CSE 332 Winter 2024 Lecture 2: Algorithm Analysis pt.1

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Terminology

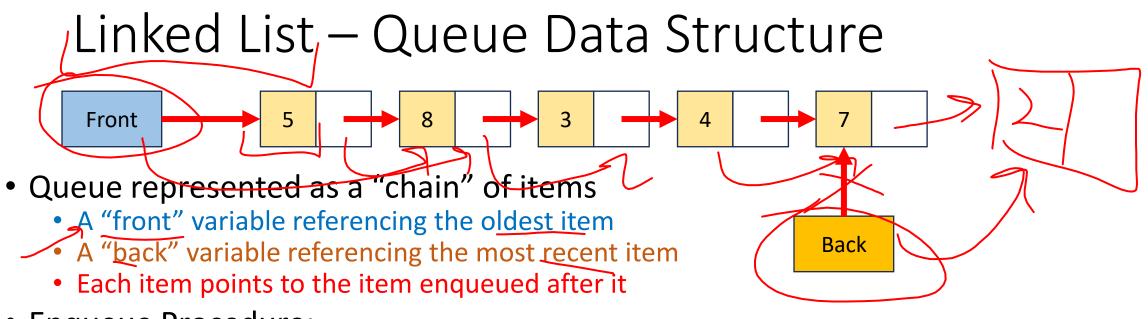
- Abstract Data Type (ADT)
 - Mathematical description of a "thing" with set of operations on that "thing"
- Algorithm
 - A high level, language-independent description of a step-by-step process

• Data structure

- A specific organization of data and family of algorithms for implementing an ADT
- Implementation of a data structure
 - A specific implementation in a specific language

ADT: Queue

- What is it?
 A "First In First Out" (FIFO) collection of items
- What Operations do we need?
 - Enqueue
 - Add a new item to the queue
 - Dequeue
 - Remove the "oldest" item from the queue
 - ls_empty
 - Indicate whether or not there are items still on the queue

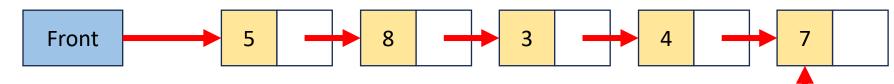


• Enqueue Procedure:

• Dequeue Procedure:

• Is_empty Procedure:

Linked List – Queue Data Structure



- Queue represented as a "chain" of items
 - A "front" variable referencing the oldest item
 - A "back" variable referencing the most recent item
 - Each item points to the item enqueued after it

• Enqueue Procedure: enqueue(x){

last = new Node(x) back.next = last back = last

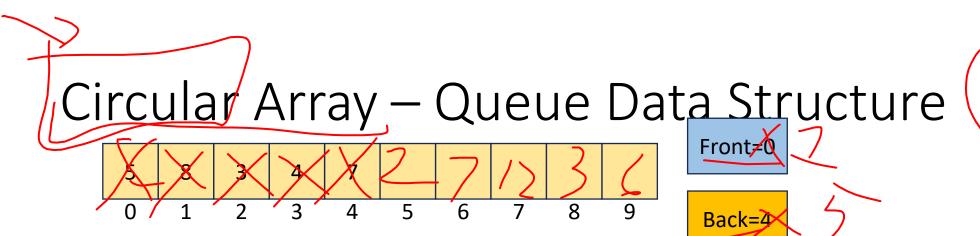
• Dequeue Procedure:

dequeue(){
 first = front.item
 front = front.next
 return first

• Is_empty Procedure: is_empty(){

return front.equals(Null)

Back

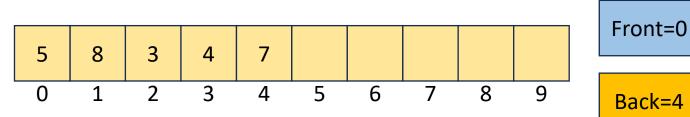


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- Enqueue Procedure:

• Dequeue Procedure:

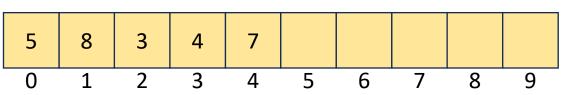
• Is_empty Procedure:

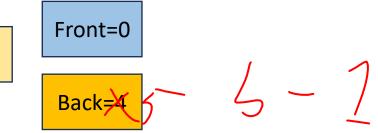
Circular Array – Queue Data Structure



- Queue represented as an array of items
 - A "front" index to indicate the oldest item in the queue
 - A "back" index to indicate the most recent item in the queue
- Enqueue Procedure:
- Dequeue Procedure:
- Is_empty Procedure:

Circular Array – Queue Data Structure





- Queue represented as an array of items
 - A "front" index to indicate the oldest item in the queue

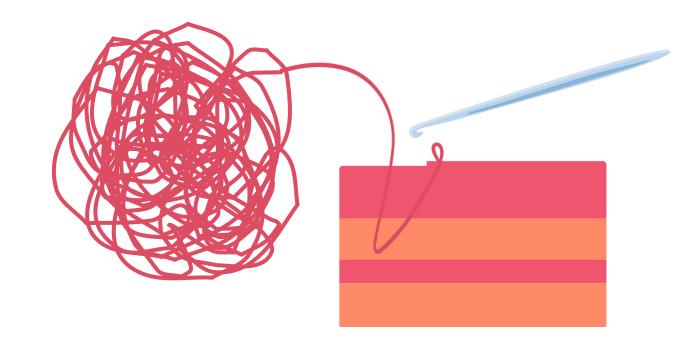
A "back" index to indicate the most recent item in the queue

Enqueue Procedure:
 Dequeue Procedure:
 dequeue(){
 first = queue[front]
 front = (front + 1) % queue.length
 }

 Is_empty Procedure:
 is_empty(){
 return front == back
 }

Linked List vs. Circular Array

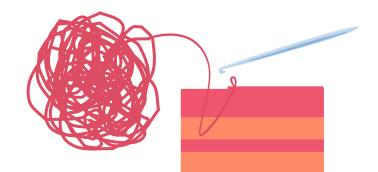
- Circular array: you need to pick the size
- If you wanted to do things other than the ADT operations (e.g. indexing) then CA is better
- LL maybe uses more space because it has the pointers
- CA might be more complex (resizing, modulus, etc)



Warm up:

- I have a pile of string
- I have one end of the string in-hand
- I need to find the other end in the pile
- How can I do this efficiently?

Algorithm Ideas

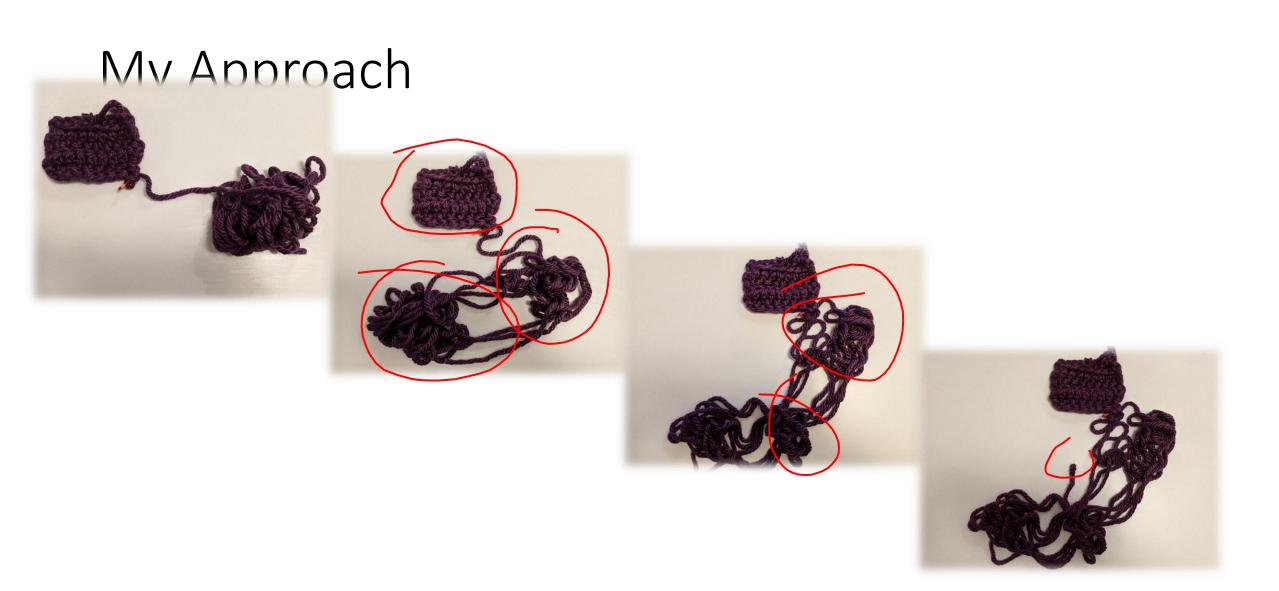


• Ideas:

Algorithm Running Times

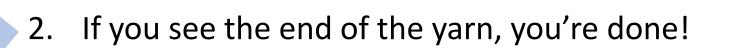
- How do we express running time? A C S
- Units of "time"
 How to express efficiency?

type: Yun LX, UM input: S. Ze ox inpux Dupput: Operation (outif



End-of-Yarn Finding

1. Set aside the already-obtained "beginning"



3. Separate the pile of yarn into 2 piles, note which connects to ______ the beginning (call it pile A, the other pile B)

B

Repeat on pile with end

4. Count the number of strands crossing the piles

5. If the count is even, pile A contains the end, else pile B does

Why Do resource Analysis?

- Allows us to compare *algorithms*, not implementations
 - Using observations necessarily couples the algorithm with its implementation
 - If my implementation on my computer takes more time than your implementation on your computer, we cannot conclude your algorithm is better
- We can predict an algorithm's running time before implementing
- Understand where the bottlenecks are in our algorithm

Goals for Algorithm Analysis

• Identify a *function* which maps the algorithm's input size to a measure of resources used

Input of the function: sizes of the input

- Number of characters in a string, number of items in a list, number of pixels in an image
- Output of the function: **counts** of resources used

Number of times the algorithm adds two numbers together, number times the algorithm
 does a or < comparison, maximum number of bytes of memory the algorithm uses at any time

• Important note: Make sure you know the "units" of your domain and codomain!

Worst Case Analysis (in general)

• If an algorithm has a worst case resource complexity of f(n)

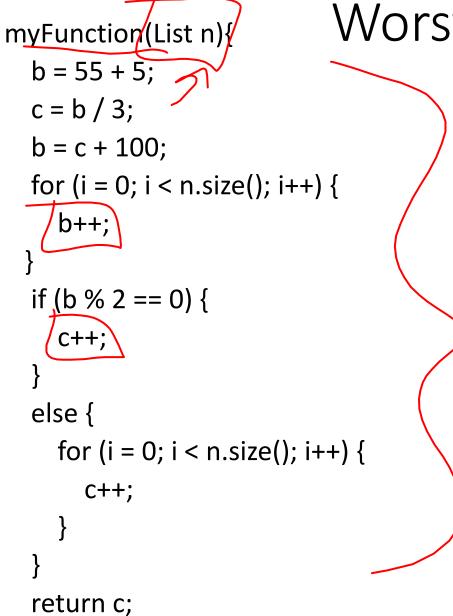
- Among all possible size-n inputs, the "worst" one will use f(n) "resources"
- I.e. f(n) gives the maximum count of resources needed from among all inputs of size n

Worst Case Running Time Analysis

- If an algorithm has a worst case running time of f(n)
 - Among all possible size- n_i inputs, the "worst" one will do f(n) "operations"
 - I.e. f(n) gives the maximum operation count from among all inputs of size n

Worst Case Space Analysis

- If an algorithm has a worst case space complexity of f(n)
 Among all possible size-n inputs, the "worst" one will need f(n) "memory units"
 - I.e. f(n) gives the maximum memory unit count from among all inputs of size n



Worst Case Running Time - Example

Questions to ask:

- What are the units of the input size?
- What are the operations we're counting?
- For each line:
 - How many times will it run?
 - How long does it take to run?
 - Does this change with the input size?

Worst Case Running Time – Example 2

```
beAnnoying(List n){
```

```
List m = [];
```

```
for (i=0; i < n.size(); i++){
```

m.add(n[i]);

```
for (j=0; j< n.size(); j++){
```

```
print ("Hi, I'm annoying");
```

Questions to ask:

- What are the units of the input size?
- What are the operations we're counting?
- For each line:
 - How many times will it run?
 - How long does it take to run?
 - Does this change with the input size?

```
return;
```

Worst Case Running Time – General Guide

- Add together the time of consecutive statements
- Loops: Sum up the time required through each iteration of the loop
 - If each takes the same time, then [time per loop × number of iterations]
- Conditionals: Sum together the time to check the condition and time of the slowest branch
- Function Calls: Time of the function's body
- Recursion: Solve a recurrence relation