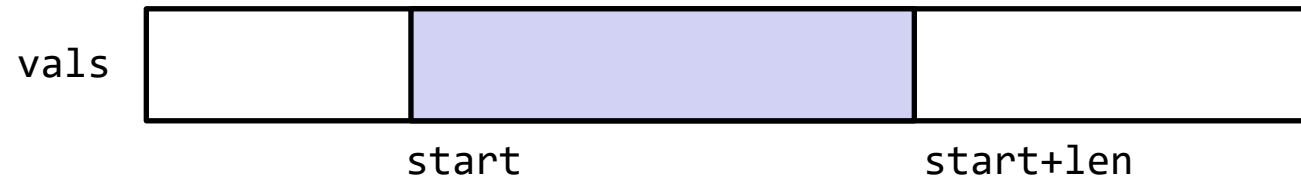




# Example: IntDeque

---

```
// List that only allows insert/remove at ends.
```



# Example: IntDeque

---

```
/** List that only allows insert/remove at ends. */
public class IntDeque {

    // AF(this) =
    //   vals[start..start+len-1]    if start+len <= vals.length
    //   vals[start..] + vals[0..?]  otherwise
    private int[] vals;
    private int start, len;

    // Creates an empty list.
    public IntDeque() {
        vals = new int[3];
        start = len = 0;
    }
}
```

← AF(this) = vals[0..-1] = []

# Example: IntDeque

---

```
/** List that only allows insert/remove at ends. */
public class IntDeque {

    // AF(this) =
    //   vals[start..start+len-1]    if start+len <= vals.length
    //   vals[start..] + vals[0..?]  otherwise
    private int[] vals;
    private int start, len;

    // ...

    // @return length of the list
    public int getLength() {
        return len;
    }
}
```

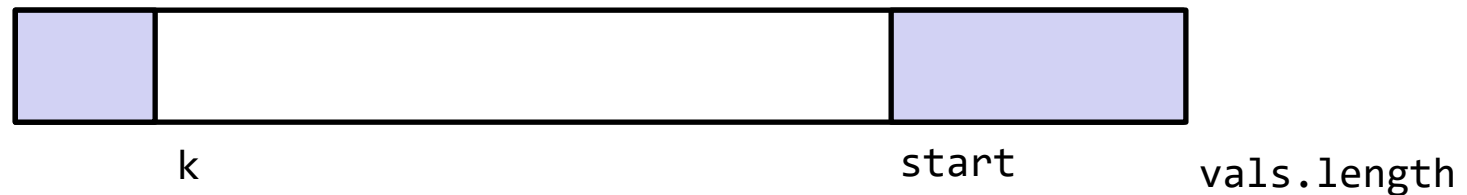
# Example: IntDeque

---

```
// List that only allows insert/remove at ends.
```



#items = len



#items = vals.length - (start - k) (= len?)

**holds iff**  $k = \text{start} + \text{len} - \text{vals.length}$

# Example: IntDeque

---

```
/** List that only allows insert/remove at ends. */
```

```
public class IntDeque {
```

```
    // AF(this) =
```

```
    //    vals[start..start+len-1]    if start+len <= vals.length
```

```
    //    vals[start..] + vals[0..k]  otherwise
```

```
    private int[] vals;
```

```
    private int start, len;
```

```
    // ...
```

```
    // @return length of the list
```

```
    public int getLength() {
```

```
        return len;
```

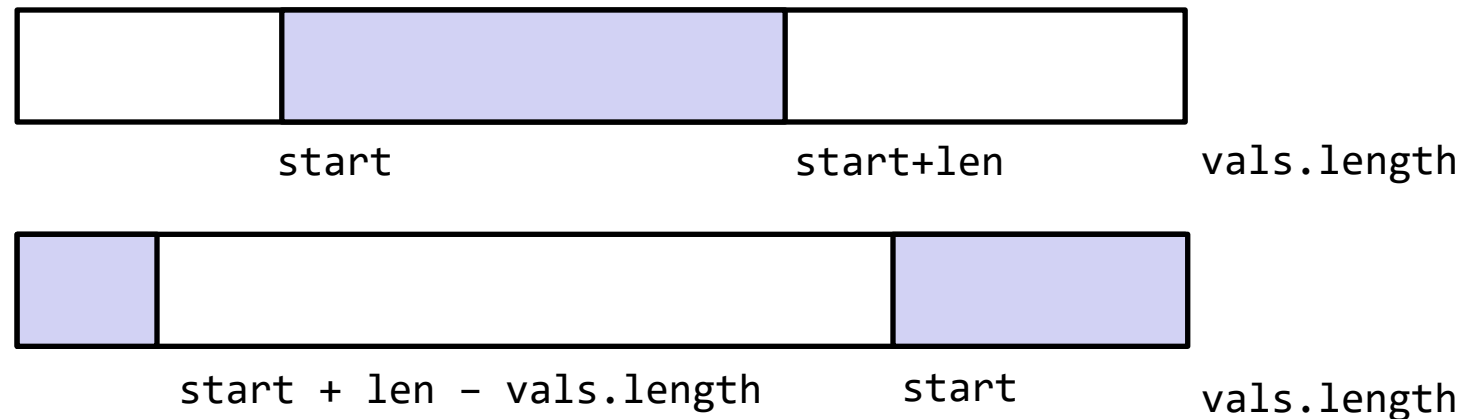
```
    }
```

**1 line of code  
but 2 cases for reasoning**

# Example: IntDeque

---

```
/** List that only allows insert/remove at ends. */  
public class IntDeque {  
  
    // @requires 0 <= i < length  
    // @return this[i]  
    public int get(int i) { ... }  
}
```



# Example: IntDeque

---

```
/** List that only allows insert/remove at ends. */
public class IntDeque {

    // @requires 0 <= i < length
    // @return this[i]
    public int get(int i) {
        if (start + len <= vals.length) {
            return vals[start + i];
        } else {
            return vals[(start + i) % vals.length];
        }
    }
}
```

# Example: IntDeque

---

```
/** List that only allows insert/remove at ends. */  
public class IntDeque {  
  
    // @requires 0 <= i < length  
    // @return this[i]  
    public int get(int i) {  
        return vals[(start + i) % vals.length];  
    }  
}
```



# Example: IntDeque

---

```
/** List that only allows insert/remove at ends. */  
public class IntDeque {  
  
    // @requires list length > 0  
    // @modifies this  
    // @effects first element of list is removed  
    // @return value at the front of the list  
    public int removeFront() { ... }
```

# Example: IntDeque

---

```
// List that only allows insert/remove at ends.
```



**removeFront**



# Example: IntDeque

---

```
// AF(this) =  
//   vals[start..start+len-1]   if start+len <= vals.length  
//   vals[start..] + vals[0..k] otherwise  
  
// @requires list length > 0  
// @modifies this  
// @effects first element of list is removed  
public void removeFront() {  
    if (start + 1 < vals.length) {  
        start += 1;  
    } else {  
        start = 0;  
    }  
    len -= 1;  
}
```

# Example: IntDeque

---

```
// AF(this) =  
//   vals[start..start+len-1]   if start+len <= vals.length  
//   vals[start..] + vals[0..k] otherwise  
  
// @requires list length > 0  
// @modifies this  
// @effects first element of list is removed  
public void removeFront() {  
    start = (start + 1) % vals.length;  
    len -= 1;  
}
```

# Example: IntDeque

---

```
// AF(this) =  
//   vals[start..start+len-1]    if start+len <= vals.length  
//   vals[start..] + vals[0..k]  otherwise  
  
// @requires list length > 0  
// @modifies this  
// @effects first element of list is removed  
// @return value at the front of the list  
public int removeFront() {  
    int val = get(0);  
    start = (start + 1) % vals.length;  
    len -= 1;  
    return val;  
}
```

# Before next class...

---

1. Start on [Prep. Quiz: HW3](#) as early as possible!
  - Reminds you about common base operations
2. Enjoy the holiday!

# Extra: Abstract Interpretation

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- Abstraction functions are good for much more (e.g. program analysis)

# Extra: Testing

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- What is testing? What makes something a good test case?