

Today

- Continue examples of functions taking and returning other functions
- Discuss *free variables* in function bodies
- In general, discuss environments and lexical scope
- See key idioms using first-class functions (more next time)

If you remember one thing...

We evaluate expressions in an evironment, and function bodies in <u>an environment</u> extended to map arguments to values.

But which one? *The environment in which the function was defined!* An equivalent description:

- Functions are values, but they're not just code.
- fun f p = e and fn p => e evaluate to values with two parts (a "pair"): the code and the current environment
- Function application evaluates the "pair"'s function body in the "pair"'s environment (extended)
- This "pair" is called a *(function) closure*.

There are *lots* of good reasons for this semantics.

For hw, exams, and competent programming, you must "get this"

Example 1

```
val x = 1
fun f y = x + y
val x = 2
val y = 3
val z = f (x+y)
```

Example 2

```
val x = 1
fun f y = let val x = 2 in fn z => x + y + z end
val x = 3
val g = f 4
val y = 5
val z = g 6
```

Example 3

```
fun f g = let val x = 3 in g 2 end
val x = 4
fun h y = x + y
val z = f h
```

Scope

A key language concept: how are user-defined things *resolved*?

We have seen that ML has *lexically scoped* variables?

Another (more-antiquated-for-variables, sometimes-useful) approach is *dynamic scope*

Example of dynamic scope: Exception handlers (where does raise (in Java throw) transfer control?)

Why lexical scope?

- 1. Functions can be reasoned about (defined, type-checked, etc.) where defined
- 2. Function meaning not related to choice of variable names
- 3. "Closing over" local variables creates private data; function definer *knows* function users cannot affect it

Example:

fun add_ $2x x = fn z \Rightarrow z + x + x$

fun $add_{2x} x = let val y = x + x in fn z => z + y end$

Key idioms with closures

- Create similar functions
- Combine functions
- Pass functions with private data to iterators (map, *fold*, ...)
- Provide an ADT
- Partially apply functions ("currying")
- As a *callback* without the "wrong side" specifying the environment.

(Will go through these today and Friday. See lec8.sml for examples for first three idioms.)

```
In all cases, a closure's "private fields" (i.e., free variables) are essential.
```

Why Google cares about functional iterators

Remember MapReduce? (fold is a slightly cleaner variant of reduce.) Often the client of fold does not care what order the data is combined

- True for all 3 examples using fold in lec8.sml.
- Not true in general (e.g., is list sorted)

So what if we had *huge* arrays of data and 1000s of computers.

- Provide map for huge arrays of data; run in parallel
- Provide reduce for combining results; run in parallel then combine results across computers

Example: How many web pages have the phrase "Converse hightops"? Example: Is "hightop" or "high-top" more common on the Web?

Key separation: MapReduce is a sophisticated fault-tolerant distributed system. Users (490H) just call map and reduce on some data.

<u>Fault-Tolerance</u>

At data-center scales, computers fail or become disconnected or start running too slow very often.

• If 1 computer has a hardware crash once every year on average, how long before 1 out of 10000 computers crash?

So part of MapReduce is redoing the computation parts that were given to a computer that fails.

But when can you take a computation, run it more than once, and know that's the same as running it exactly once?

When you do not use mutation!

A "new" style of programming: Computation in terms of maps and folds instead of sequences of assignment statements.

• Not new at all of course, just new to BusinessWeek. :-)