# CSE341: Programming Languages 

# Lecture 8 <br> Lexical Scope and Function Closures 

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## Very important concept

- We know function bodies can use any bindings in scope
- But now that functions can be passed around: In scope where?


## Where the function was defined (not where it was called)

- There are lots of good reasons for this semantics
- Discussed after explaining what the semantics is
- For HW, exams, and competent programming, you must "get this"
- This semantics is called lexical scope


## Example

Demonstrates lexical scope even without higher-order functions:

$$
\begin{aligned}
& (* 1 *) \operatorname{val} x=1 \\
& (* 2 *) \text { fun } f y=x+y \\
& (* 2 *) \operatorname{val} x=3 \\
& (* 4 *) \operatorname{val} y=4 \\
& (* 5 *) \operatorname{val} z=f(x+y)
\end{aligned}
$$

- Line 2 defines a function that, when called, evaluates body $\mathbf{x + y}$ in environment where $\mathbf{x}$ maps to 1 and $\mathbf{y}$ maps to the argument
- Call on line 5:
- Looks up $f$ to get the function defined on line 2
- Evaluates $\mathbf{x + y}$ in current environment, producing 7
- Calls the function, which evaluates the body in the old environment, producing 8


## Closures

How can functions be evaluated in old environments that aren't around anymore?

- The language implementation keeps them around as necessary

Can define the semantics of functions as follows:

- A function value has two parts
- The code (obviously)
- The environment that was current when the function was defined
- This is a "pair" but unlike ML pairs, you cannot access the pieces
- All you can do is call this "pair"
- This pair is called a function closure
- A call evaluates the code part in the environment part (extended with the function argument)


## Example

$$
\begin{aligned}
& (* 1 *) \text { val } x=1 \\
& (* 2 *) \text { fun } f y=x+y \\
& (* 3 *) \text { val } x=3 \\
& (* 4 *) \text { val } y=4 \\
& \left(\begin{array}{ll}
* & 4
\end{array}\right) \text { val } z=f(x+y)
\end{aligned}
$$

- Line 2 creates a closure and binds f to it:
- Code: "take y and have body x+y"
- Environment: "x maps to 1 "
- (Plus whatever else is in scope, including $\mathbf{f}$ for recursion)


## So what?

Now you know the rule. Next steps:

- (Silly) examples to demonstrate how the rule works for higherorder functions
- Why the other natural rule, dynamic scope, is a bad idea
- Powerful idioms with higher-order functions that use this rule
- This lecture: Passing functions to iterators like filter
- Next lecture: Several more idioms


## Example: Returning a function

$$
\begin{aligned}
& \left(\begin{array}{ll}
* & *
\end{array}\right) \text { val } x=1 \\
& (* 2 *) \text { fun } f y= \\
& (* 2 a *) \\
& (* 2 b *) \\
& \text { let val } x=y+1 \\
& (* 3 *) \text { val } x=3 \\
& (* 4 *) \text { val } g=f 4 \\
& (* 5 *) \text { val } y=5 \\
& (* 6 *) \text { val } z=96
\end{aligned}
$$

- Trust the rule: Evaluating line 4 binds to $g$ to a closure:
- Code: "take z and have body $\mathbf{x + y + z "}$
- Environment: "y maps to 4, x maps to 5 (shadowing), ..."
- So this closure will always add 9 to its argument
- So line 6 binds 15 to $\mathbf{z}$


## Example: Passing a function

```
(* 1 *) fun \(f\) g = (* call arg with 2 *)
(* 1a *) let val x = 3
(* 1b *) in g 2 end
(* 2 *) val \(\mathrm{x}=4\)
(* 3 *) fun \(h y=x+y\)
(* 4 *) val \(z=f\) h
```

- Trust the rule: Evaluating line 3 binds h to a closure:
- Code: "take y and have body x+y"
- Environment: "x maps to 4, f maps to a closure, ..."
- So this closure will always add 4 to its argument
- So line 4 binds 6 to $\mathbf{z}$
- Line 1a is as stupid and irrelevant as it should be


## Why lexical scope?

1. Function meaning does not depend on variable names used

Example: Can change body to use $q$ instead of $\mathbf{x}$

- Lexical scope: it can't matter
- Dynamic scope: Depends how result is used

$$
\begin{aligned}
& \text { fun } f y= \\
& \quad \text { let val } x=y+1 \\
& \text { in fn } z=>x+y+z \text { end }
\end{aligned}
$$

Example: Can remove unused variables

- Dynamic scope: But maybe some g uses it (weird)

$$
\begin{aligned}
& \text { fun } \mathrm{f} g= \\
& \text { let val } \mathrm{x}=3 \\
& \text { in } \mathrm{g} 2 \text { end }
\end{aligned}
$$

## Why lexical scope?

2. Functions can be type-checked \& reasoned about where defined

Example: Dynamic scope tries to add a string and an unbound variable to 6

$$
\begin{aligned}
& \text { val } x=1 \\
& \text { fun } f y= \\
& \quad \text { let val } x=y+1 \\
& \text { in fn } z=>\times+y+z \text { end } \\
& \text { val } x=\text { hi" } \\
& \text { val } g=f 4 \\
& \text { val } z=96
\end{aligned}
$$

## Why lexical scope?

3. Closures can easily store the data they need

- Many more examples and idioms to come

```
fun greaterThanX x = fn y => y > x
fun filter (f,xs) =
    case xs of
        [] => []
    | x::xs => if f x
    then x::(filter(f,xs))
    else filter(f,xs)
```

fun noNegatives xs = filter (greaterThanX ~1, xs)

## Does dynamic scope exist?

- Lexical scope for variables is definitely the right default
- Very common across languages
- Dynamic scope is occasionally convenient in some situations
- So some languages (e.g., Racket) have special ways to do it
- But most don't bother
- If you squint some, exception handling is more like dynamic scope:
- raise e transfers control to the current innermost handler
- Does not have to be syntactically inside a handle expression (and usually isn't)


## Recomputation

These both work and rely on using variables in the environment

```
fun allShorterThan1 (xs,s) =
    filter(fn x => String.size x < String.size s,
        xs)
fun allShorterThan2 (xs,s) =
    let val i = String.size s
    in filter(fn x => String.size x < i, xs) end
```

The first one computes String.size once per element of $\mathbf{x s}$ The second one computes String.size s once per list

- Nothing new here: let-bindings are evaluated when encountered and function bodies evaluated when called


## Iterators made better

- Functions like map and filter are much more powerful thanks to closures and lexical scope
- Function passed in can use any "private" data in its environment
- Iterator "doesn't even know the data is there" or what type it has


## Another famous function: Fold

fold (and synonyms / close relatives reduce, inject, etc.) is another very famous iterator over recursive structures

Accumulates an answer by repeatedly applying f to answer so far

- fold(f,acc,[x1,x2,x3,x4]) computes $\mathrm{f}(\mathrm{f}(\mathrm{f}(\mathrm{f}(\mathrm{acc}, \mathrm{x} 1), \mathrm{x} 2), \mathrm{x} 3), \mathrm{x} 4)$

```
fun fold (f,acc,xs) =
    case xs of
        [] => acc
    | x::xs => fold(f, f(acc,x), xs)
```

- This version "folds left"; another version "folds right"
- Whether the direction matters depends on $\mathbf{f}$ (often not)

```
val fold = fn : ('a * 'b -> 'a) * 'a * 'b list -> 'a
```


## Examples with fold

These are useful and do not use "private data"

```
fun f1 xs = fold((fn (x,y) => x+y), 0, xs)
fun f2 xs = fold((fn (x,y) => x andalso y>=0),
    true, xs)
```

These are useful and do use "private data"

```
fun f3 (xs,hi,lo) =
    fold(fn (x,y) =>
        x + (if y >= lo andalso y <= hi
        then 1
        else 0)),
        0, xs)
fun f4 (g,xs) = fold(fn (x,y) => x andalso g y),
    true, xs)
```


## Why iterators again?

- These "iterator-like" functions are not built into the language
- Just a programming pattern
- Though many languages have built-in support, which often allows stopping early without using exceptions
- This pattern separates recursive traversal from data processing
- Can reuse same traversal for different data processing
- Can reuse same data processing for different data structures

