

### List Review

- Build lists: [], ::, and shorthand [e1,e2,...,en]
- Use lists: null, hd, tl
- Types: Each list has elements of the same type. Examples: int list

```
(int*int) list
```

```
((int*int) list) list
```

- So what are the typing rules for [], ::, null, hd, and tl?
- Functions that build or use lists are usually recursive
  - And/or use other recursive functions
  - Elegant algorithms by "thinking high-level" (e.g., append)

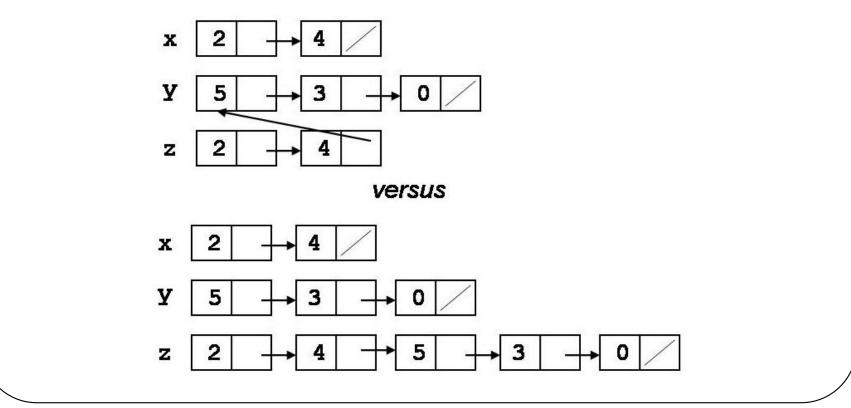
### Sharing

Recall append([2,4],[5,3,0]) evaluates to [2,4,5,3,0].

```
Similarly, t1 [9,7,4,2] evaluates to [7,4,2].
```

Do the results *share*, i.e., *alias* the arguments?

Example: val x=[2,4]; val y=[5,3,0]; val z=append(x,y)



### Sharing, good or bad?

Java programmer's view:

- A never-ending *obsession* with what is shared. This obsession is *necessary* because everything is mutable.
- Sharing is wrong if you don't want a mutation of "one list" to "affect the other" and right if you do.
- So sometimes make copies just to avoid sharing in case some other code might do a mutation.

### Sharing, good or bad?

ML programmer's view:

- It is actually *impossible* to tell if there is sharing or not!
- So stop worrying and just write append; all lists [2,4,5,3,0] behave the same no matter what they do or do not share with.
- Amount of sharing is just a "space optimization"
  - Usually good to share.
  - tl shares, which makes it very fast (O(1)).

# Let bindings

Motivation: Functions without local variables can be poor style and/or really inefficient.

Syntax: let b1 b2 ... bn in e end where each bi is a *binding*.

Typing rules: Type-check each bi and e in context including previous bindings. Type of whole expression is type of e.

Evaluation rules: Evaluate each bi and e in environment including previous bindings. Value of whole expression is result of evaluating e.

Elegant design worth repeating:

- Let-expressions can appear anywhere an expression can.
- Let-expressions can have any kind of binding.
  - Local functions can refer to any bindings *in scope*.
  - Better style than passing around unchanging arguments.

#### More than style

Exercise: hand-evaluate bad\_max and good\_max for lists, [3,2,1], [1,2], and [1,2,3].

Moral: Repeating expensive (recursive) computations is not just bad style; it is the wrong algorithm performance-wise.

## Options

"Options are like lists that can have at most one element."

- Create a t option with NONE or SOME e where e has type t.
- Use a t option with isSome and valOf

Why not just use lists? An interesting style trade-off:

- Options better express purpose, enforce invariants on callers, maybe faster.
- But cannot use functions for lists already written.

### Summary and general pattern

Major progress: recursive functions, pairs, lists, let-expressions, options

Each has a syntax, typing rules, evaluation rules.

Functions, pairs, lists, and options are very different, but we can describe them in the same way:

- How do you create values?
  - function definition; pair expressions; [] and ::; NONE and SOME
- How do you use values?
  - function application; #1 and #2; null, hd, and tl; isSome and valOf

Soon: much better ways to use pairs and lists (pattern-matching)