CSE 341: Programming Languages

Spring 2006 Lecture 12 — Type Inference, Parametric Polymorphism, Type Constructors

Today

- We have learned an interesting subset of the ML expression language
- But we have been really informal about some aspects of the type system:
 - Type inference (what types do bindings implicitly have)
 - Type variables (what do 'a and 'b really mean)
 - Type constructors (why is int list a type but not list)
- Note: Type inference and parametric polymorphism are separate concepts that end up intertwined in ML. A different language could have one or the other.

Type Inference

Some languages are untyped or dynamically typed.

ML is *statically typed*; every binding has one type, determined during type-checking (compile-time).

ML is *implicitly typed*; programmers rarely need to write the types of bindings.

The type-inference question: Given a program without explicit types, produce types for all bindings such that the program type-checks, or reject (only) if it is impossible.

Whether type inference is easy, hard, or impossible depends on details of the type system: Making it more or less powerful (i.e., more programs typecheck) may make inference easier or harder.

ML Type Inference

- Determine types of bindings in order (earlier first) (except for mutual recursion)
- For each val or fun binding, analyze the binding to determine necessary facts about its type.
- Afterward, use *type variables* (e.g., 'a) for any unconstrained types in function arguments or results.
- Some extra details for type variables and references we'll mention later.

Amazing fact: For the ML type system, "going in order" this way never causes unnecessary rejection.

Example 1

```
fun f x =
  let val (y,z) = x in
      (Real.abs y) + z
  end
```

Example 2

```
fun sum lst =
   case lst of
   [] => 0
   | hd::tl => hd + (sum tl)
```

Example 3

fun compose (f,g,x) = f (g x)

Comments on ML type inference

- If we had subtyping, the "equality constraints" we generated would be unnecessarily restrictive.
- If we did not have type variables, we would not be able to give a type to compose until we saw how it was used.
 - But type variables are useful regardless of inference.
- Inference is why the following aren't really equivalent:
 - let val x = e1 in e2 end
 - (fn x => e2) e1

E.g., let's try $e^2 = (x \ 0, x \ "foo")$ and something simple for e^1 like fn y => y:

- let val $x = (fn y \Rightarrow y)$ in (x 0, x "foo") end

$$- (fn x \Rightarrow (x 0, x "foo")) (fn y \Rightarrow y)$$

The latter gives a type error ...

Parametric polymorphism

Fancy words for "forall-types". Coming to next version of Java, C#, VB, etc. Sometimes called generics. A bit like C++ templates if C++ didn't have operator-overloading.

In principle, just two new kinds of types:

Given an expression of type forall 'tv. t, we can *instantiate* it at type t2 to get an expression of type "t with 'tv replaced by t2"

```
Example: We can instantiate
forall 'a. forall 'b. ('a * 'b) -> ('b * 'a)
with string for 'a and int->int for 'b to get
(string * (int->int)) -> ((int->int) * string)
```

ML-style polymorphism

The ML type system is actually more restrictive:

- "forall" must appear "all the way on the outside-left"
- So it's implicit; no way to write the words "for all"

Example: ('a * 'b) -> ('b * 'a) means forall 'a. forall 'b. ('a * 'b) -> ('b * 'a) Non-example: There's no way to have a type like int -> (forall 'a. 'a -> int)

Versus Subtyping

Compare

fun swap (x,y) = (y,x) (* ('a * 'b) -> ('b * 'a) *)with

class Pair { Object x; Object y; ... }
Pair swap(Pair pr) { return new Pair(pr.y, pr.x); }
ML wins in two ways (for this example):

- Caller instantiates types, so doesn't need to cast result
- Callee cannot return a pair of any two objects.

Containers

Parametric polymorphism (forall types) are also the right thing for containers (lists, sets, hashtables, etc.) where elements have the same type.

Example: ML lists

val :: : ('a * ('a list)) -> 'a list (* infix is syntax *)
val map : (('a -> 'b) * ('a list)) -> 'b list
val sum : int list -> int
val fold : ('a * 'b -> 'b) -> 'b -> ('a list) -> 'b

list is a type *constructor*, not a type; if t is a type, then t list is a type.

User-defined type constructors

Language-design: don't provide a fixed set of a useful thing.

Let programmers declare type constructors.

Examples:

You can have multiple type-parameters (not shown here).

And now, finally, everything about lists is syntactic sugar!